

# The Grid-Based Path Planning Competition

-or-

Contractions, contractions everywhere

Nathan R. Sturtevant  
University of Denver

Symposium on Combinatorial Search  
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UNIVERSITY *of*  
DENVER

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DANIEL FELIX RITCHIE SCHOOL OF  
ENGINEERING & COMPUTER SCIENCE

# Testing Heuristics: We Have It All Wrong

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May 1995



# Testing Heuristics

- Suppose: bright idea for a new algorithm



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- Test on a standard set of benchmark problems





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- Suppose: bright idea for a new algorithm
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- Approach “spawns a host of evils”



# Complaints



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- The emphasis on competition is fundamentally antiintellectual
  - Does not build the sort of insight...(for)...more effective algorithms



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- The emphasis on competition is fundamentally antiintellectual
  - Does not build the sort of insight...(for)...more effective algorithms
- Competition diverts time and resources from productive investigation
  - Hours spent crafting the fastest possible code



# Example

- 2nd DIMACS challenge
  - Studied SAT problems
  - Stimulated great interest
  - Difficult to know why one approach is better
- Studies which tease out why approaches work without performance increase are hard to publish, but important intellectually



# Conclusion

- New norms for research:
  - “That experimental results be evaluated on the basis of whether they contribute to our understanding rather than whether they show that the authors algorithm can win a race with the state of the art.”
  - Algorithm researchers shouldn’t have the “burden of exhibiting faster and better algorithms in each paper.”

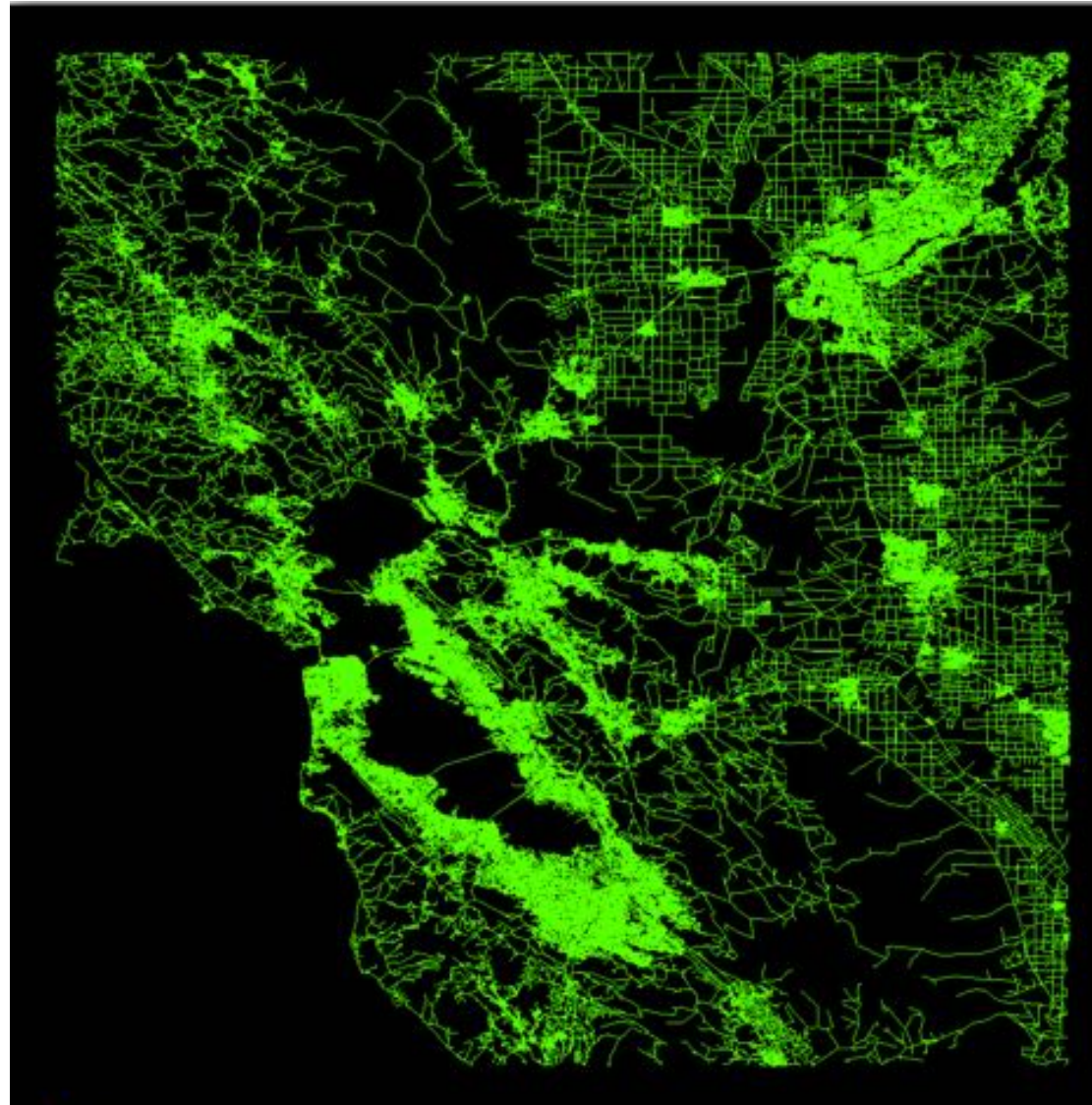


# Talk Goals

- Present latest GPPC results
- Present insights into commonalities in approaches
- Discuss future challenges

# Recent (related) example

- 9th DIMACS challenge
  - Begun in 2005
  - Path planning on road networks





# Result of Challenge

- Road networks for testing made available
  - 200k to 24 million nodes
  - 700k to 60 million edges



# Result of Challenge

- **Better Heuristics:**

- Computing the shortest path: A search meets graph theory [Goldberg & Harrelson, 2005]

- **Better Bounding:**

- Better Landmarks Within Reach [Goldberg et. al., 2007]

- **Exploiting Structure:**

- In Transit to Constant Time Shortest-Path Queries in Road Networks [Bast et. al. 2007]
- Contraction Hierarchies: Faster and Simpler Hierarchical Routing in Road Networks [Geisberger et. al. 2008]
- A Hub-Based Labeling Algorithm for Shortest Paths in Road Networks [Abraham et. al., 2011]

- **Theoretical Justification:**

- Highway Dimension, Shortest Paths, and Provably Efficient Algorithms [Abraham et. al., 2010]

# Observation

Benchmark data spurs research

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Imperfect benchmarks are better than no benchmarks.

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Imperfect benchmarks are better than no benchmarks.

You have to have (flawed) benchmarks before  
you can fix/improve them.



# Grid Map Benchmarks

- Between Fall 2006 - Dec. 2008  
consulted with BioWare on Dragon  
Age: Origins



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  - They agreed to allow free distribution of map data!
- Combined with other sources to form the “movingai” grid map repository
  - [Sturtevant, 2012]





# Grid-Based Path Planning Competition

- Started in 2012; goals to:
  - Improve evaluation
  - Establish metrics
  - Improve comparisons

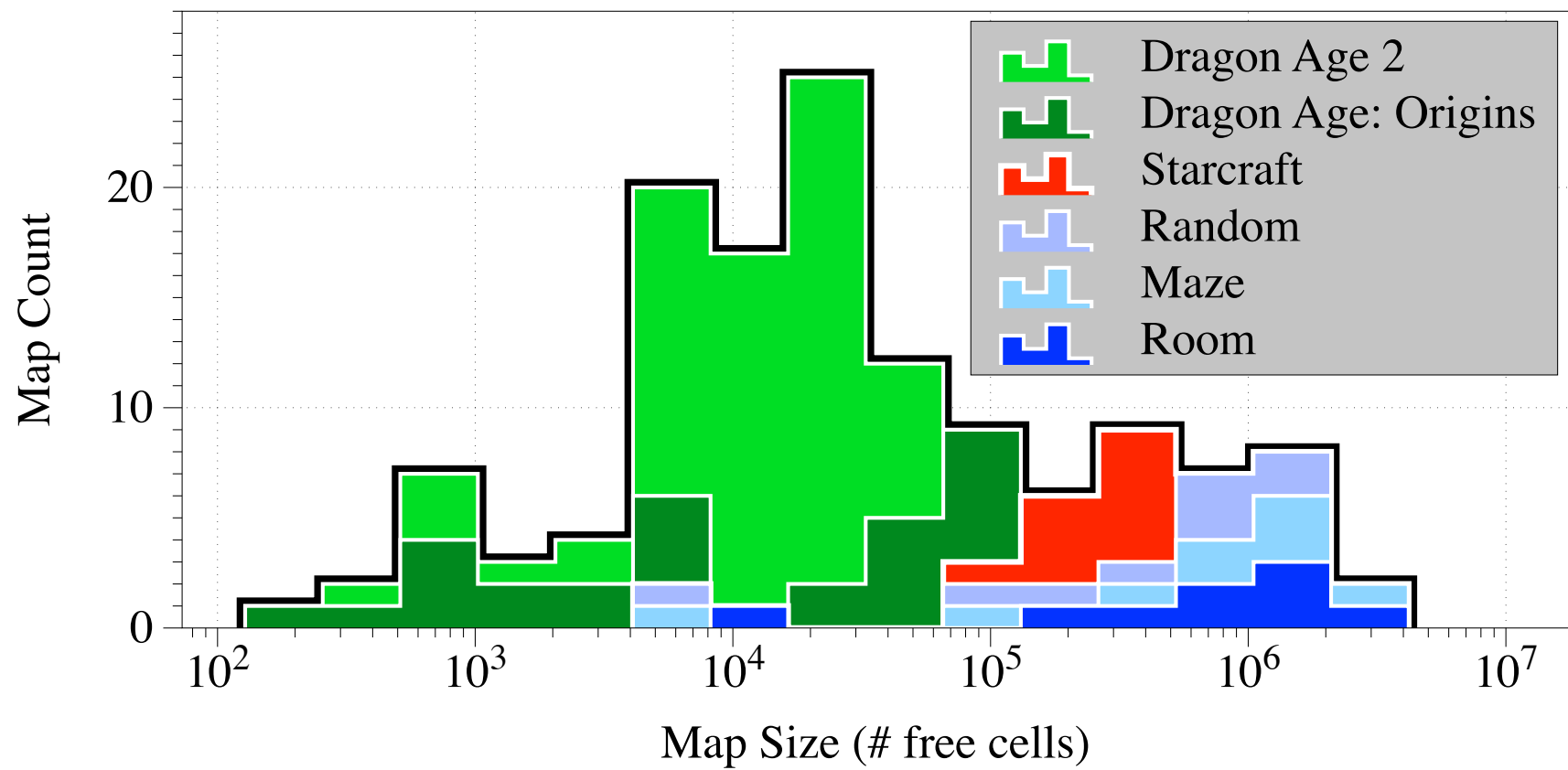


# Entry Specification

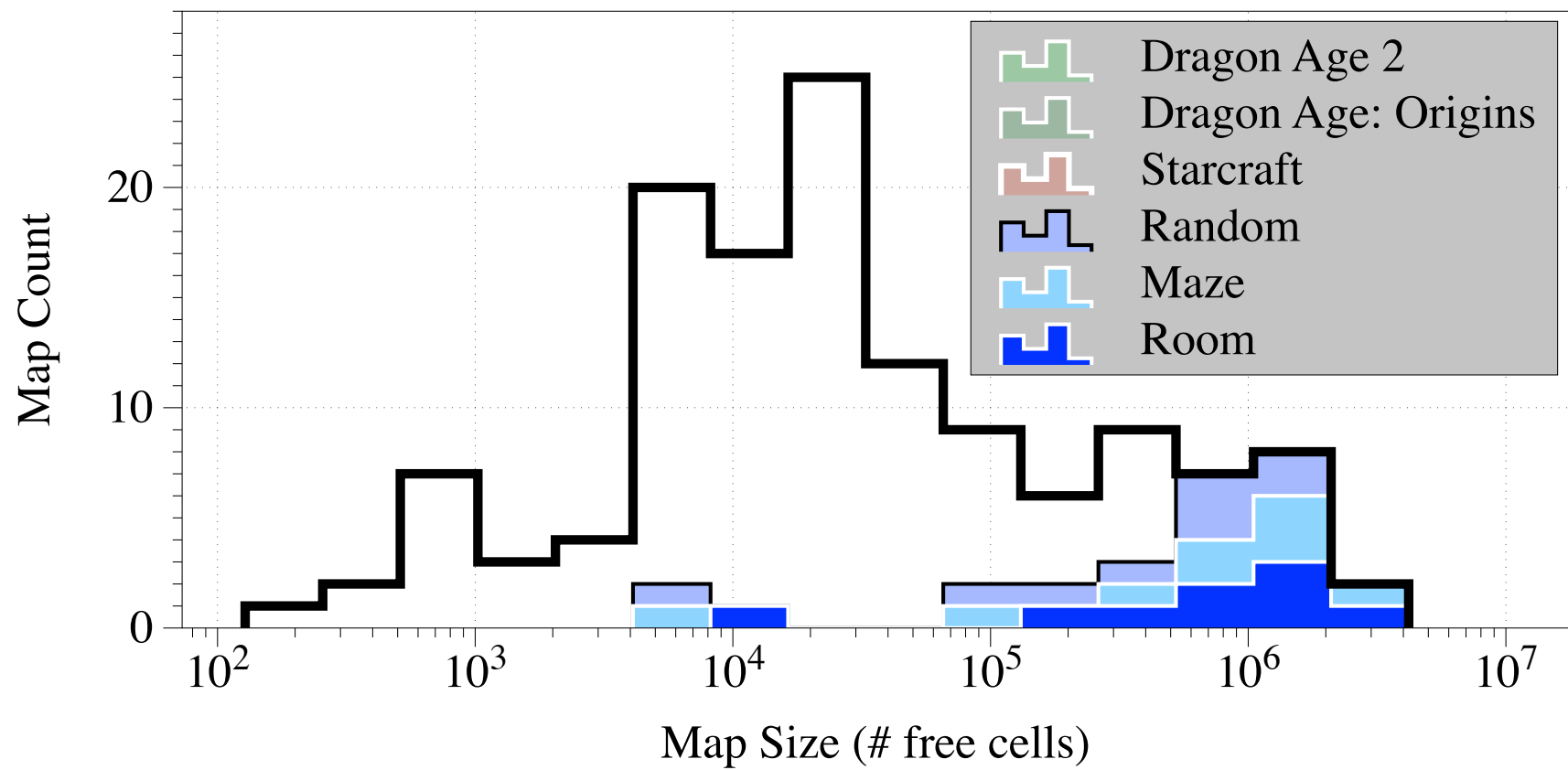
- Time allowed for pre-processing
- At runtime:
  - Load pre-processed data
  - Path query (start, goal) given to entry
    - Entry returns full or partial path
    - Query repeated until full path returned
- Run 5 times for statistical significance

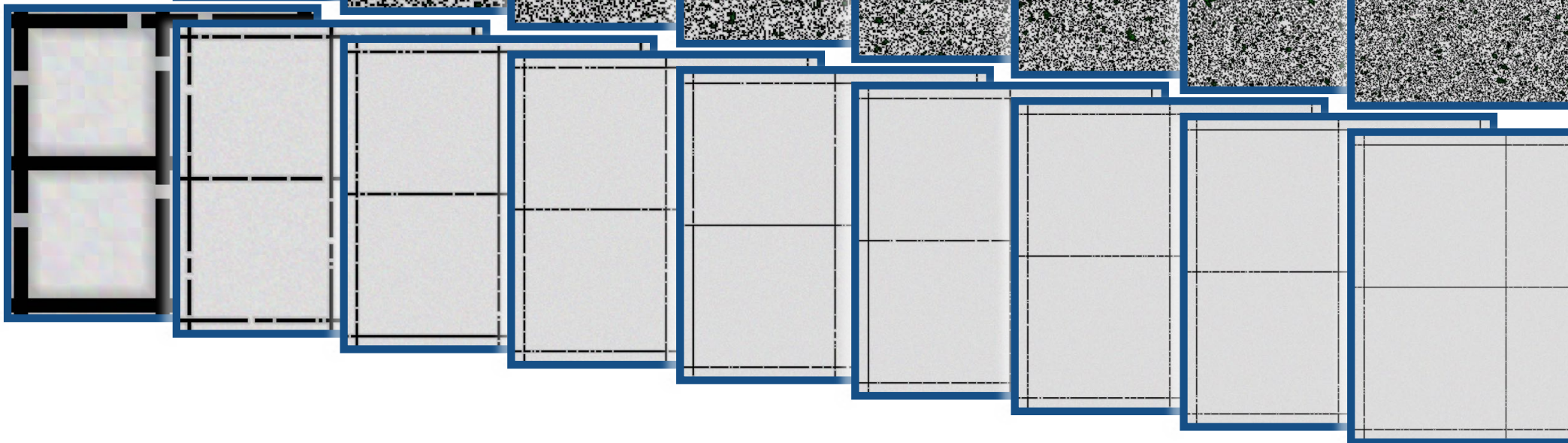
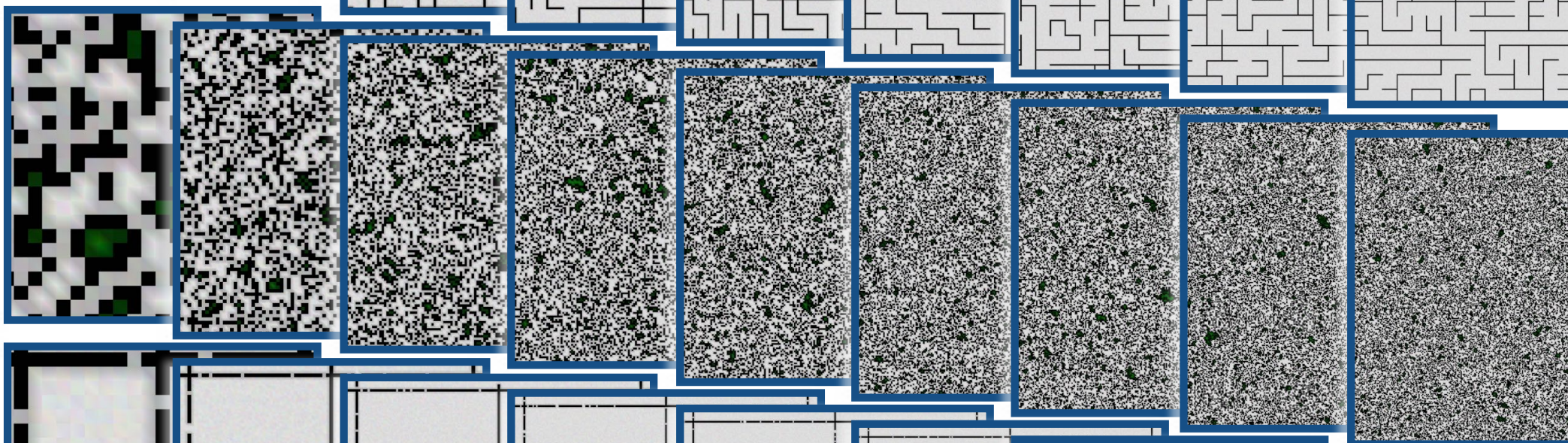
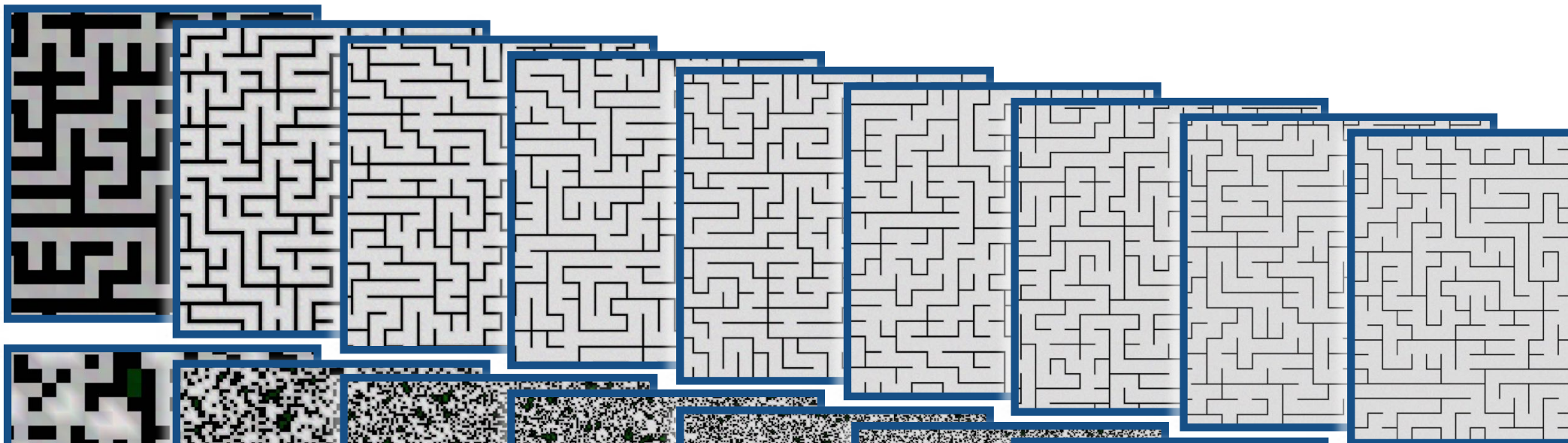
# Problem Setup

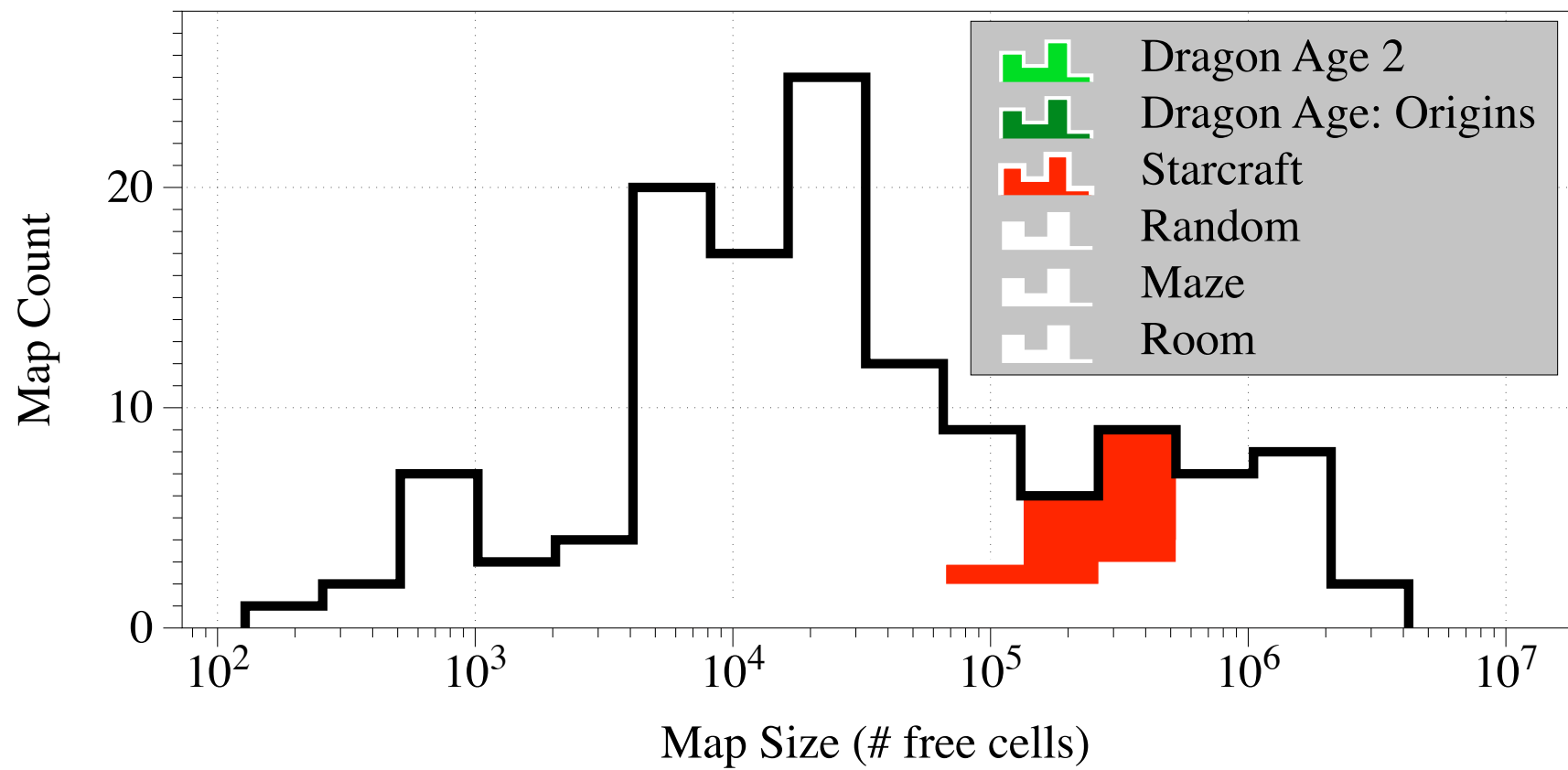
Source	# Maps	# Problems
Starcraft	11	29,970
Dragon Age: Origins	27	44,414
Dragon Age 2	57	54,360
Mazes	18	145,976
Random	18	32,228
Rooms	18	27,130
Total	132	347,868



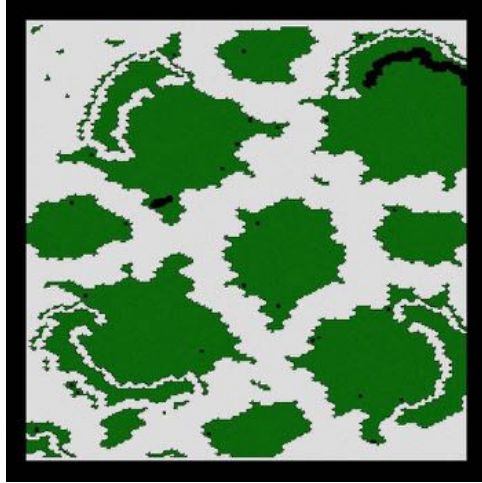
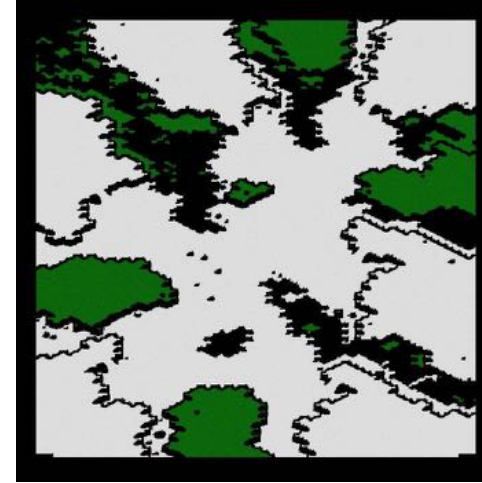
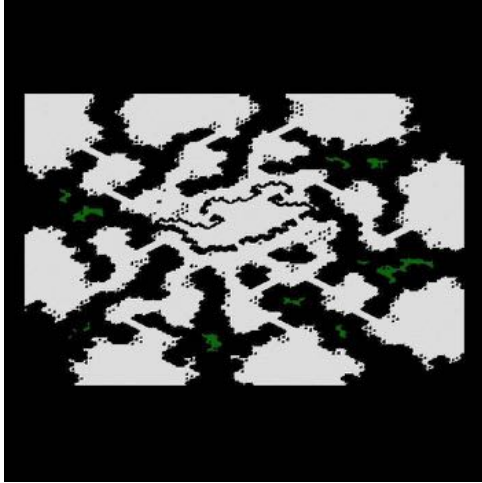
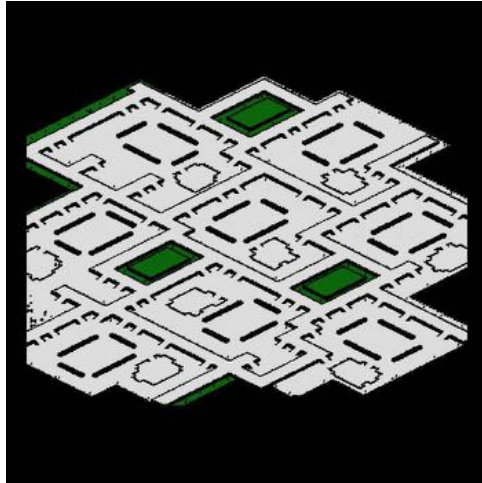
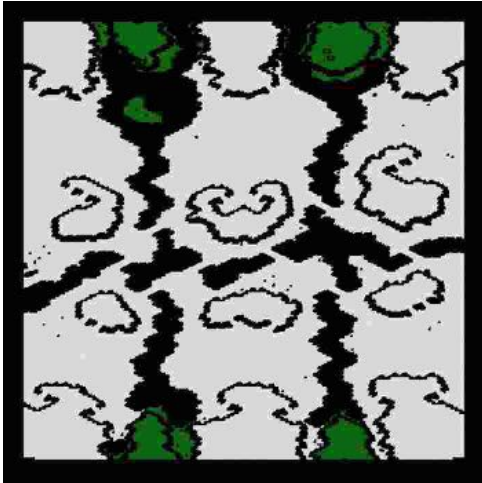
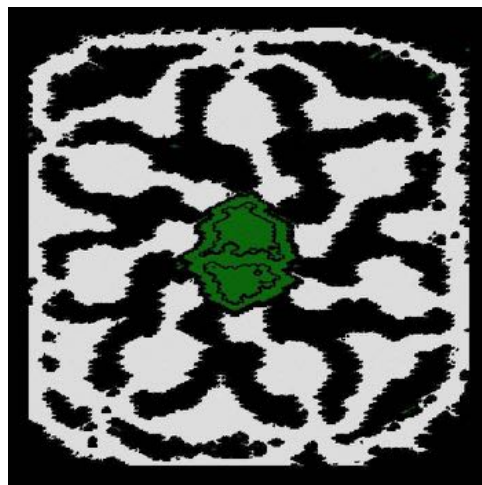
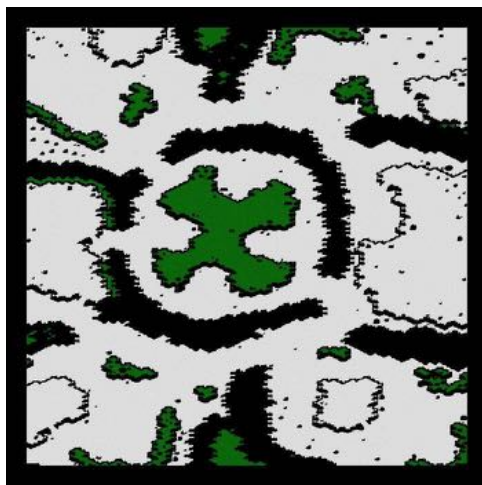
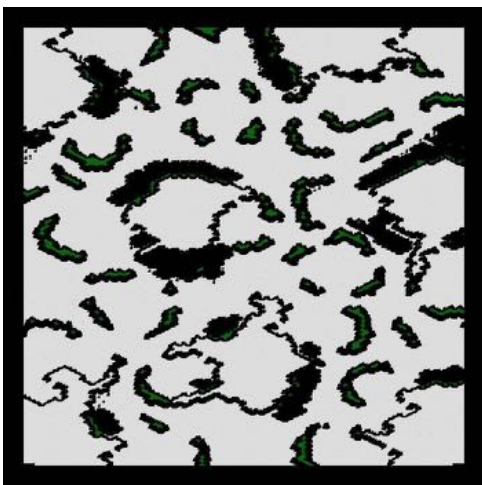
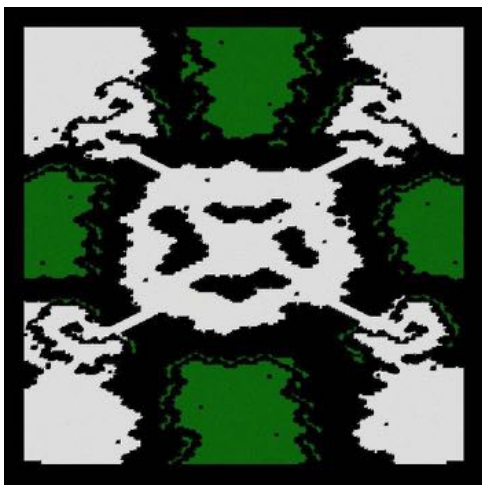


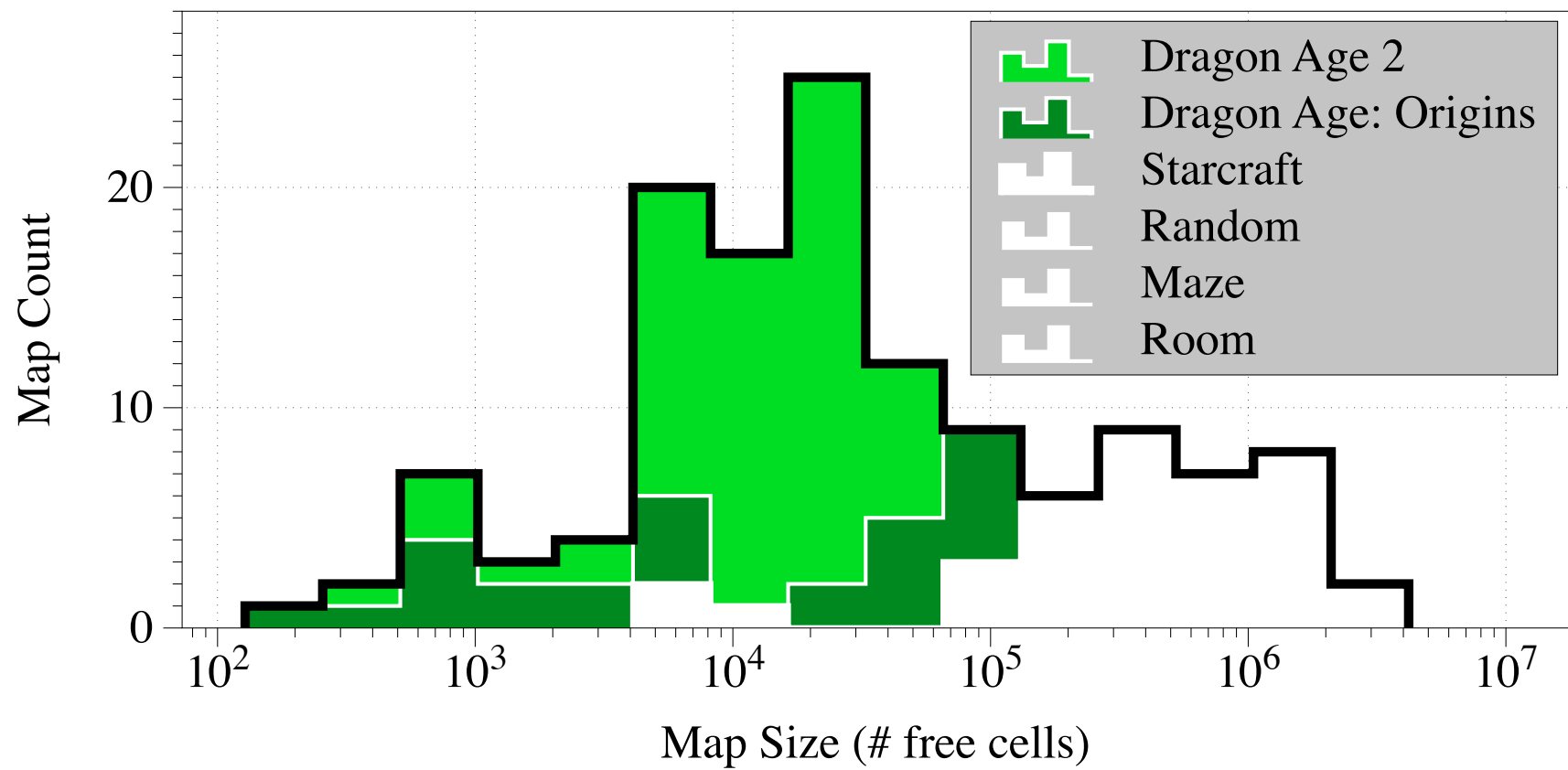


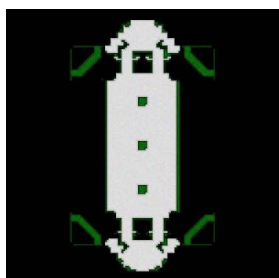
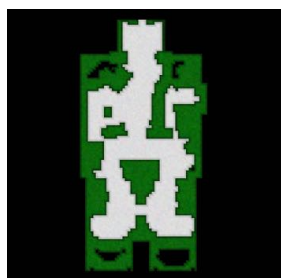
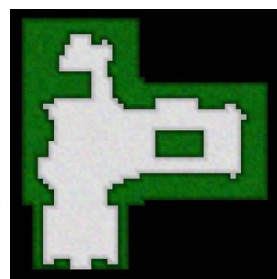
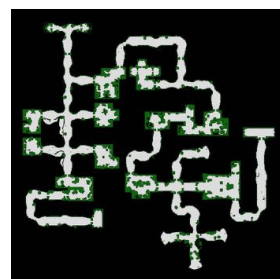
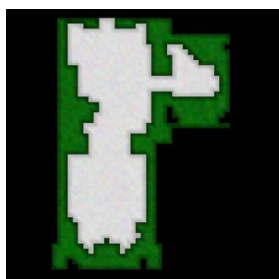
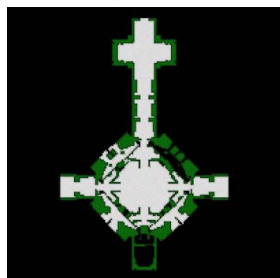
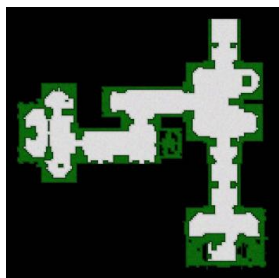
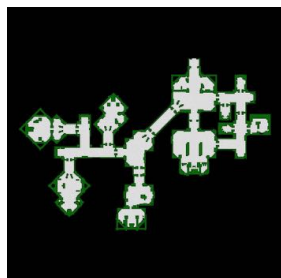
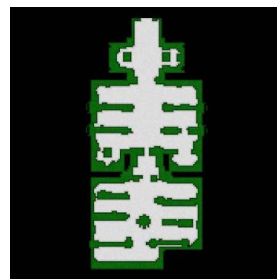
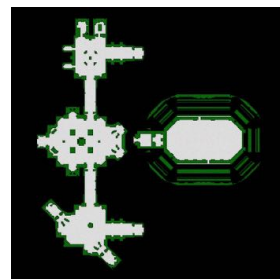
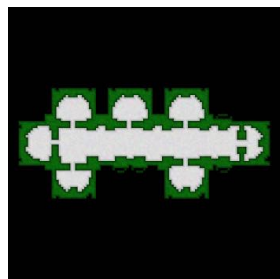
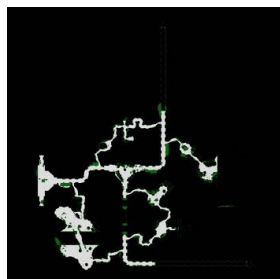
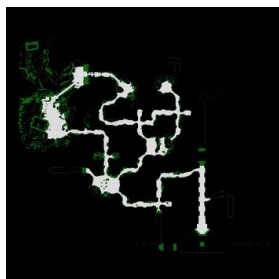
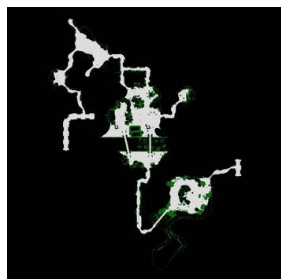
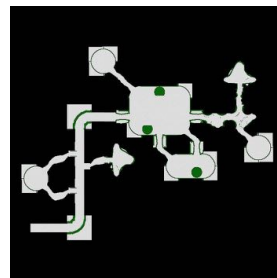
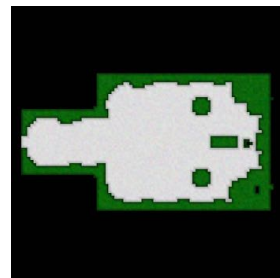
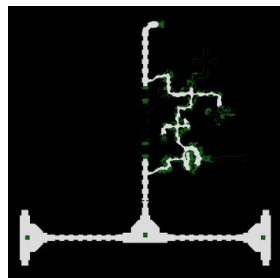
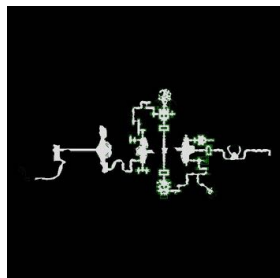
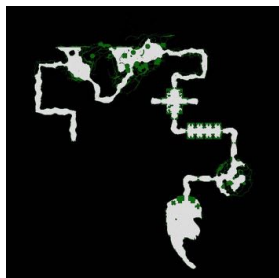
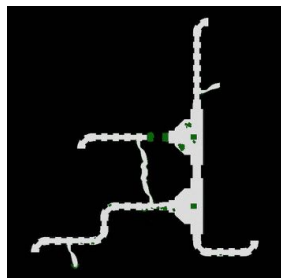




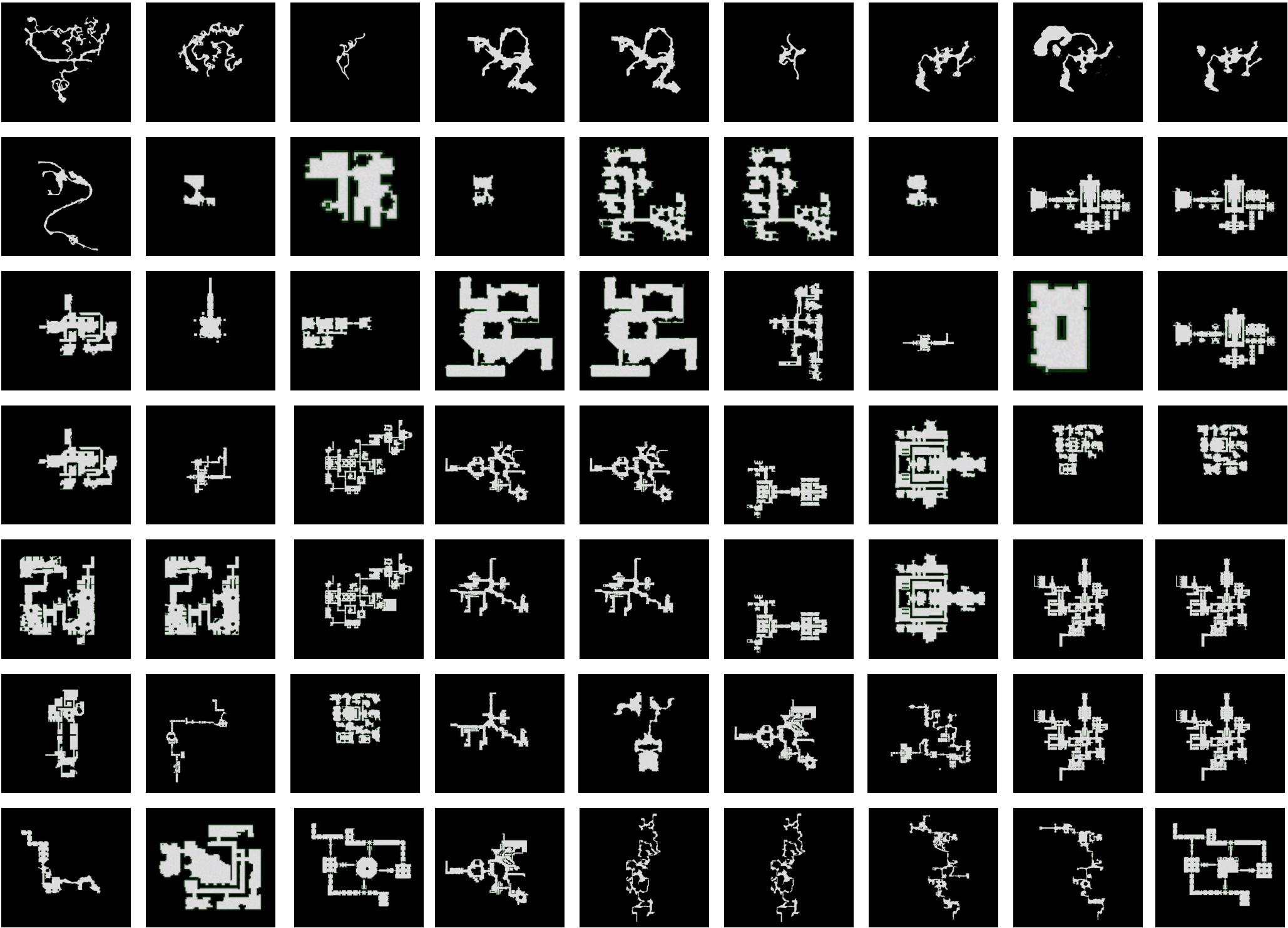














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- Time for 20 steps (real-time startup)



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- Maximum segment time (real-time steady state)



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- Disk storage



# Metrics

- Total/average time to solve problem set
- Time for 20 steps (real-time startup)
- Maximum segment time (real-time steady state)
- Suboptimality
- Correctness
- RAM at runtime (before/after)
- Disk storage
- Pre-computation



# All 2014 Approaches

- Single-Row Compression (SRC) (4 variants)





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- JPS+, JPS+ Bucket, A\* Bucket
- BLJPS (2 variants), BLJPS\_Subgoal
- Relaxed A\*, Relaxed A\* Subgoal

# Single Row Compression

- Ben Strasser [KIT], Adi Botea [IBM Dublin], and Daniel Harabor [NICTA]
  - Build full all-pairs-shortest-path data
  - Run-length encoding to compress each row
  - Incremental or non-incremental path generation
- *Fast First-Move Queries through Run-Length Encoding, Strasser, Harabor and Botea (2014)*
- *Complexity Results for Compressing Optimal Paths, Botea, Strasser and Harabor (2015)*

# Contraction Hierarchies

- Ben Strasser [KIT]
  - Originally developed by [Geisberger et. al. 2008]
  - Wasn't optimized for grids [Sturtevant and Geisberger, 2010]
  - Later optimization for grids [Storandt, 2013]
- *Contraction Hierarchies: Faster and Simpler Hierarchical Routing in Road Networks, Robert Geisberger, Peter Sanders, Dominik Schultes and Daniel Delling, 2008*

# N-level Subgoals

- Tansel Uras and Sven Koenig [USC]
  - 3rd entry into GPPC
  - Builds a n-level hierarchy from the basic subgoal approach
  - Basic subgoals are built up from visibility graphs
- *Identifying Hierarchies for Fast Optimal Search, Uras and Koenig, 2014*





# JPS+

- Steve Rabin [Digipen & Games Industry\*]
  - Independently invented JPS+
  - Based on Jump Point Search
- *Improving Jump Point Search, Daniel Harabor and Alban Grastien, 2014*
- *Online Graph Pruning for Pathfinding On Grid Maps, Daniel Harabor and Alban Grastien, 2011*



# BLJPS

- Jason Traish and James Tulip [Charles Sturt University]
- Boundary Lookup JPS
- Alternate optimization similar to JPS+
  - Also applied ideas to subgoals
- *Optimization using Boundary Lookup Jump Point Search, Traish and Tulip, 2015*



# Relaxed A\*

- <http://www.iroboapp.org/>
- Doesn't perform A\* re-expansions & other optimizations
  - Also applied to subgoal search

# Results



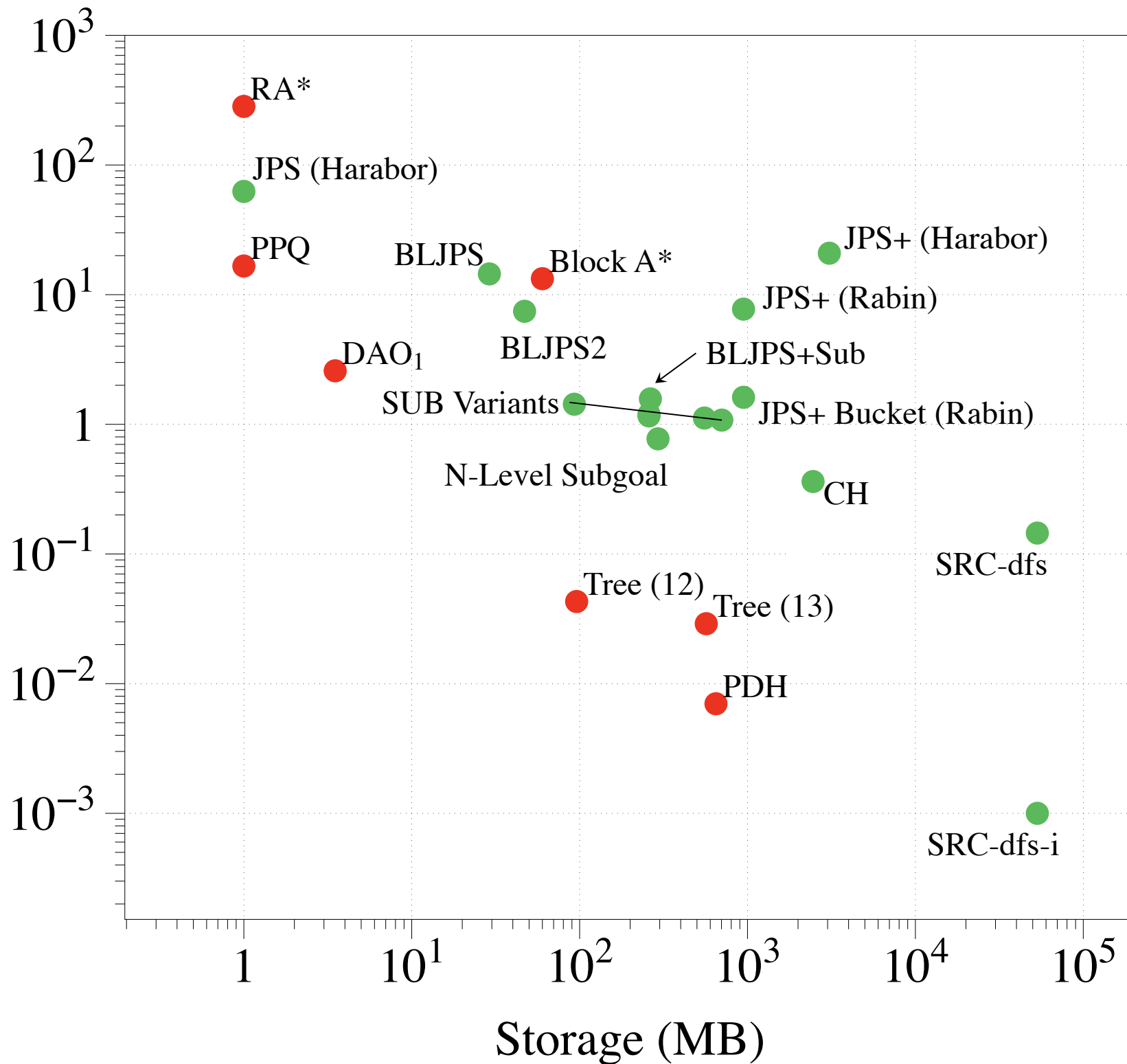
# Non-Dominated Approaches

- RA\*, RA\* Subgoal
- BLJPS, BLJPS2
- N-level Subgoals
- Contraction Hierarchies (CH)
- Single-Row Compression (SRC) (2 variants)

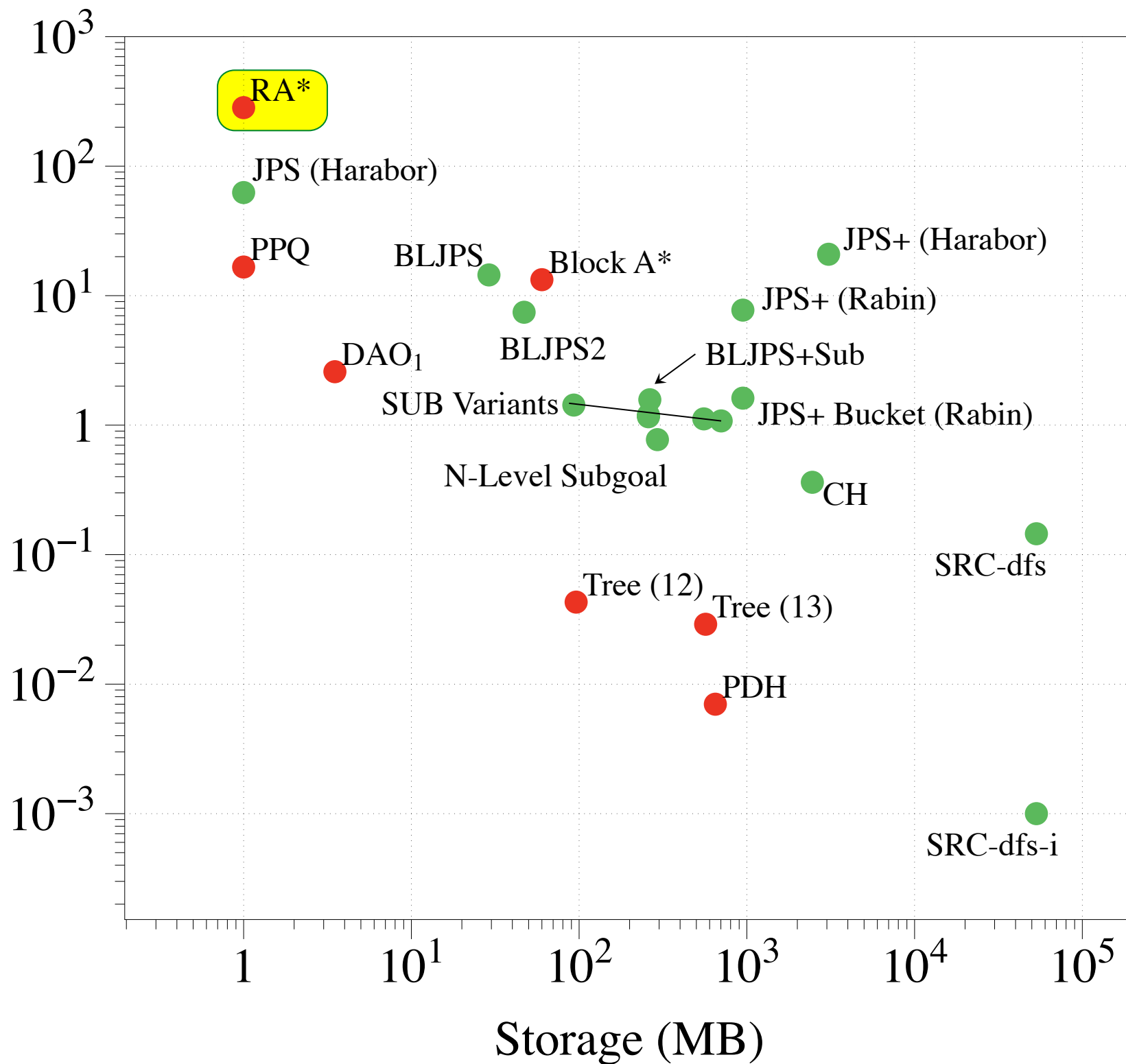
# Speed vs Storage (2014)

Entry	Average (ms)	Storage
RA*	282.995	0
BLJPS	14.453	20 MB
BLJPS2	7.444	47 MB
RA* Subgoal	1.688	264 MB
NSubgoal	0.773	293 MB
CH	0.362	2.4 GB
SRC-dfs	0.145	28 GB

Max Time per Segment (ms)

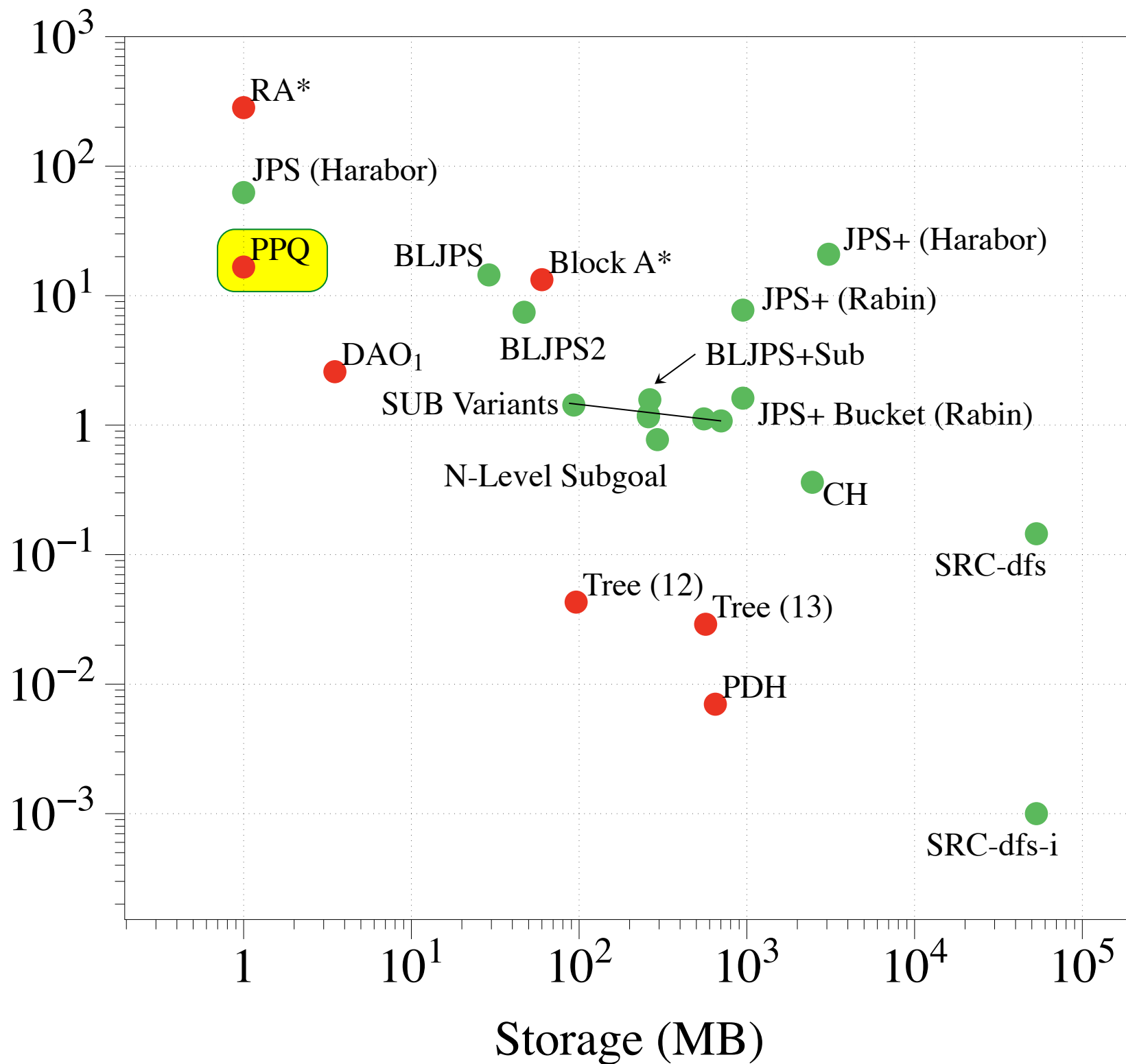


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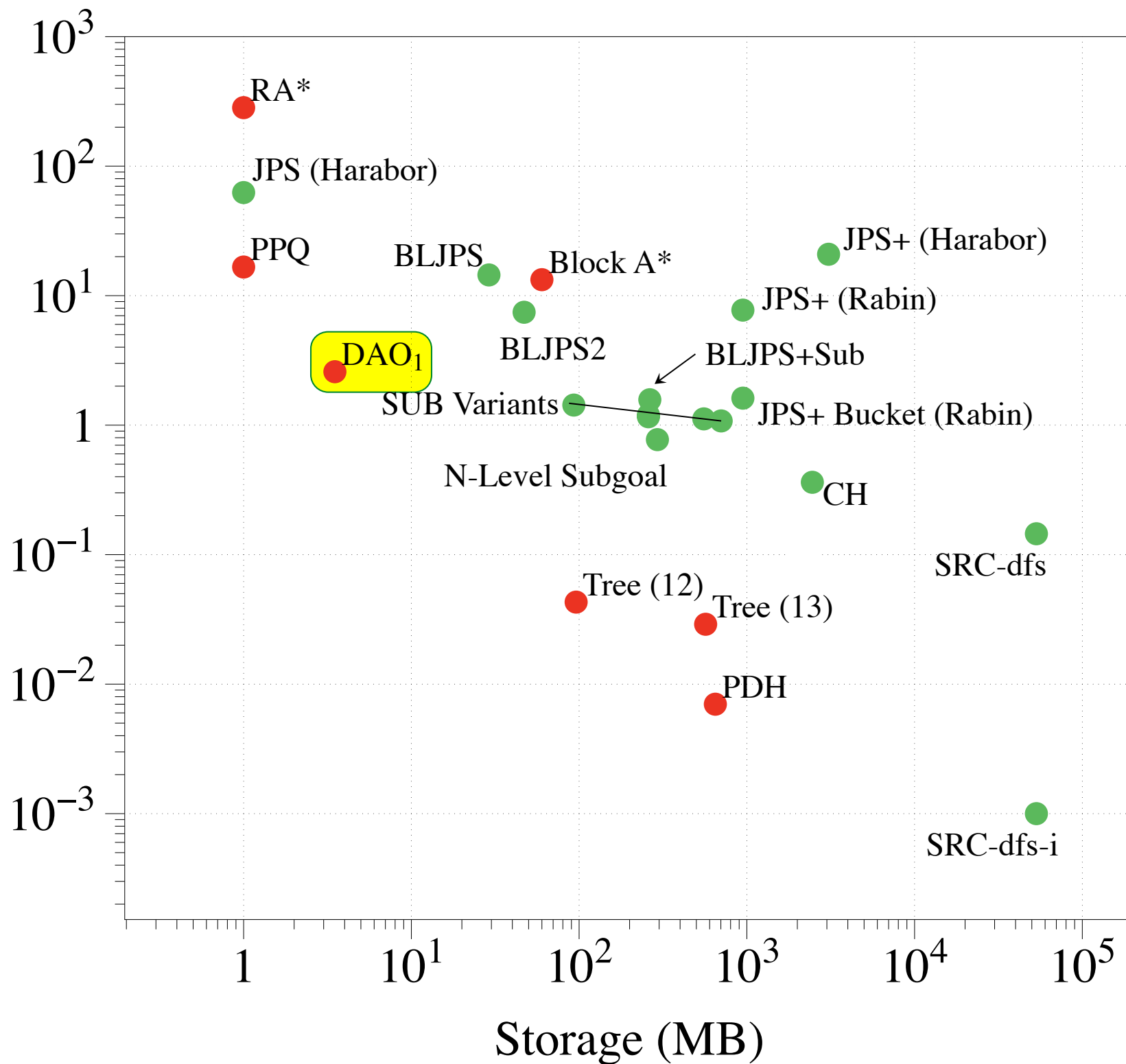




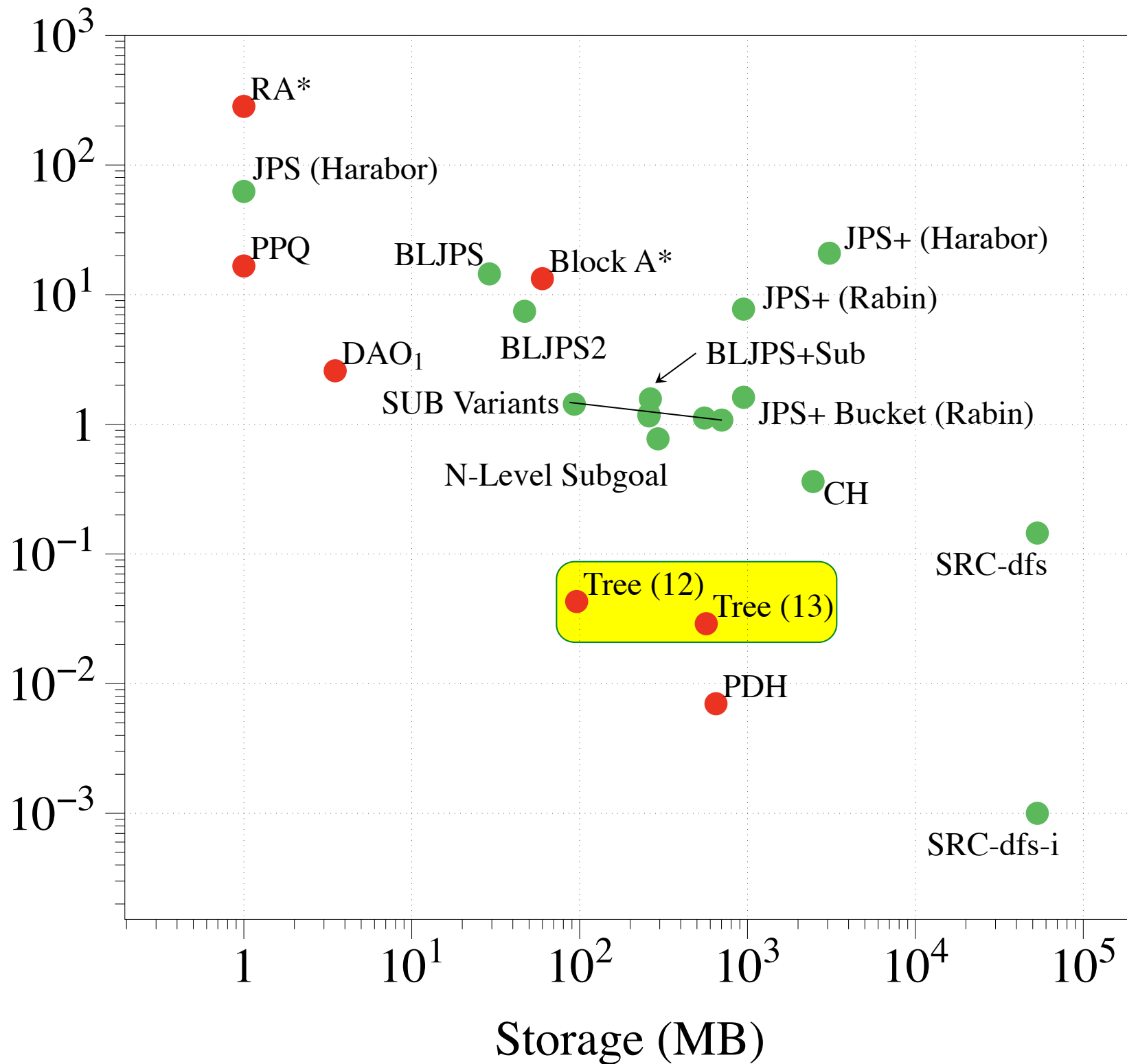
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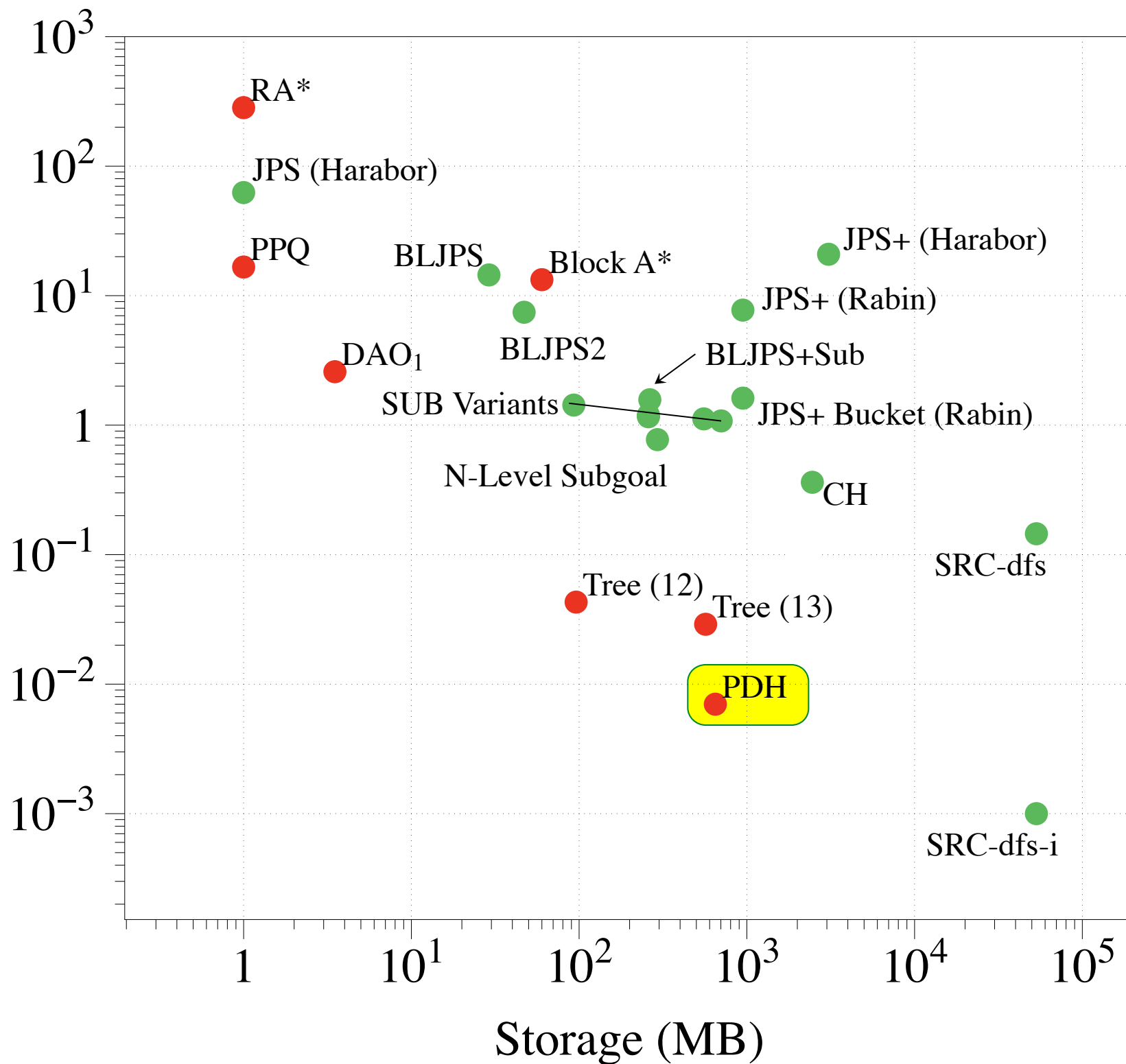
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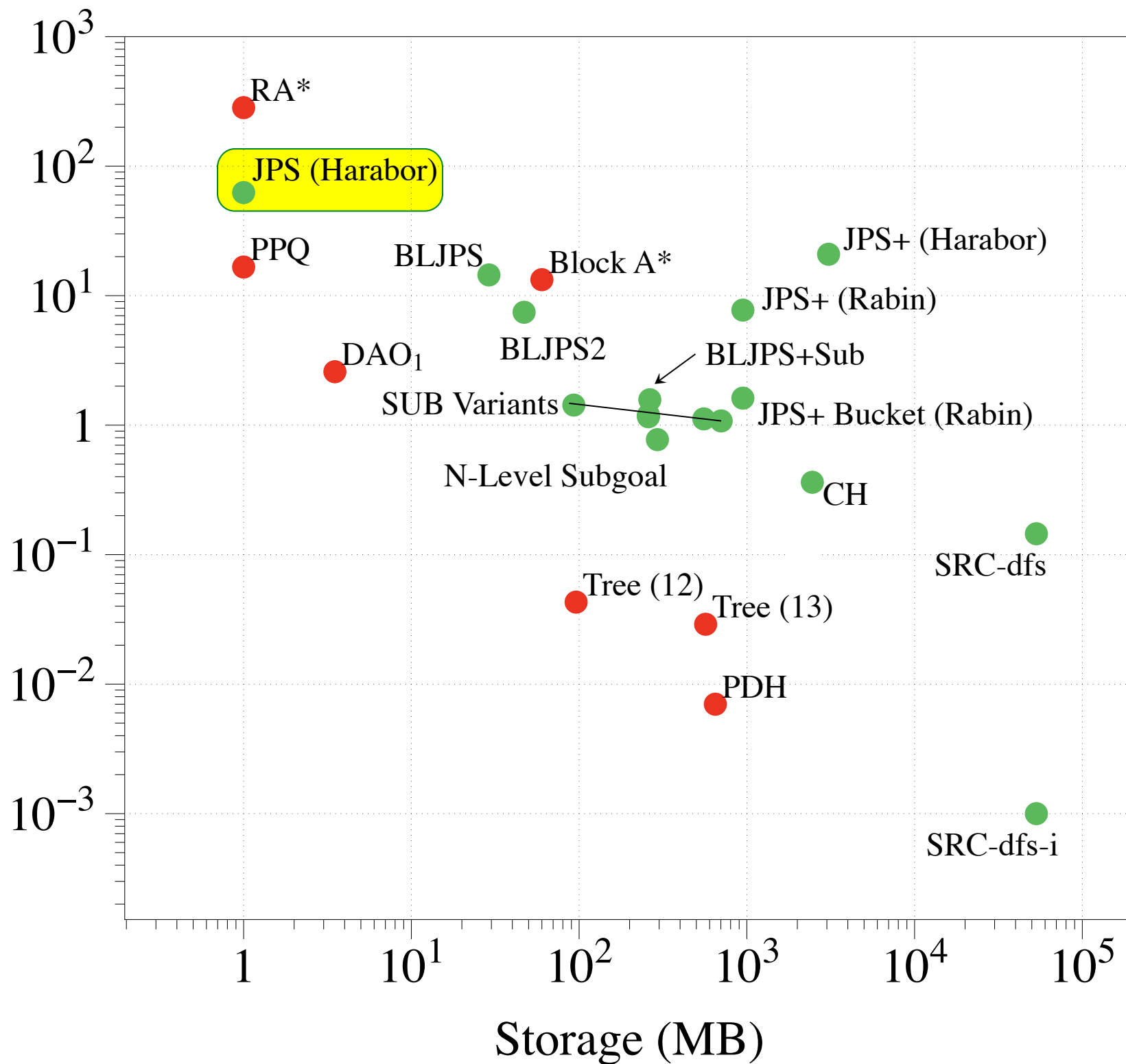
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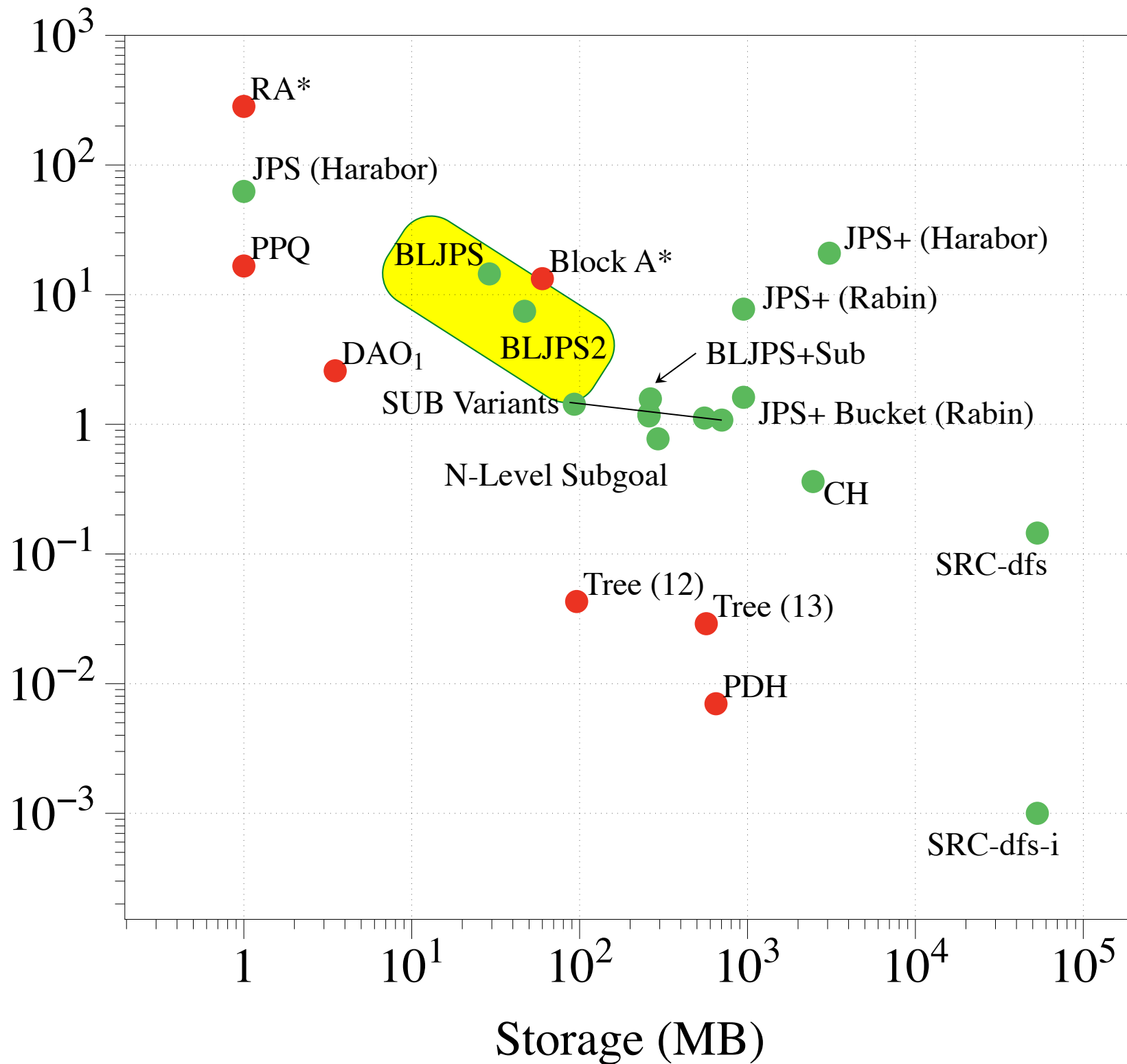
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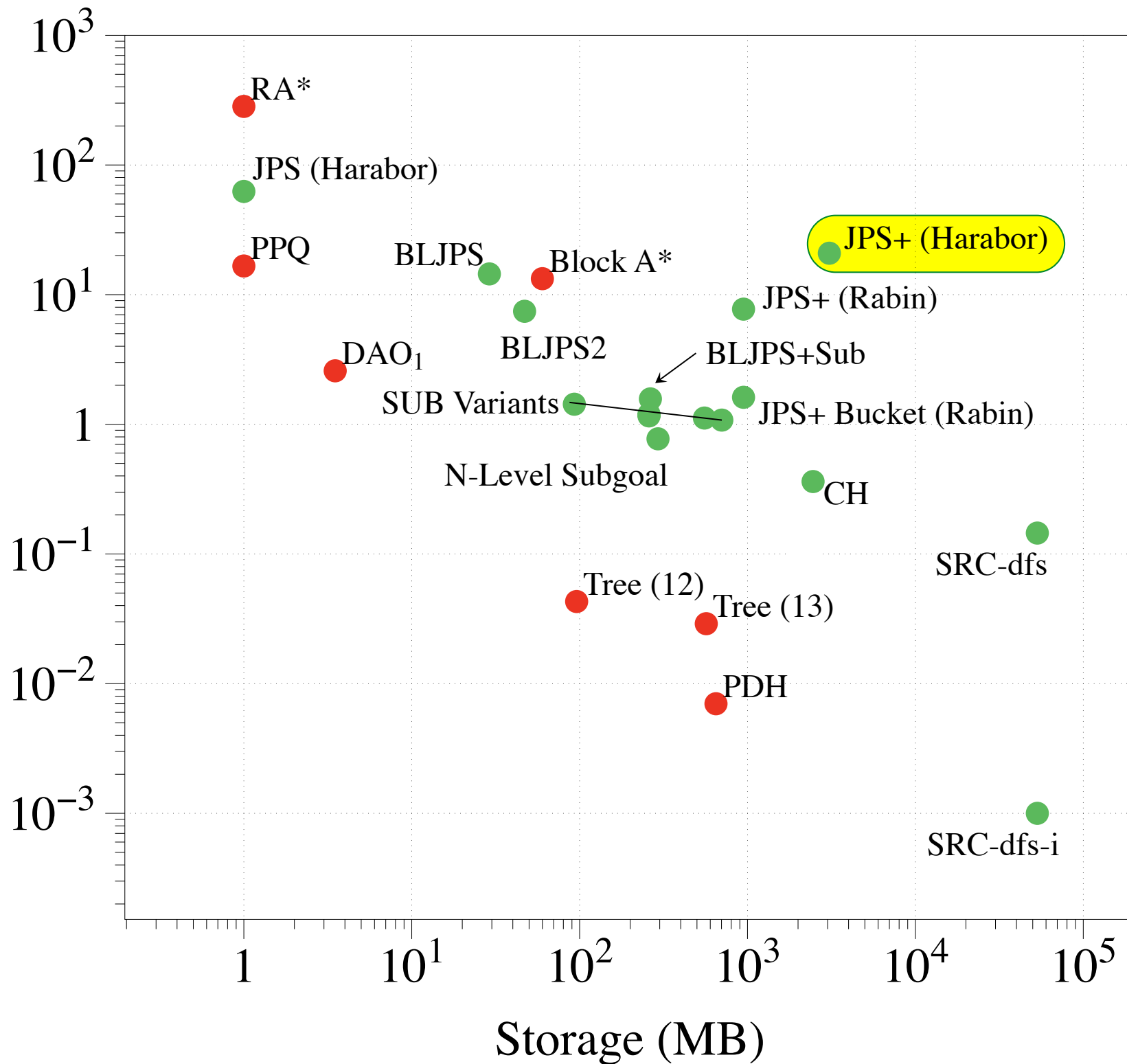
Max Time per Segment (ms)



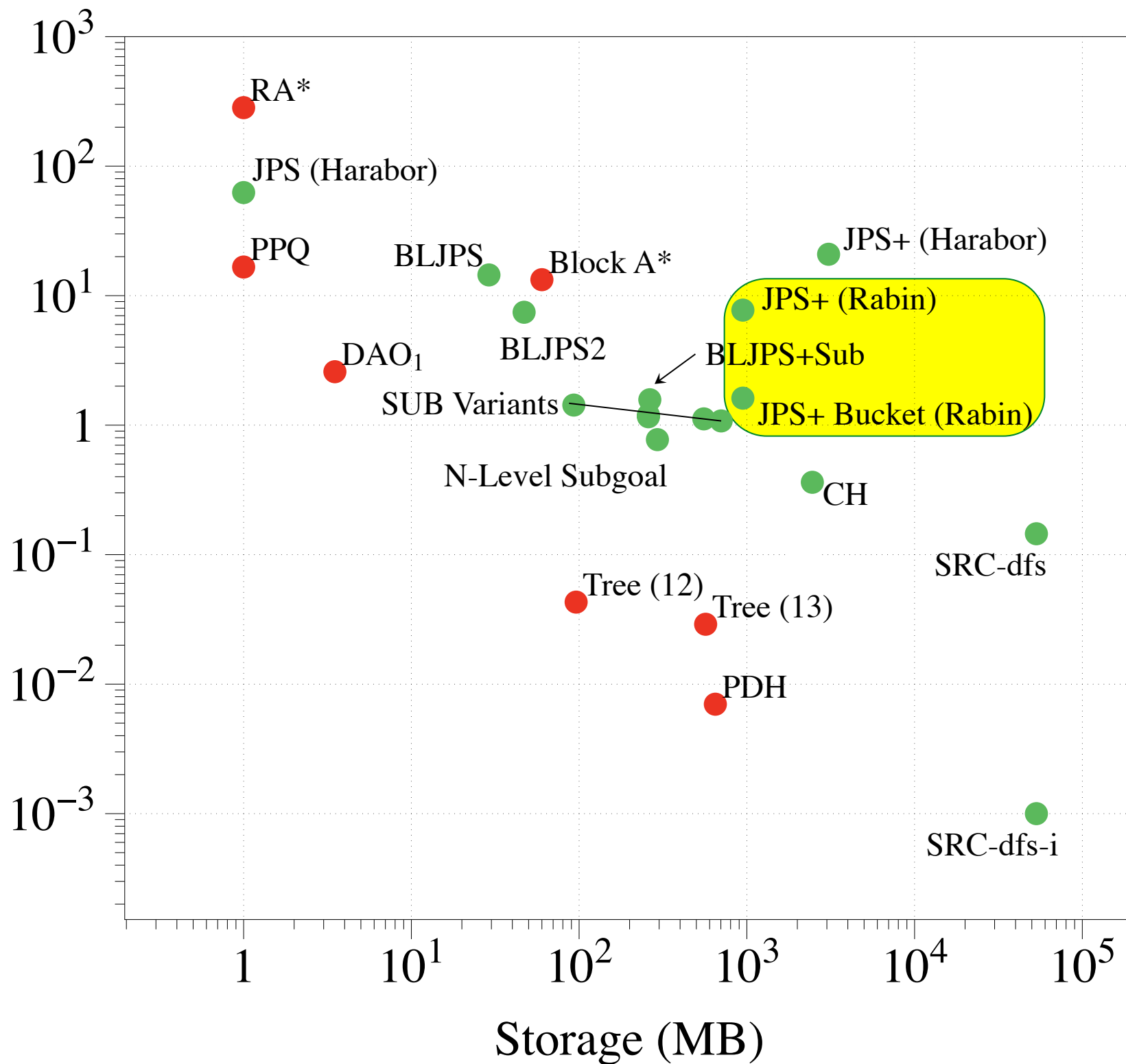
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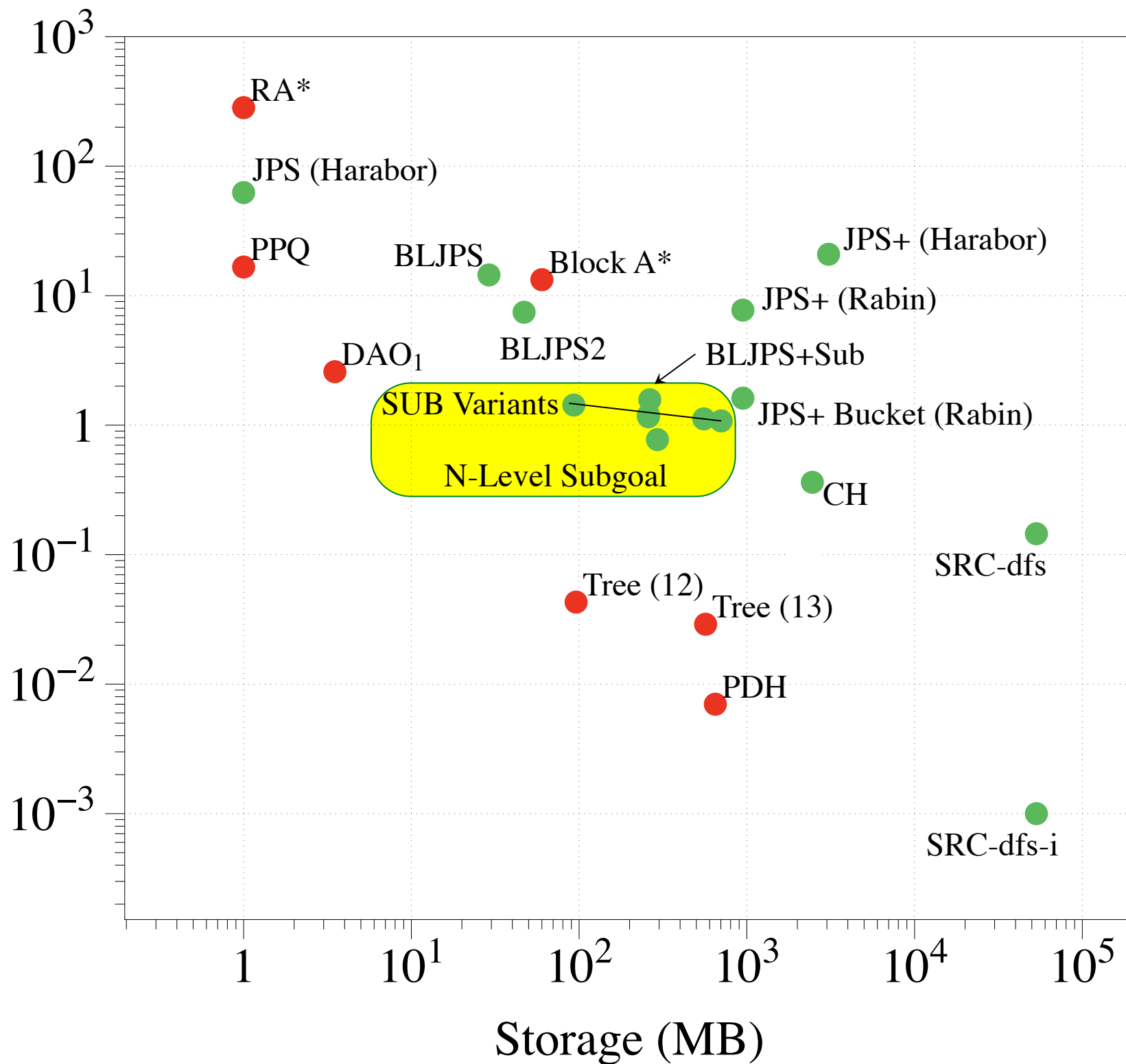


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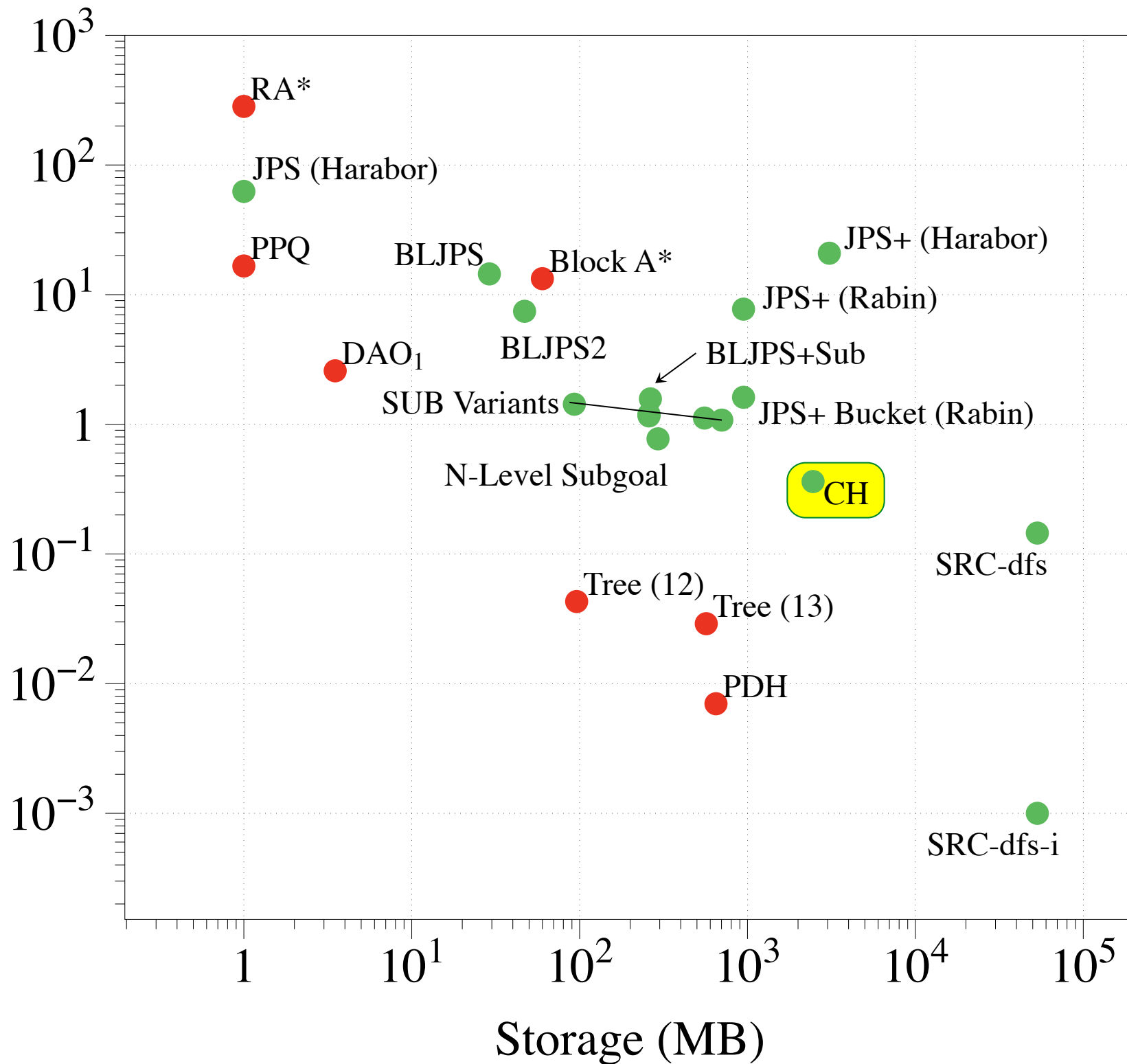




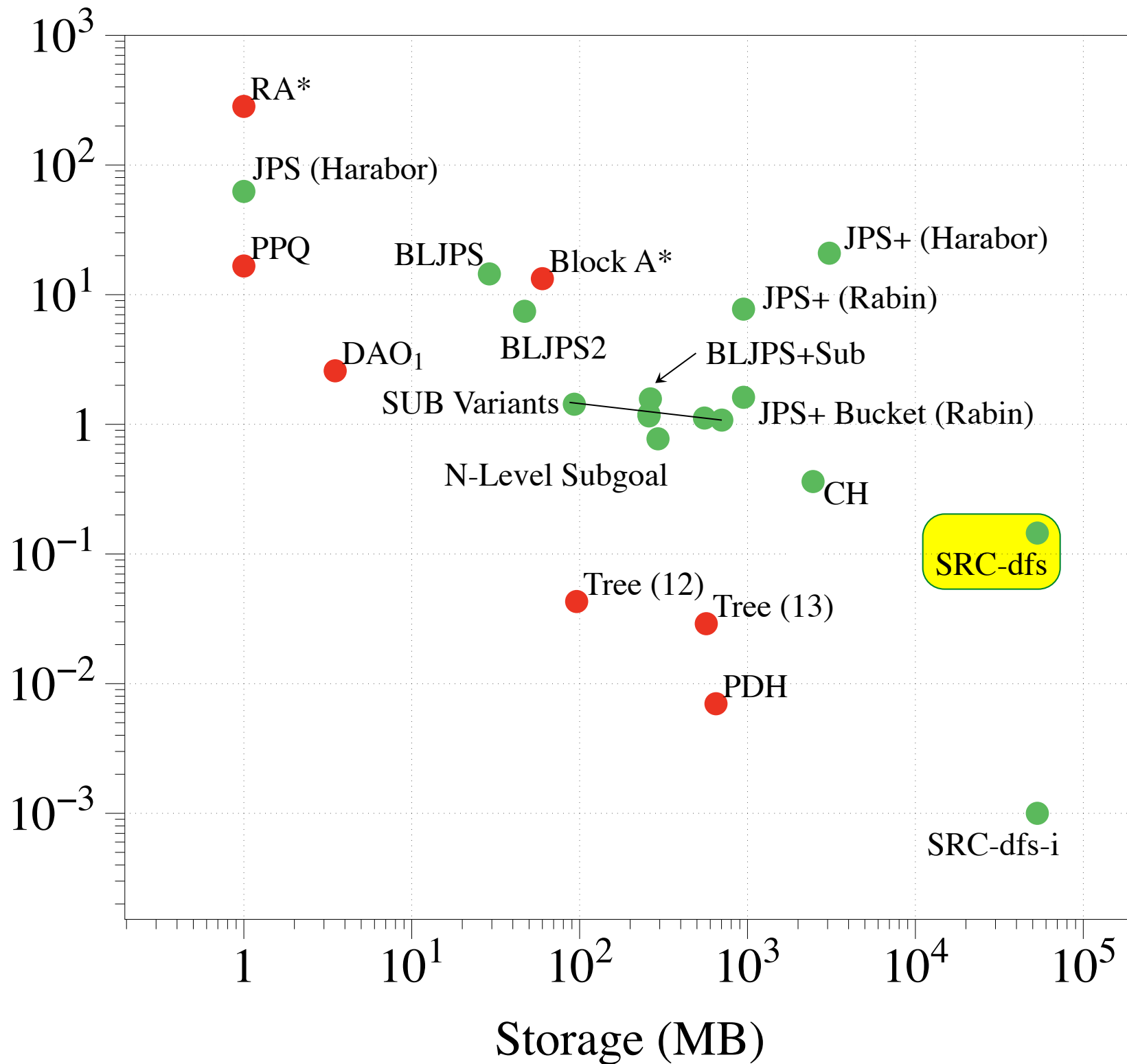
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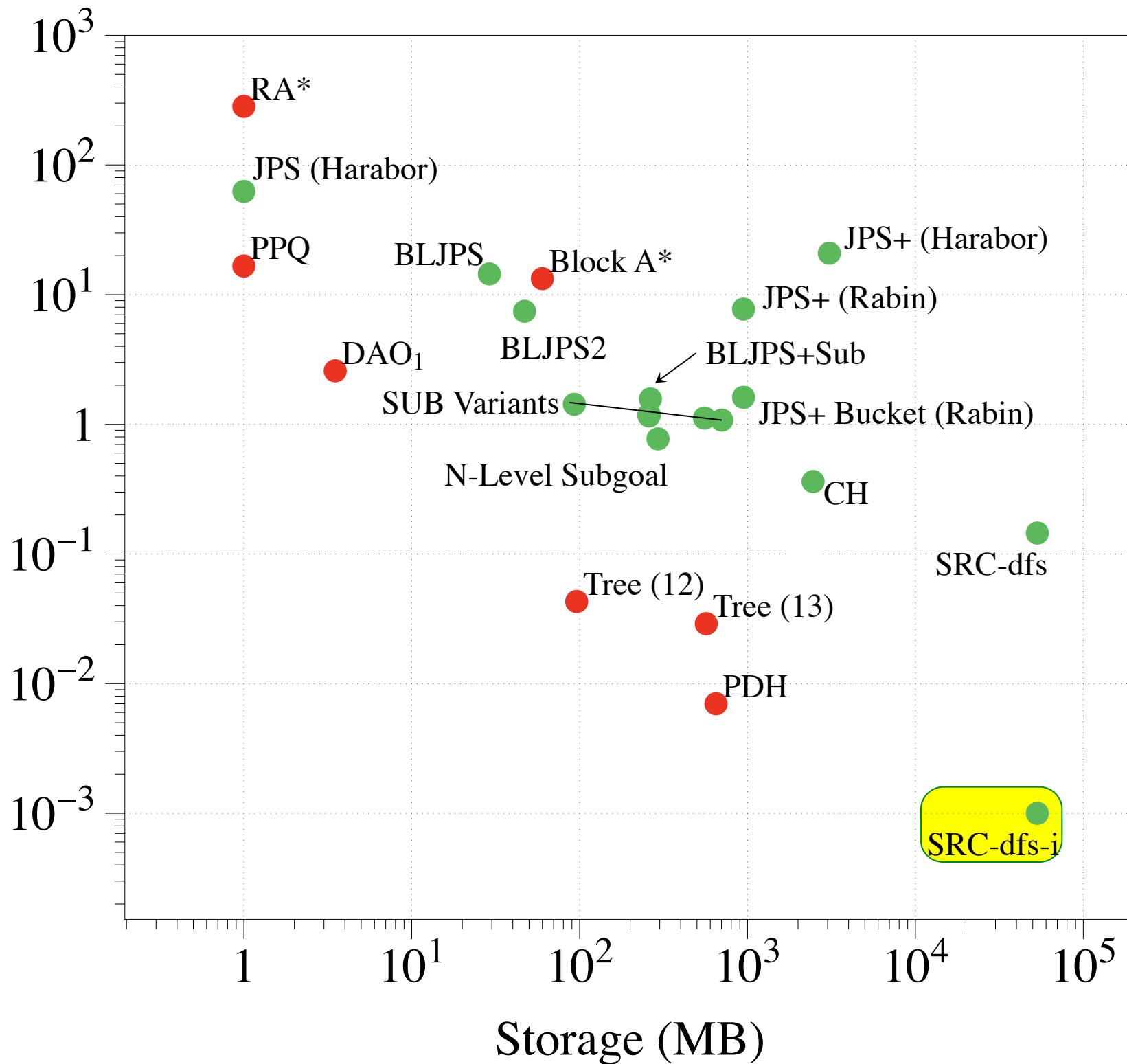
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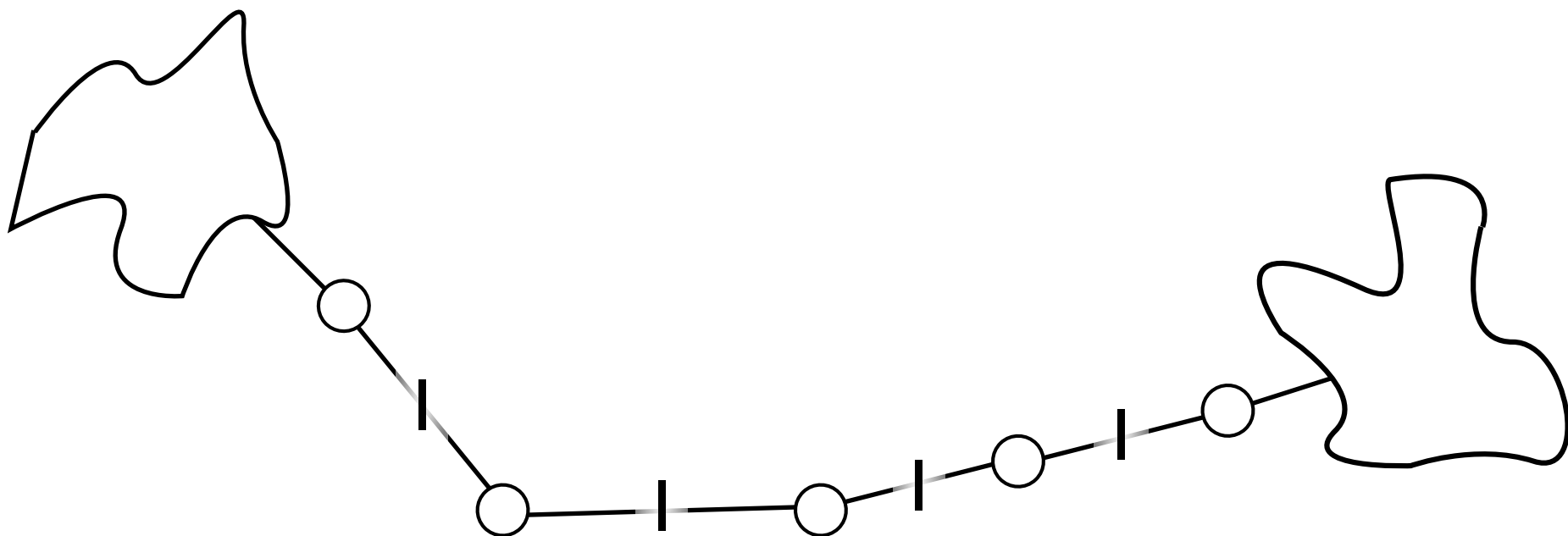
# Contractions everywhere!

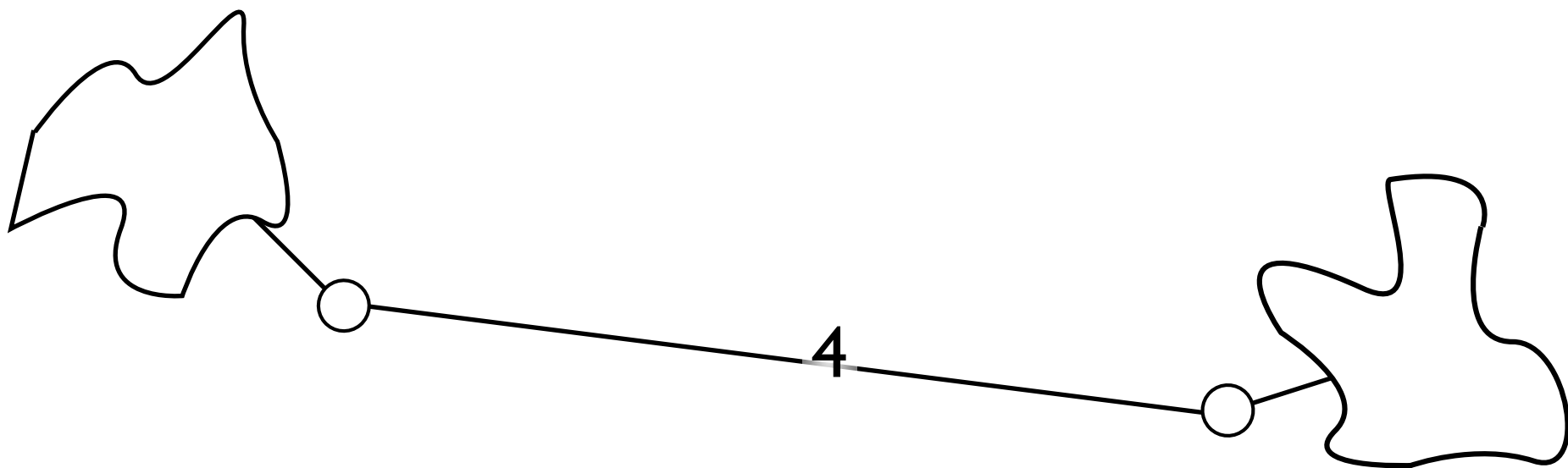
- Describe majority of approaches as contraction:
  - Contraction Hierarchies
  - DAO abstraction
  - Subgoal Graphs
  - Jump Point Search



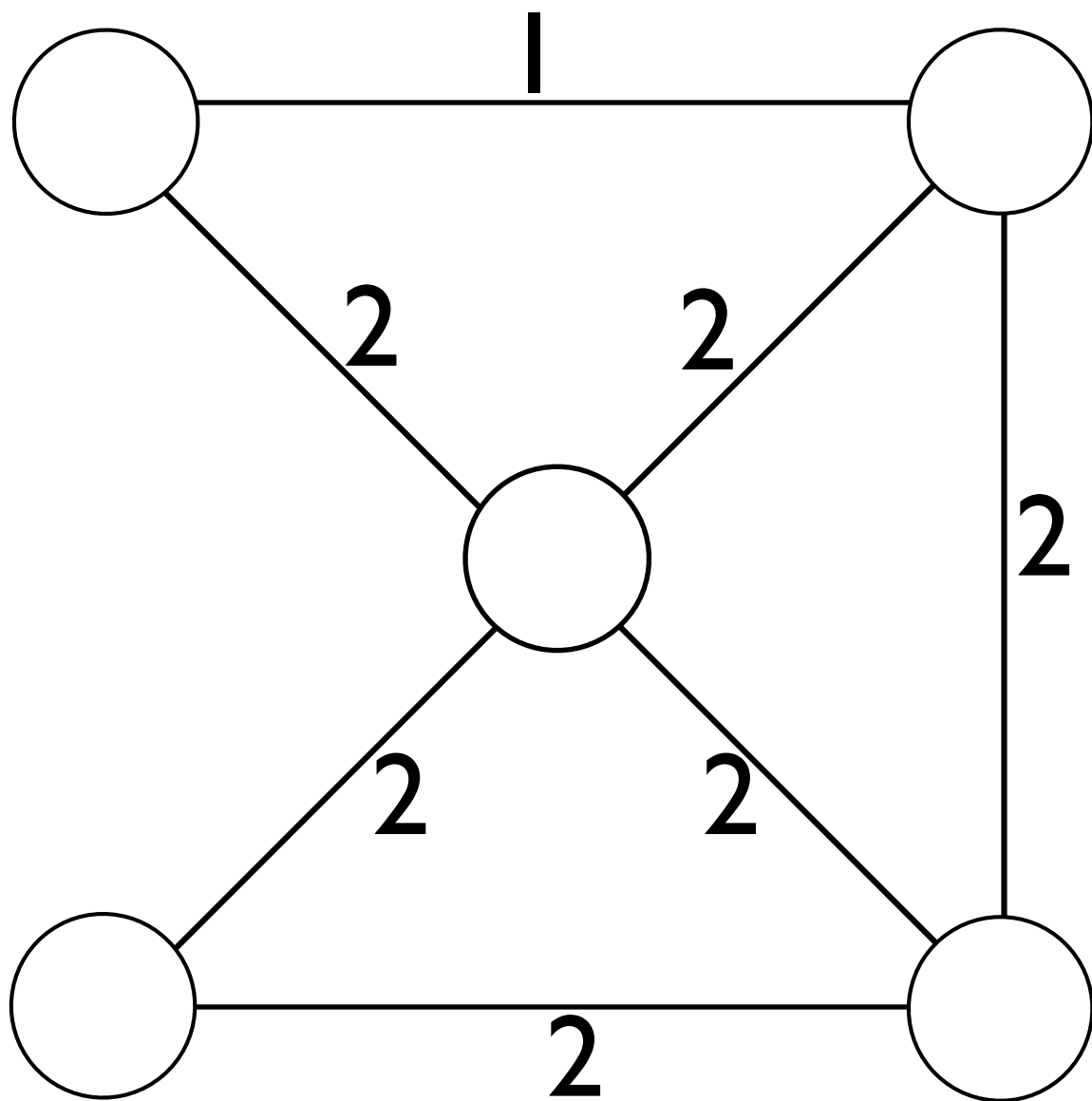
# Graph Contraction

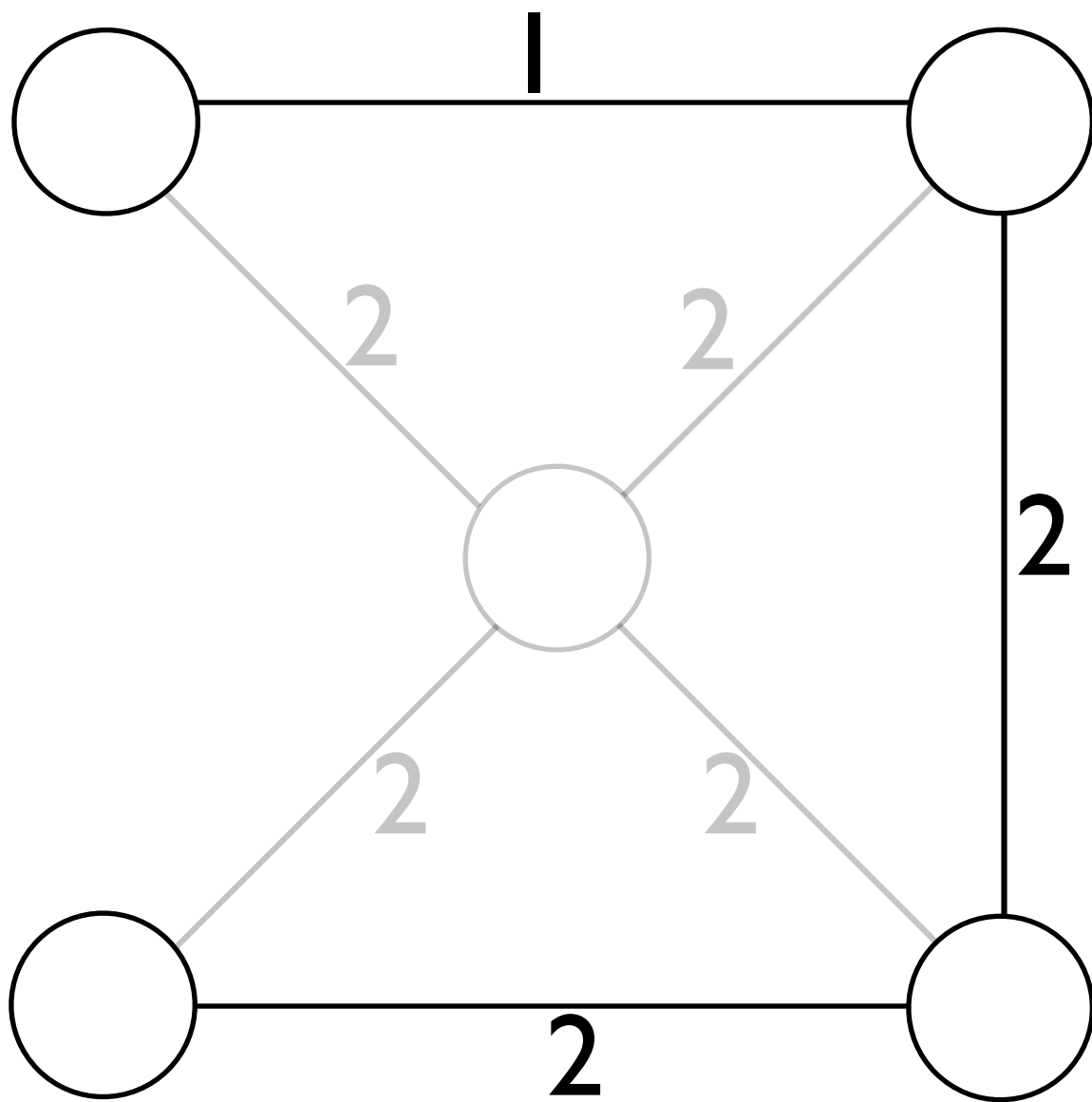
- Remove a set  $S$  of states from a graph  $G$
- Optimal:
  - Ensure that the shortest path between all states  $G \setminus S$  are not changed
  - Add edges (shortcuts) to preserve shortest paths
- Suboptimal:
  - Ensure that completeness is not lost

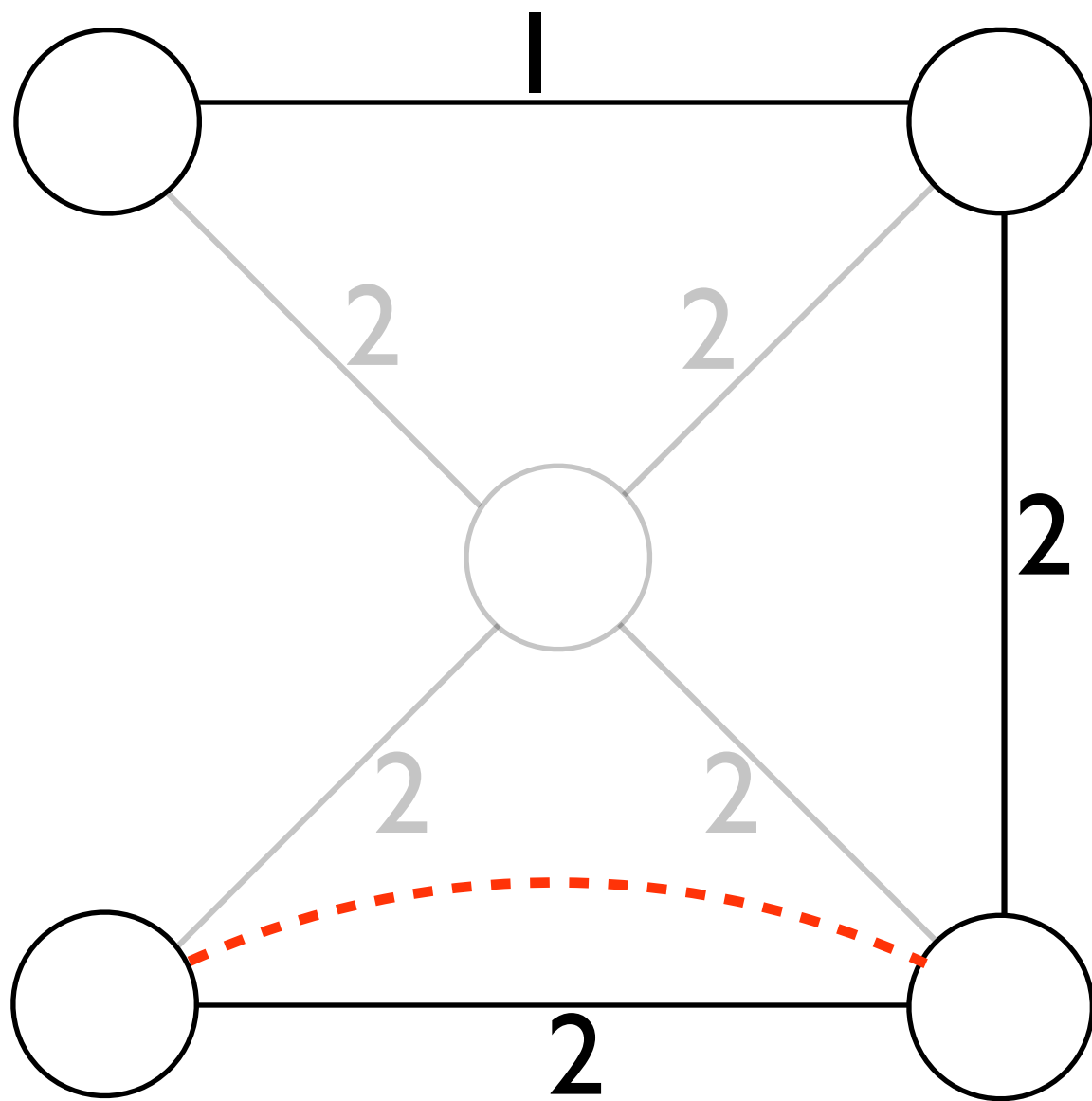


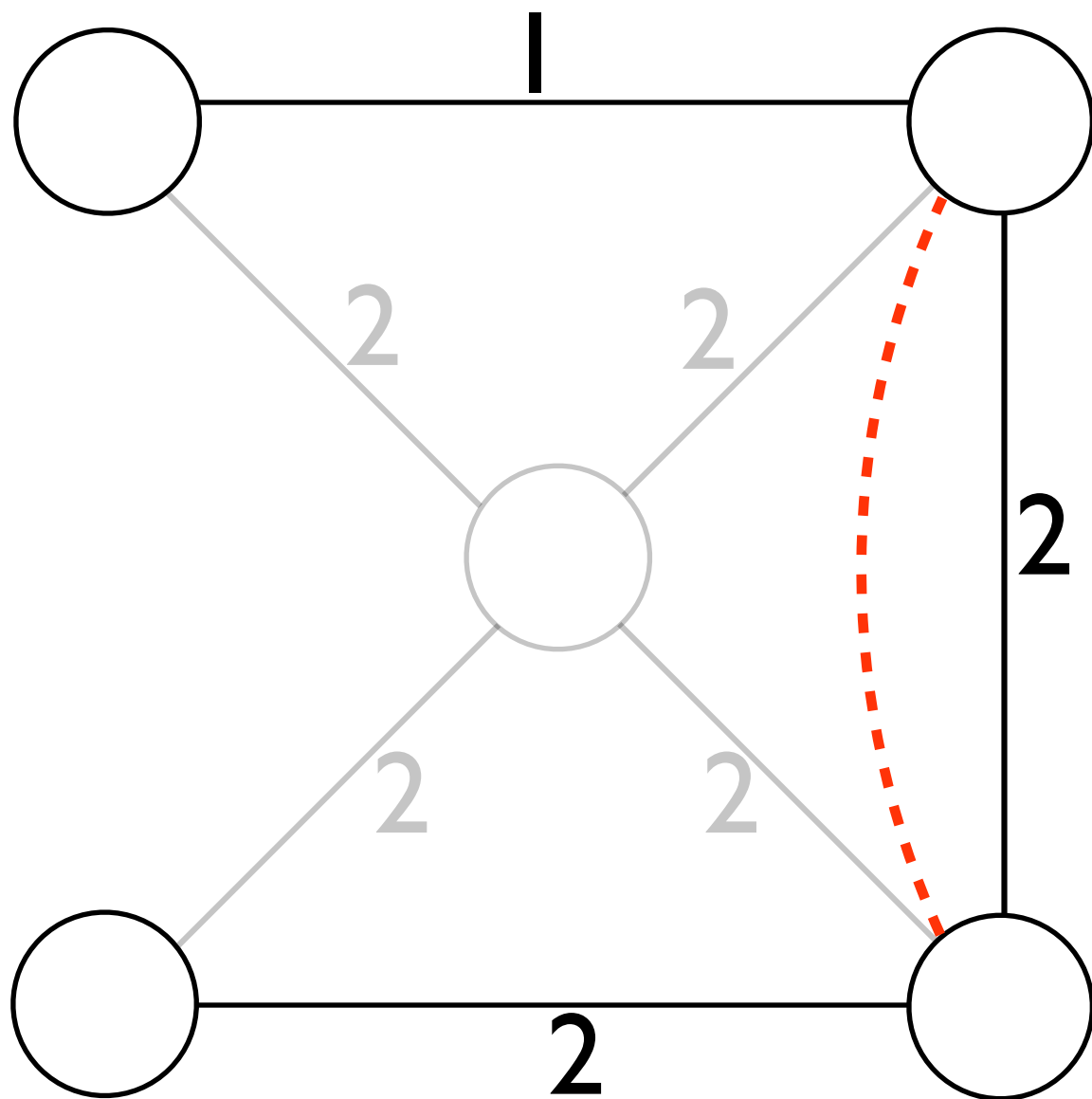


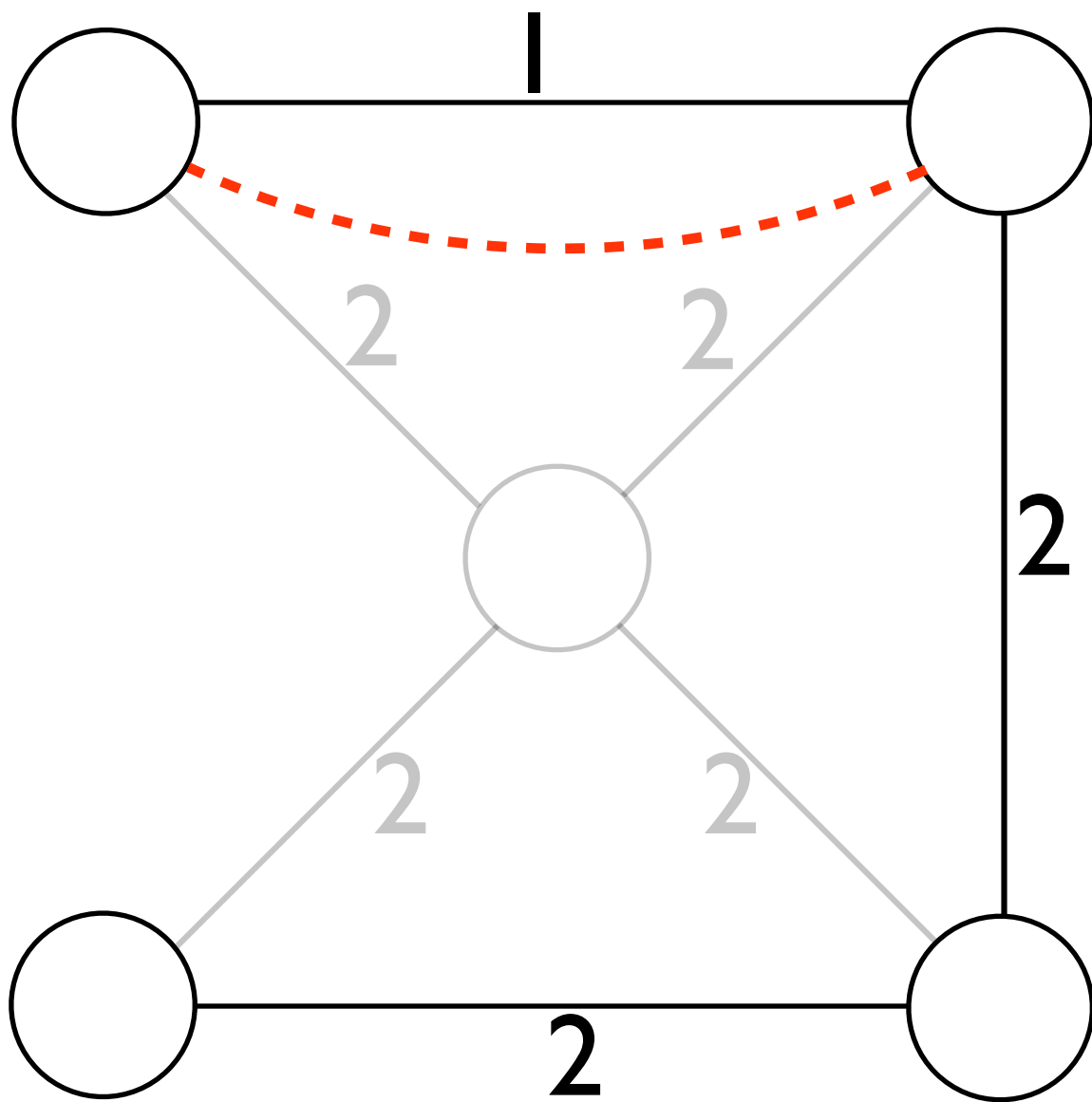


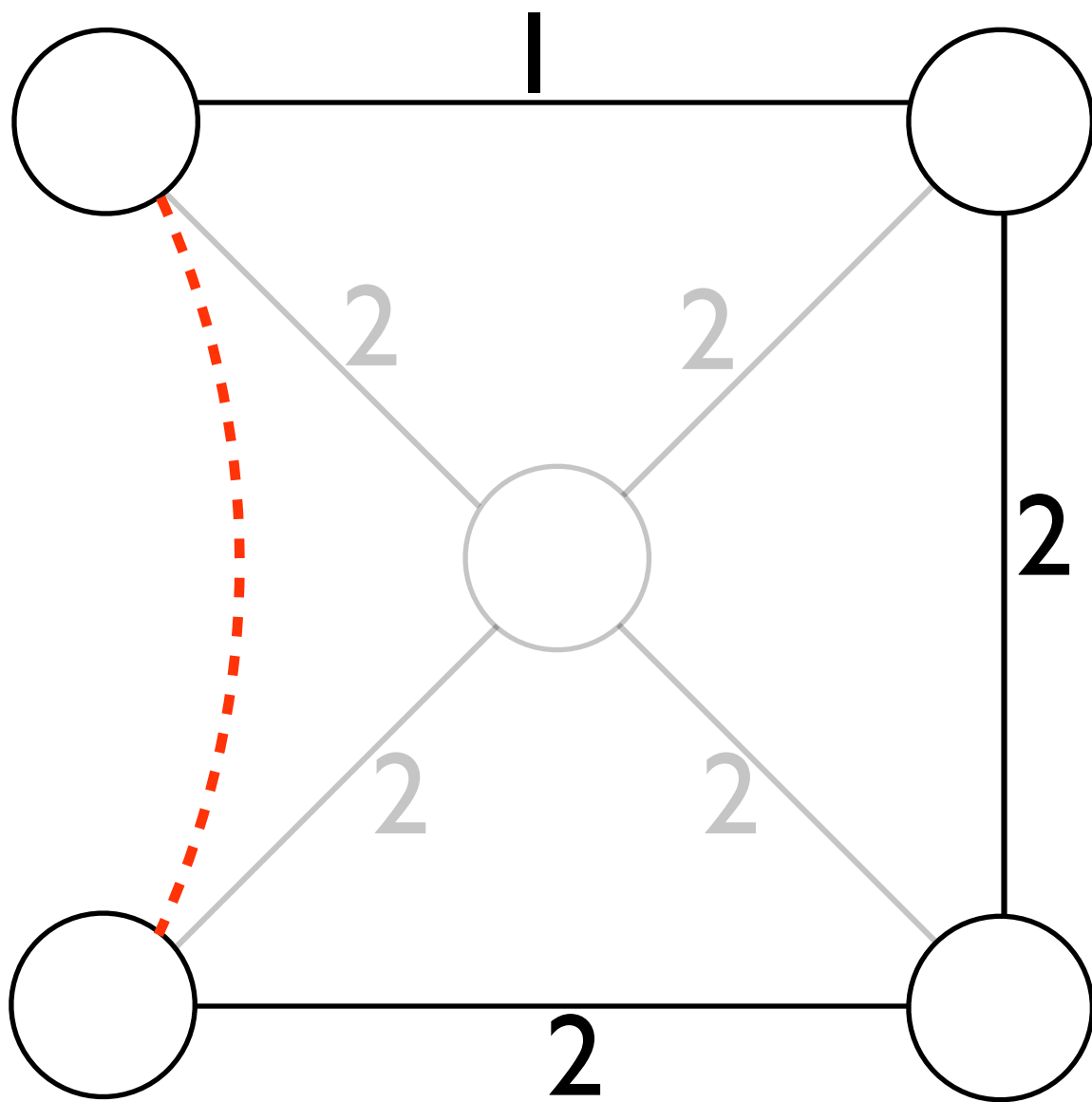


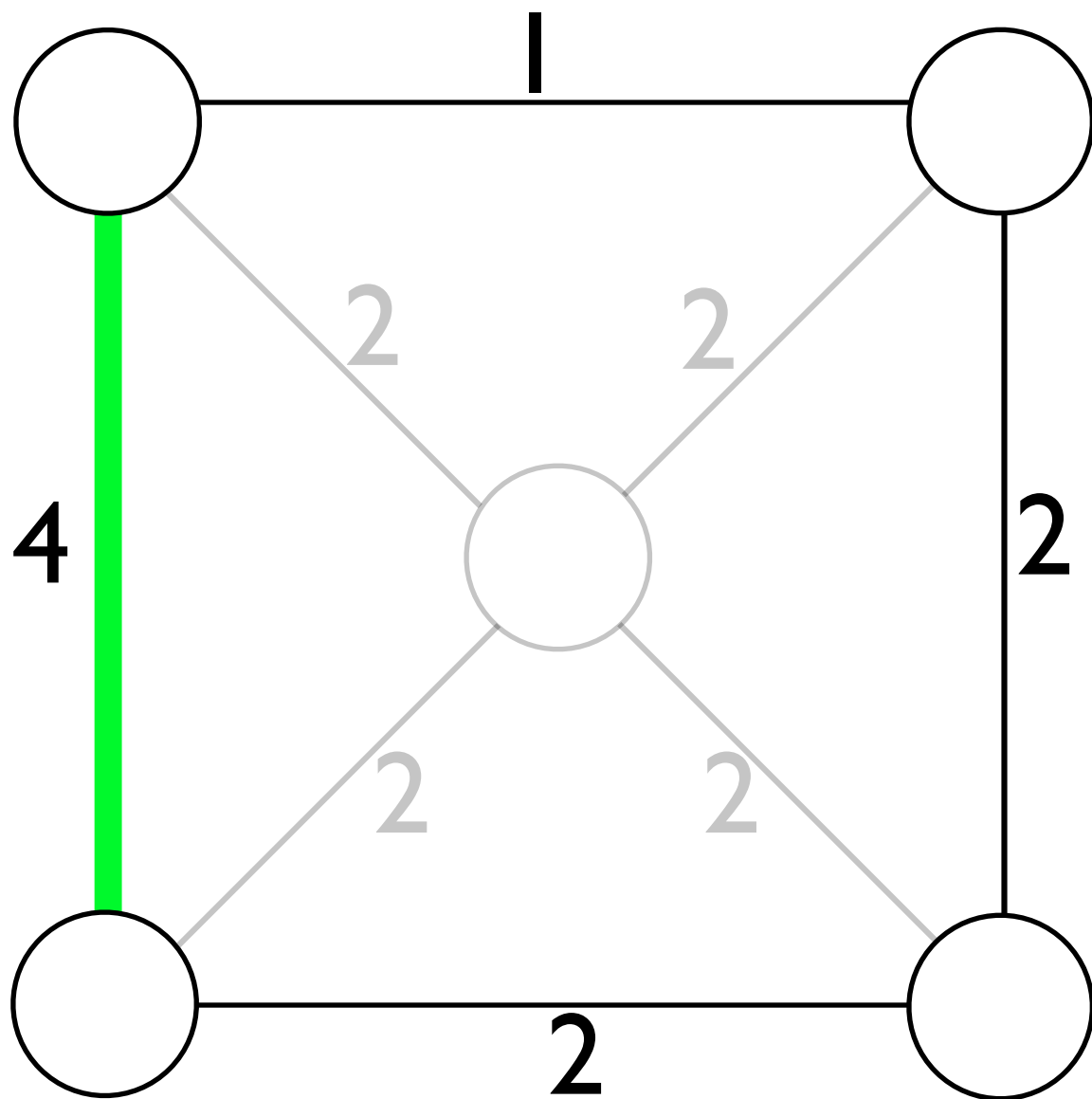


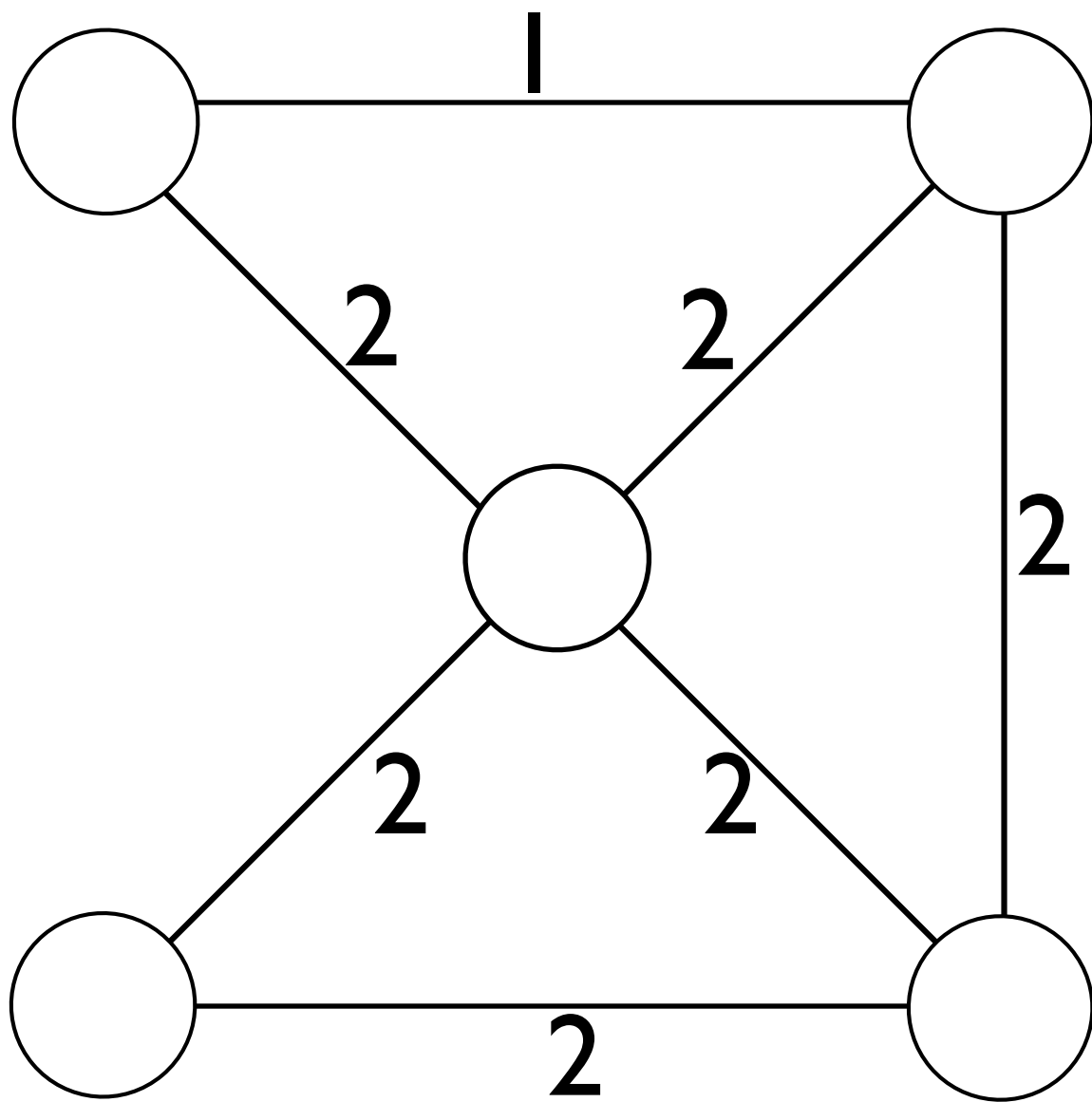




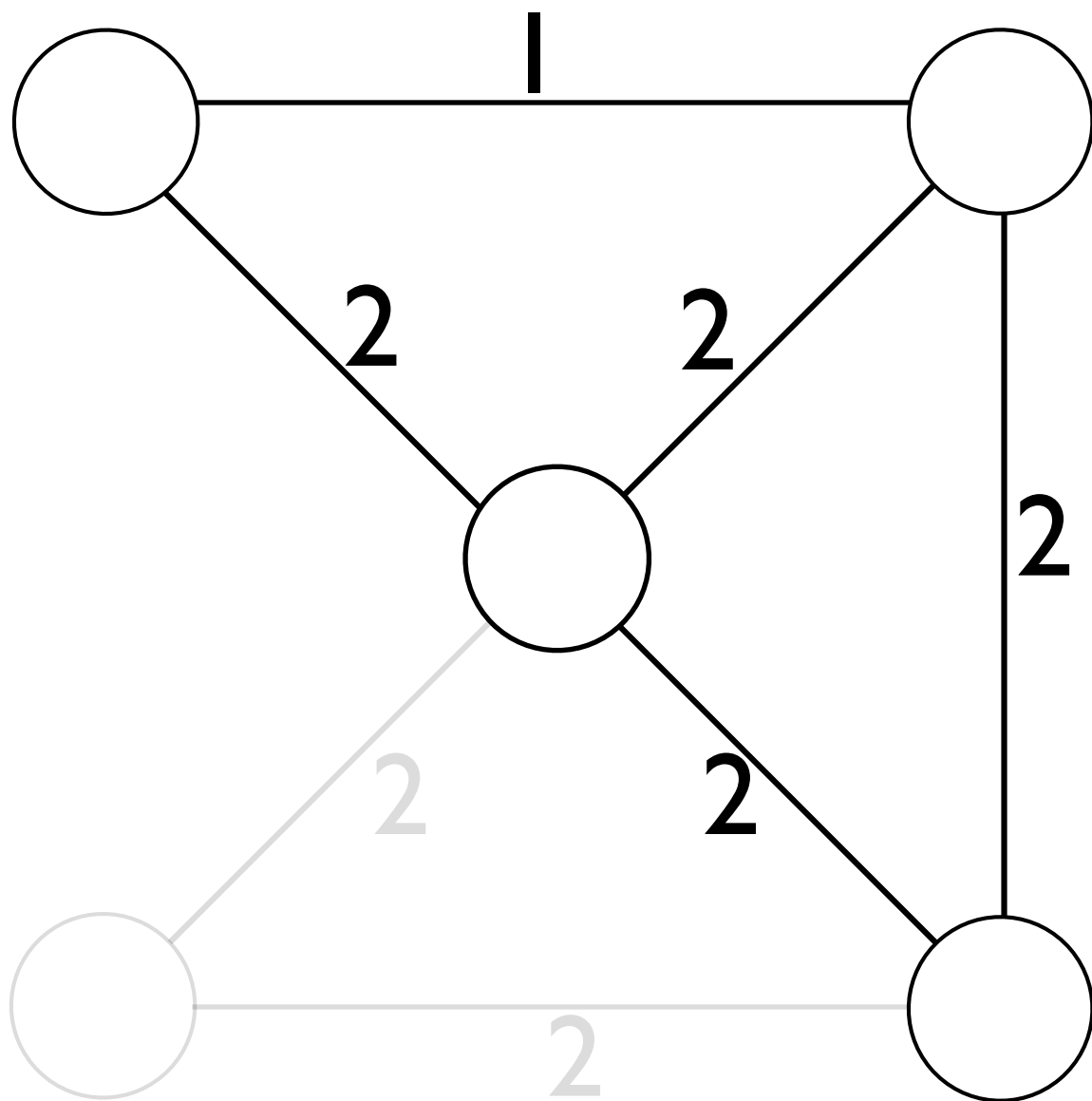














# Contraction Hierarchies

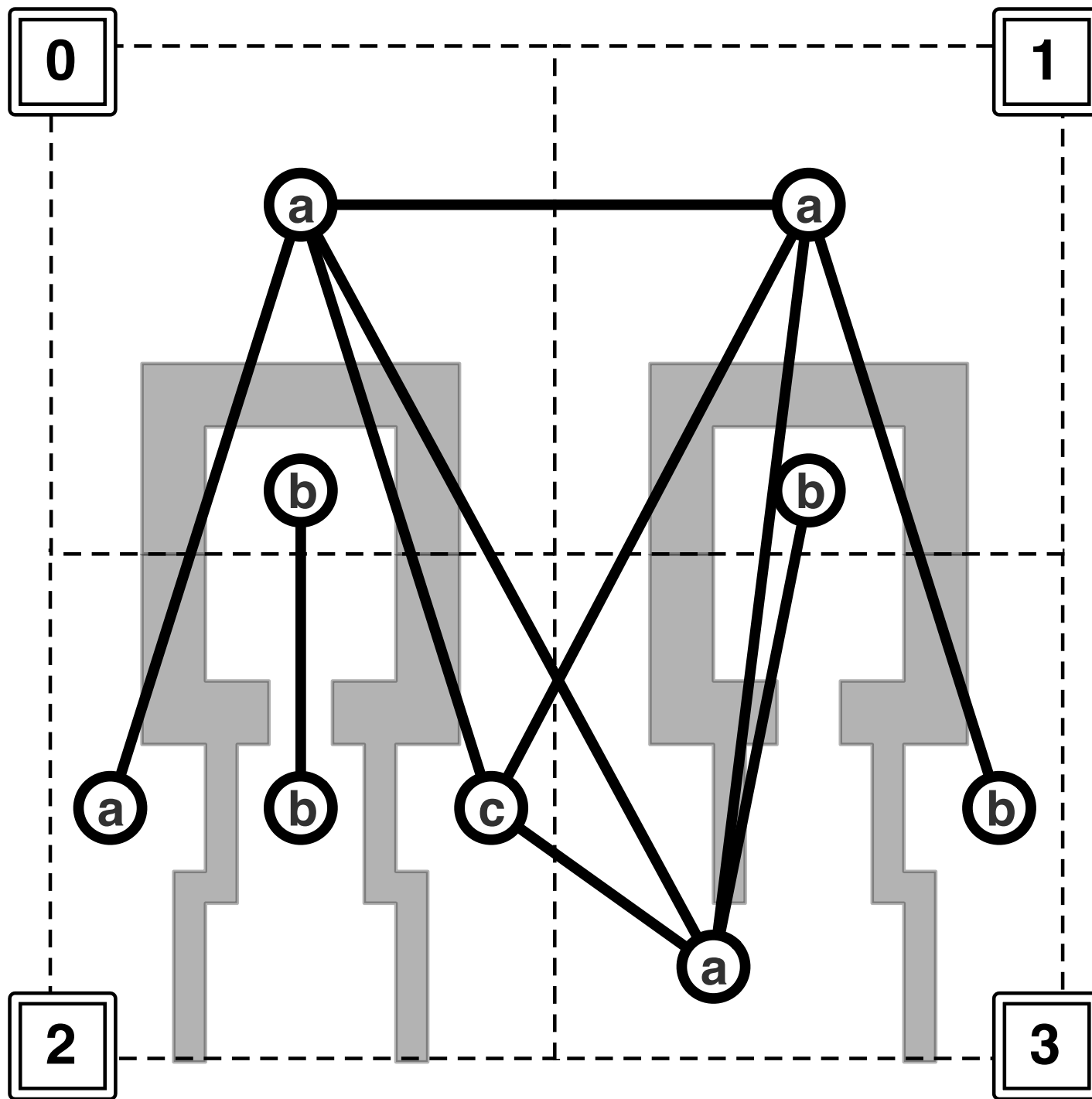
- Optimal approach
- Key idea is finding good orderings for contracting nodes from the graph
- Contract one node at a time
  - Add shortcut edges



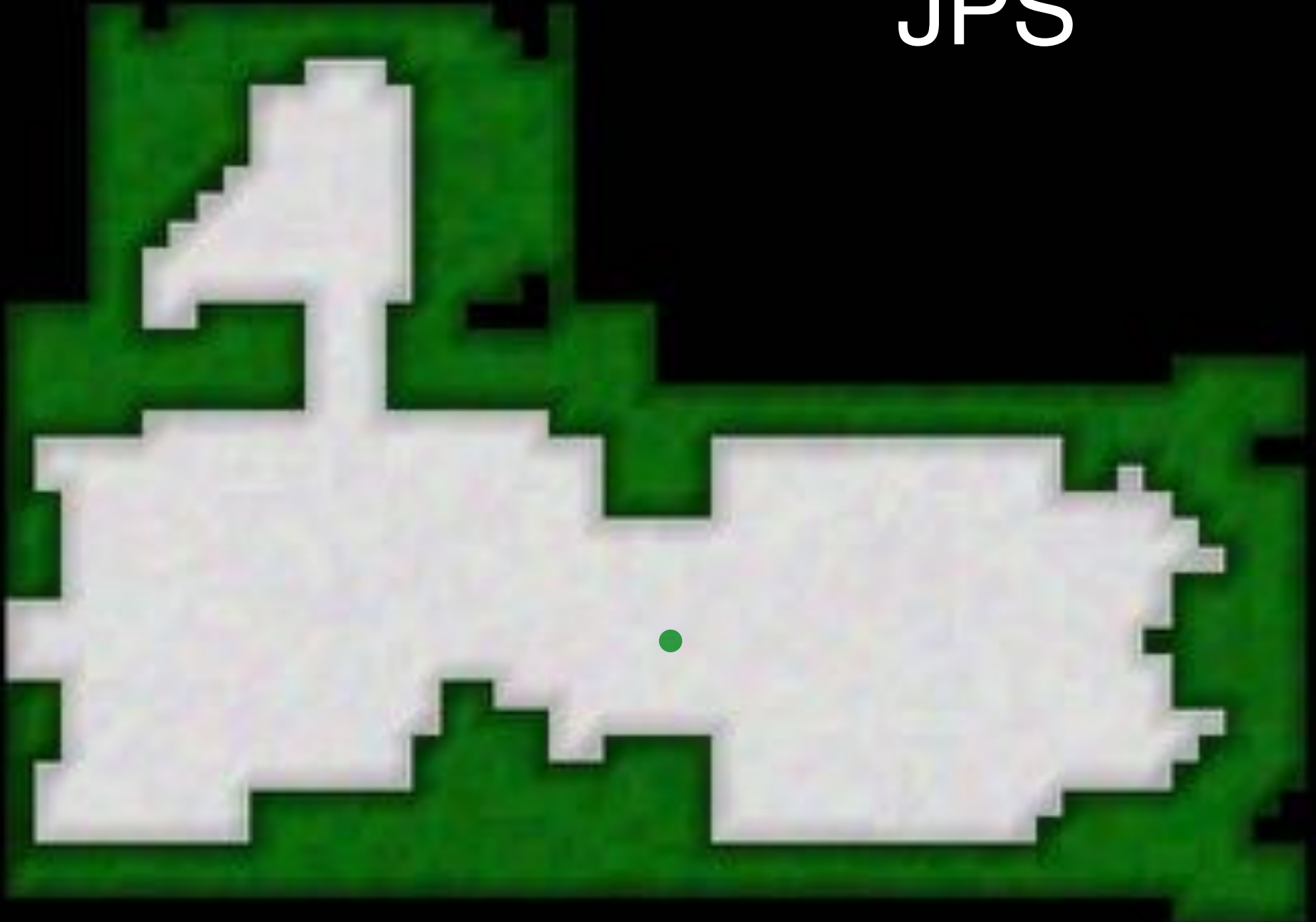
# Traditional Abstraction/ Refinement

- Find strongly connected components
  - Abstract them together into a single abstract state
  - (Holte et al, 1996), (Fernández, & González, 2002), (Botea et. al., 2004), (Sturtevant & Buro, 2005), (Sturtevant 2007)
  - *Downward refinement property*
- Approach discarded in road networks after optimal approaches discovered

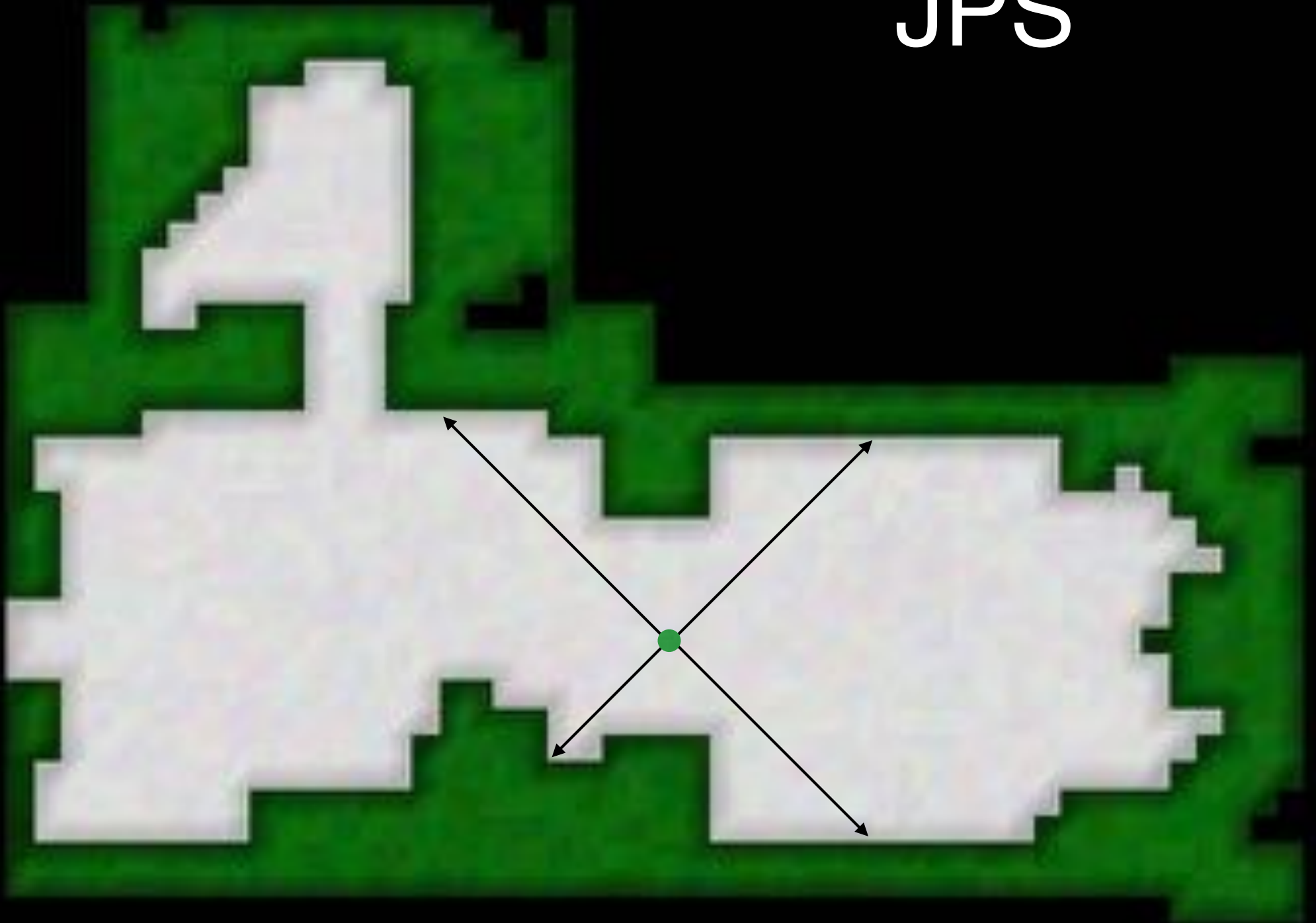




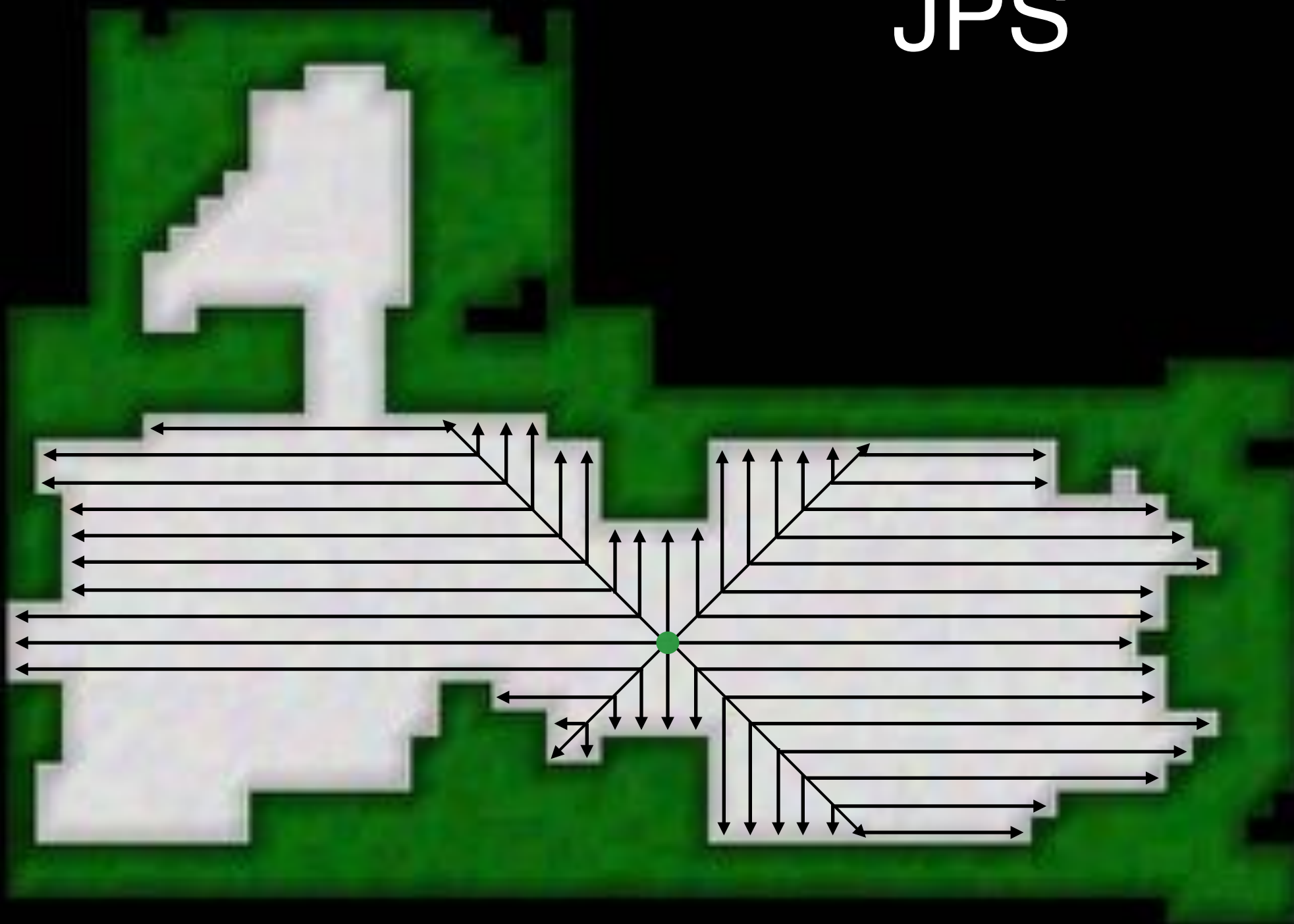
JPS



JPS

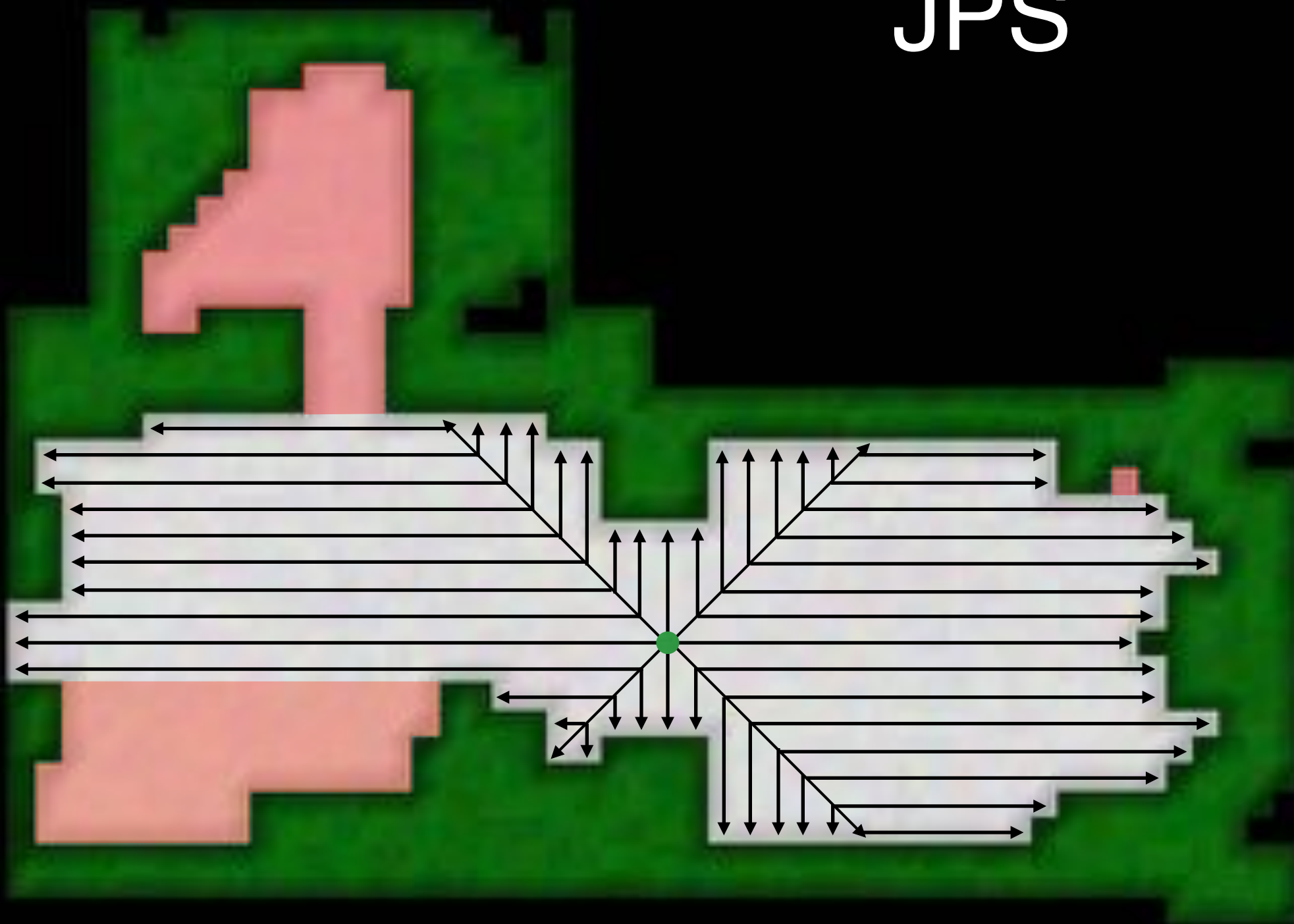


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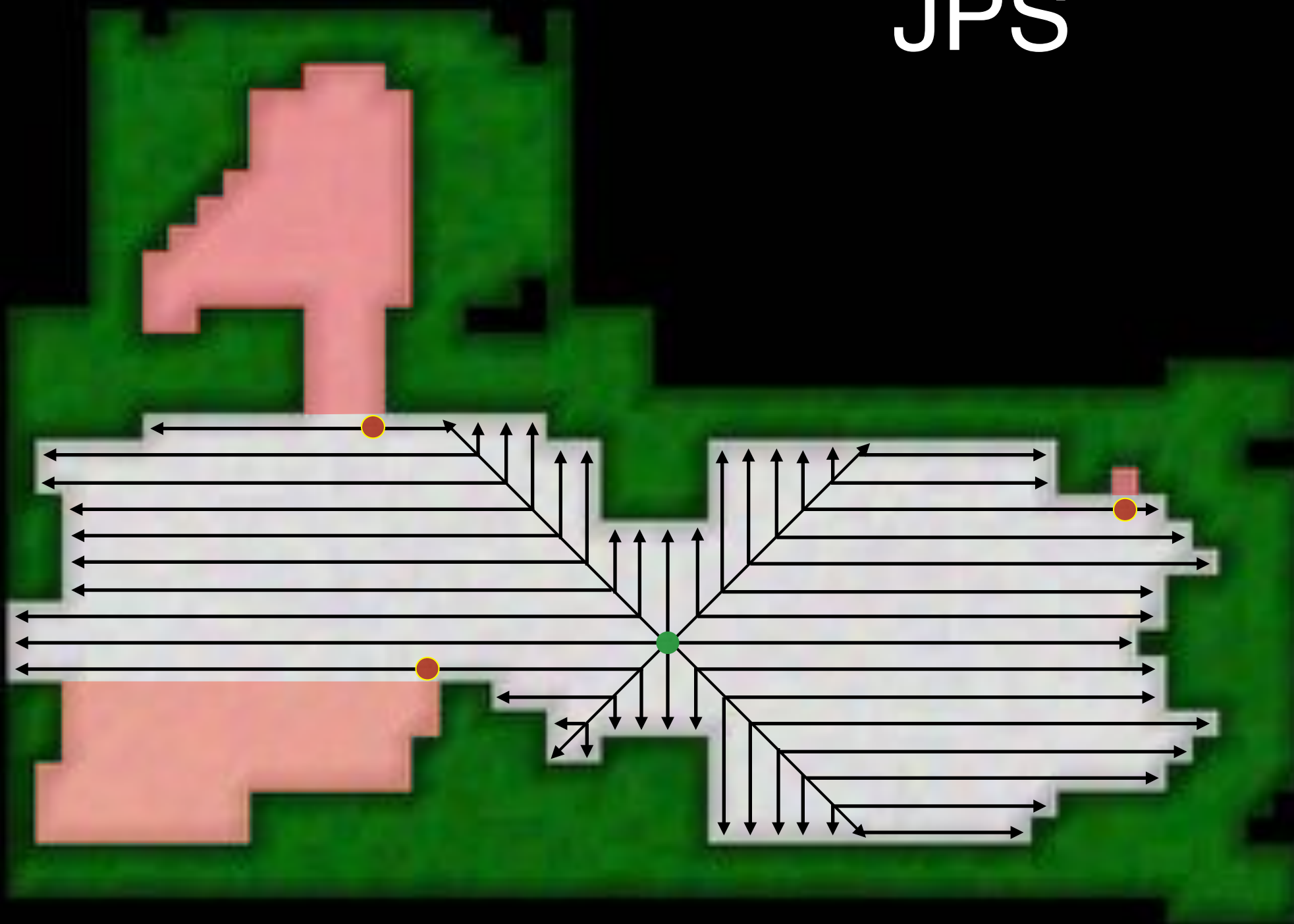




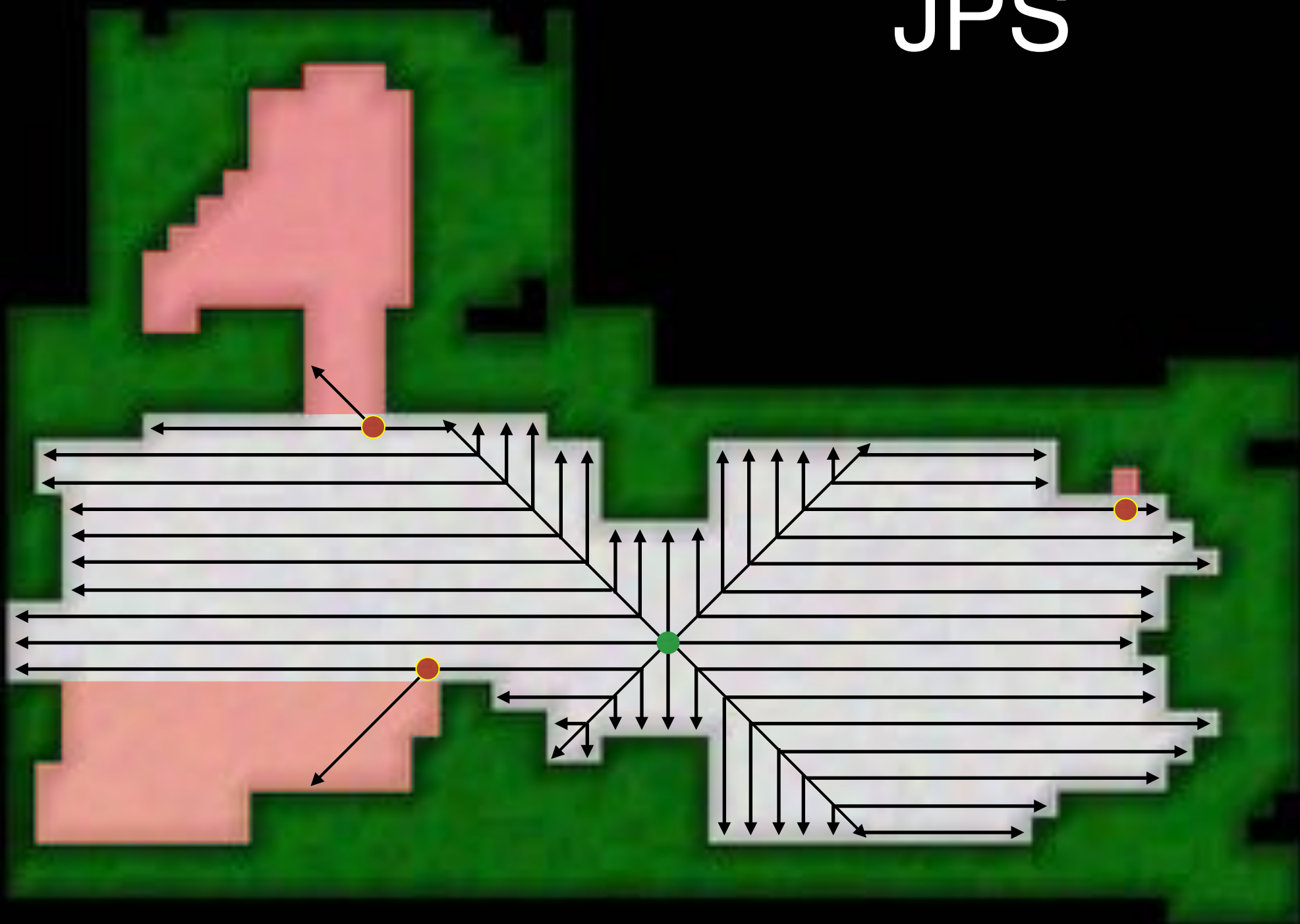
# JPS



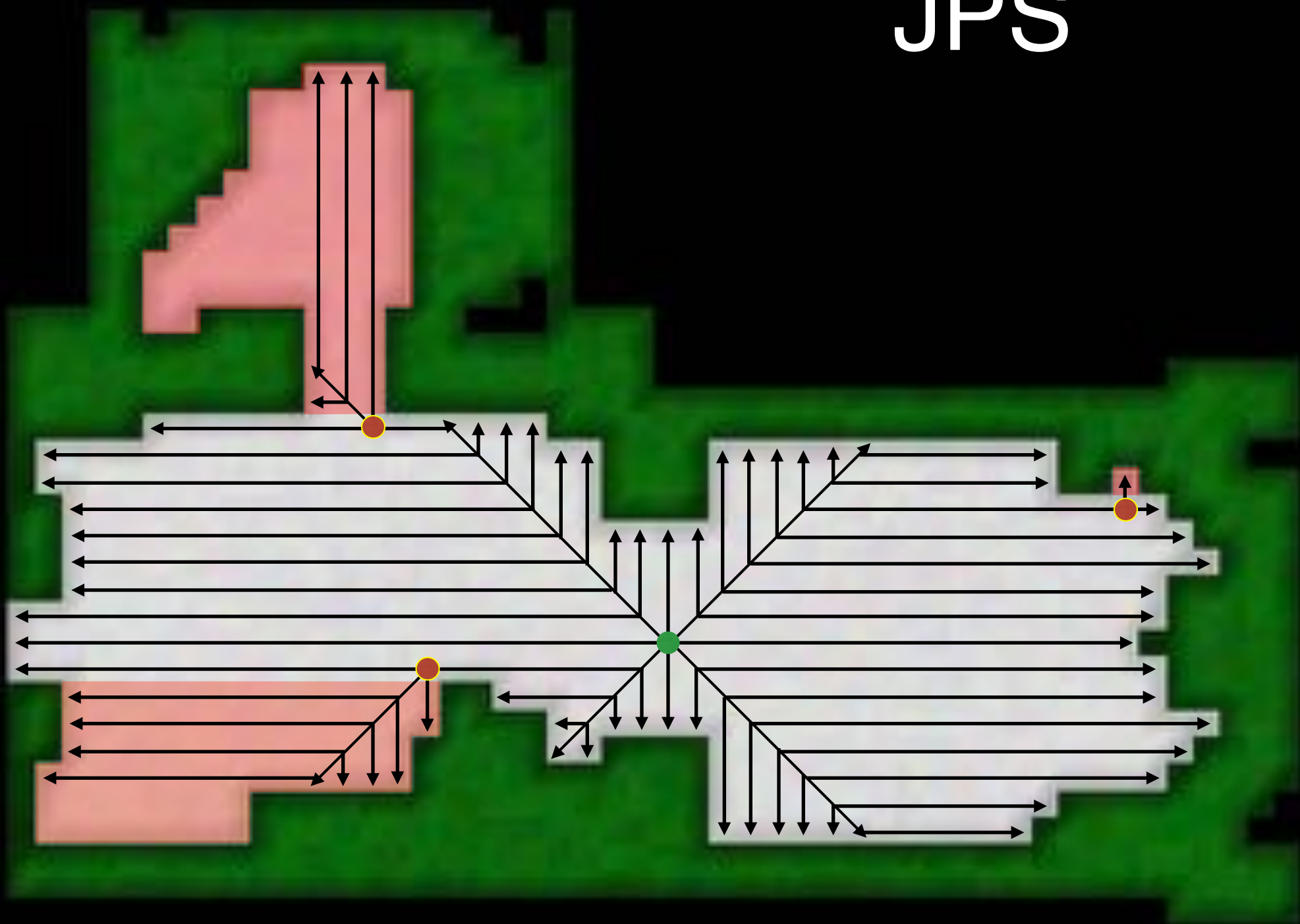
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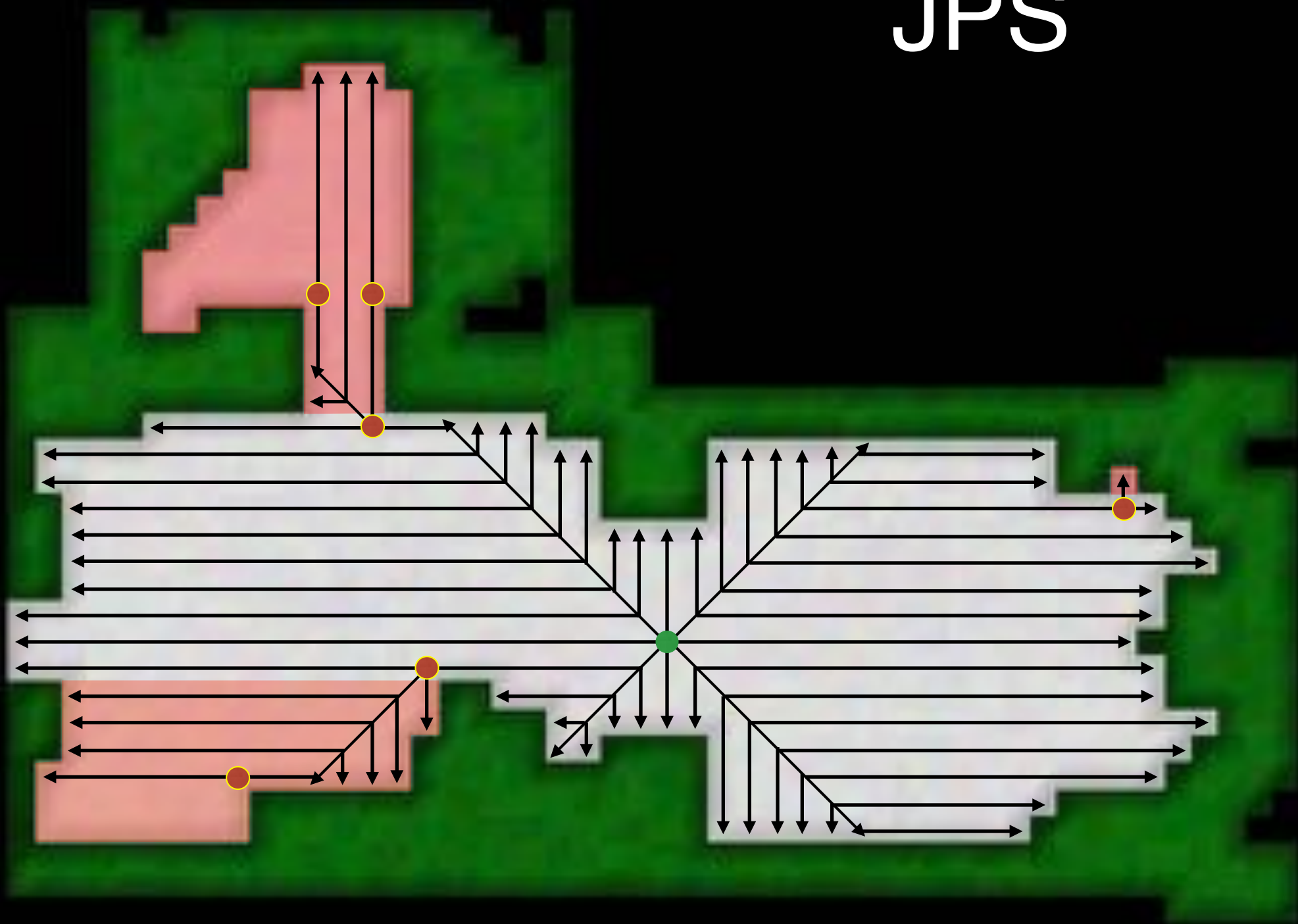
# JPS



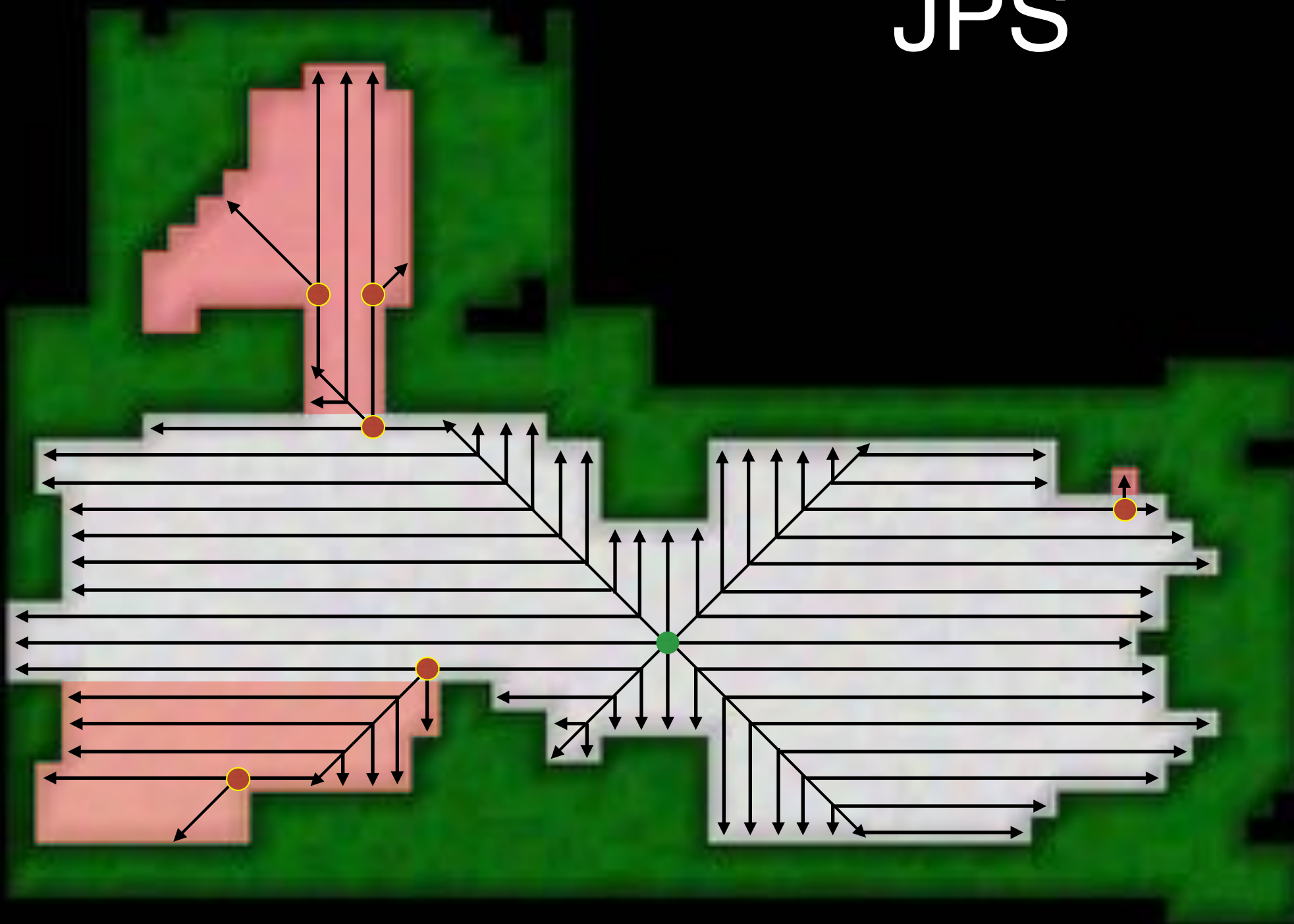
# JPS



# JPS

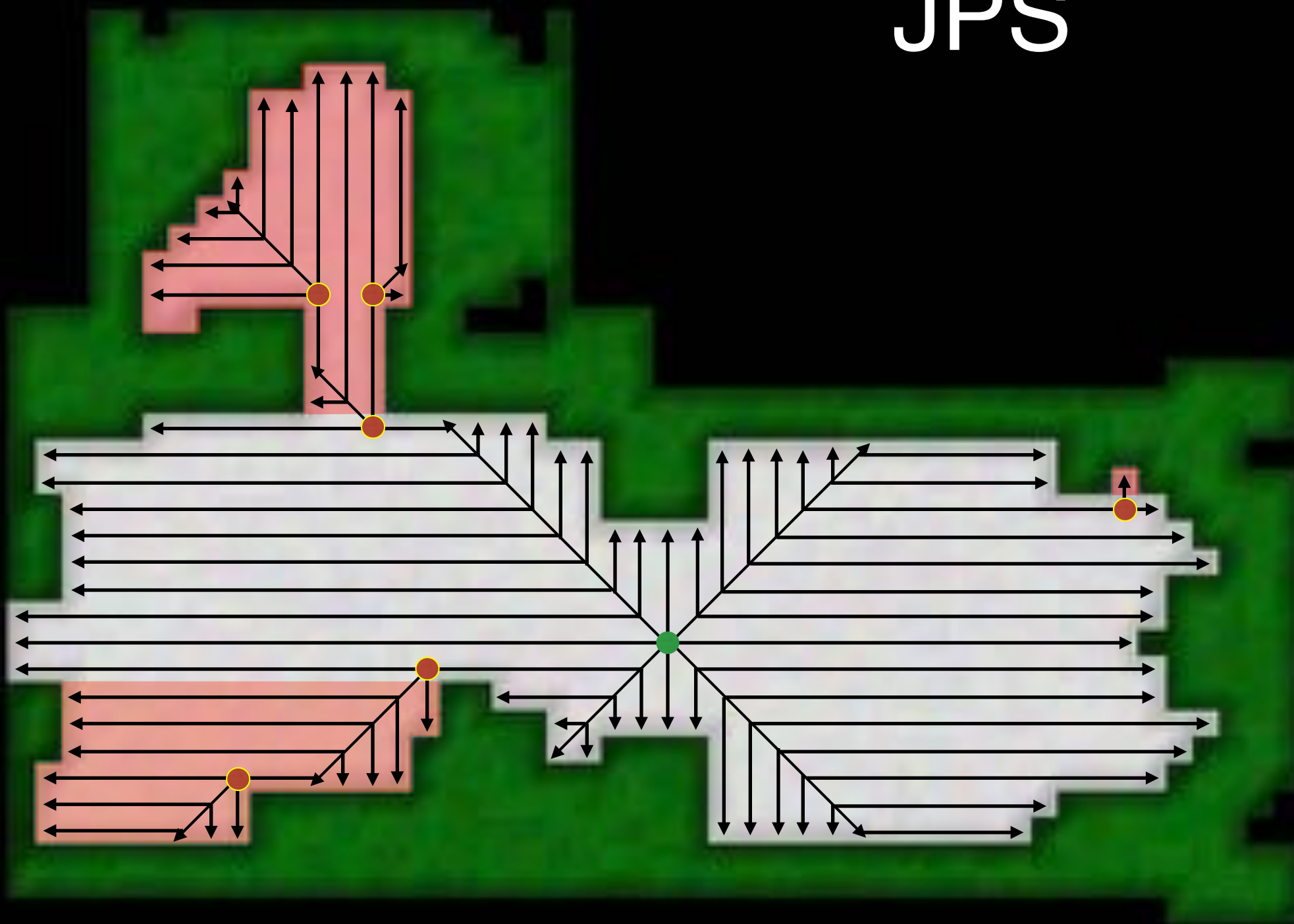


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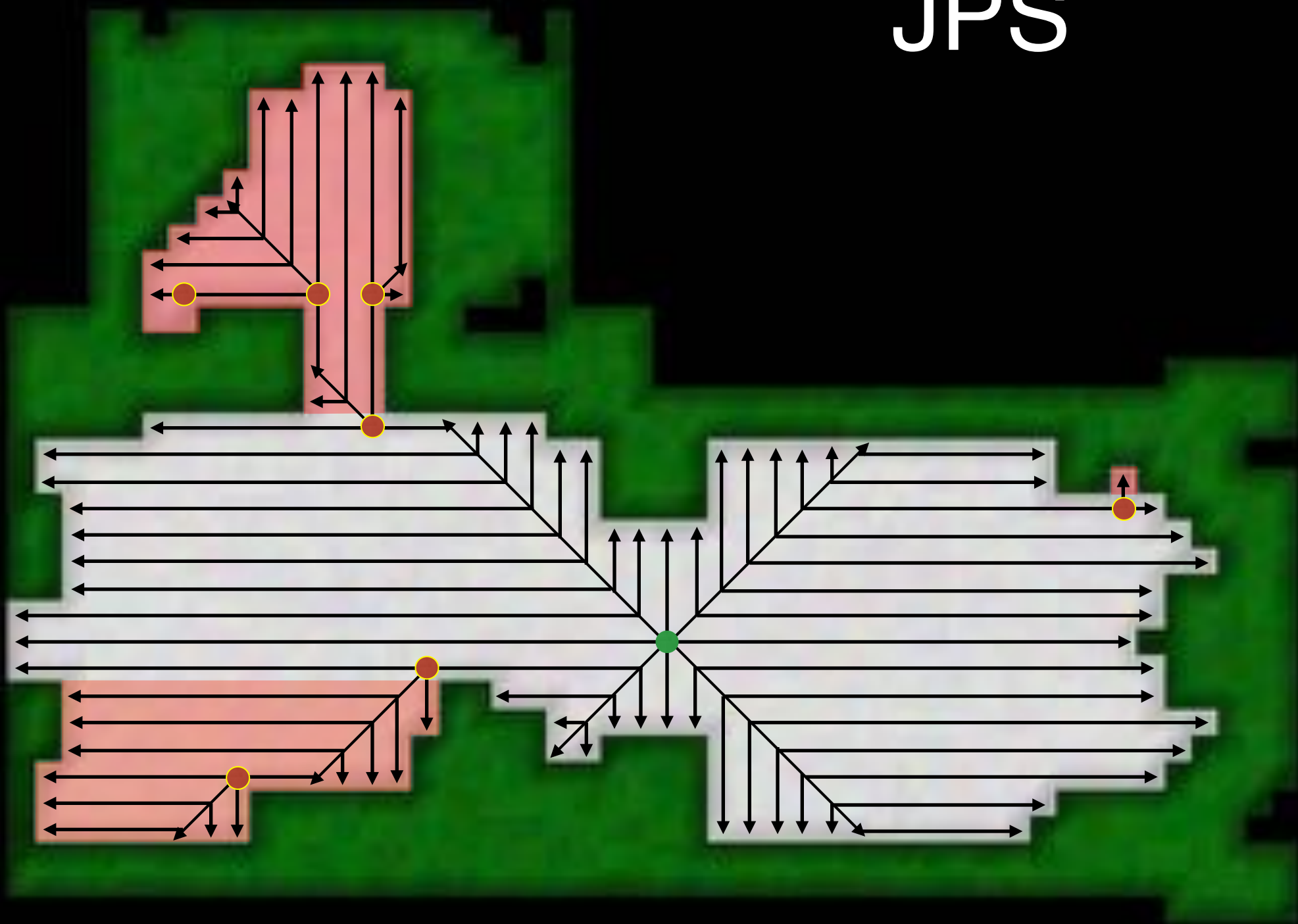




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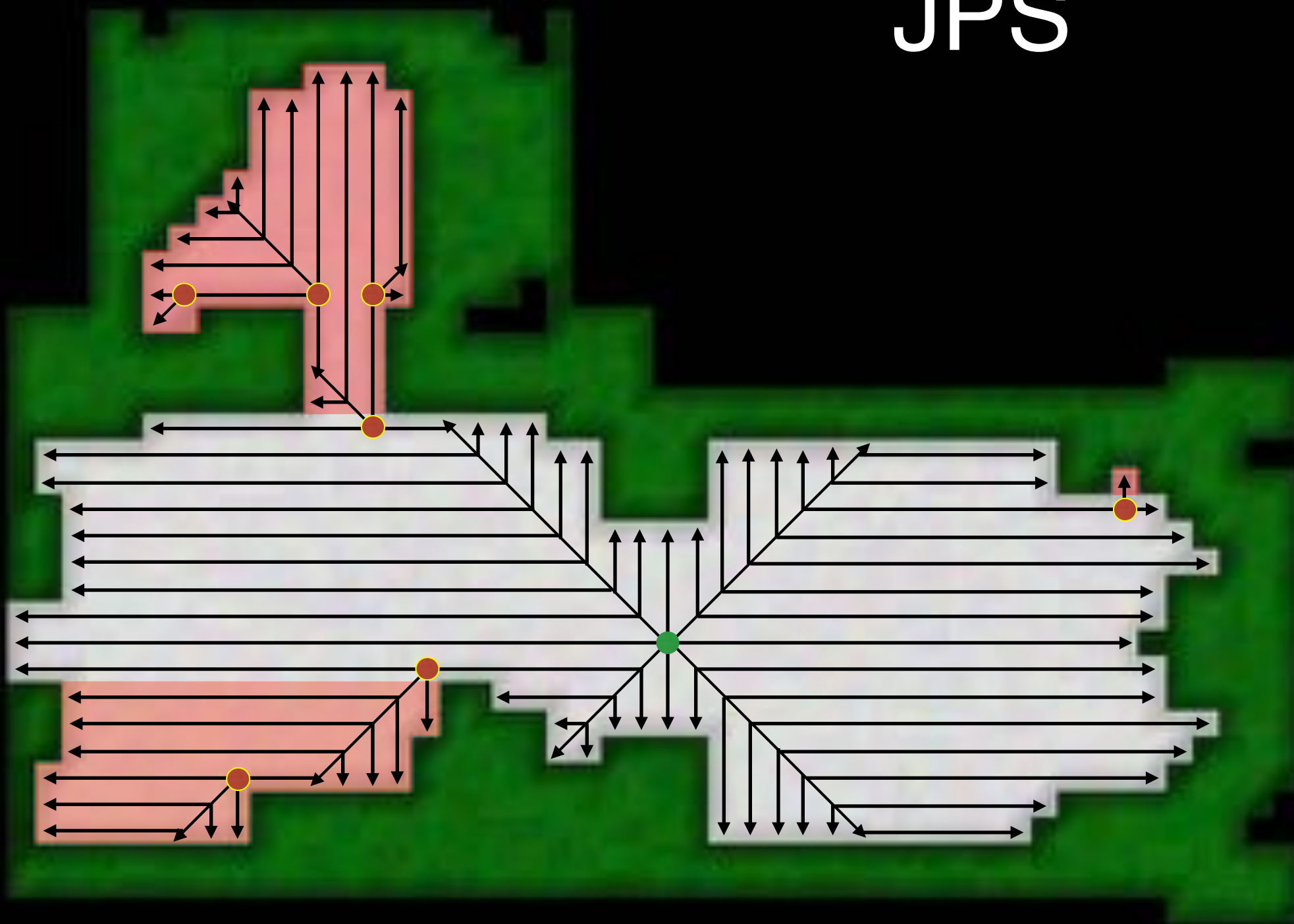


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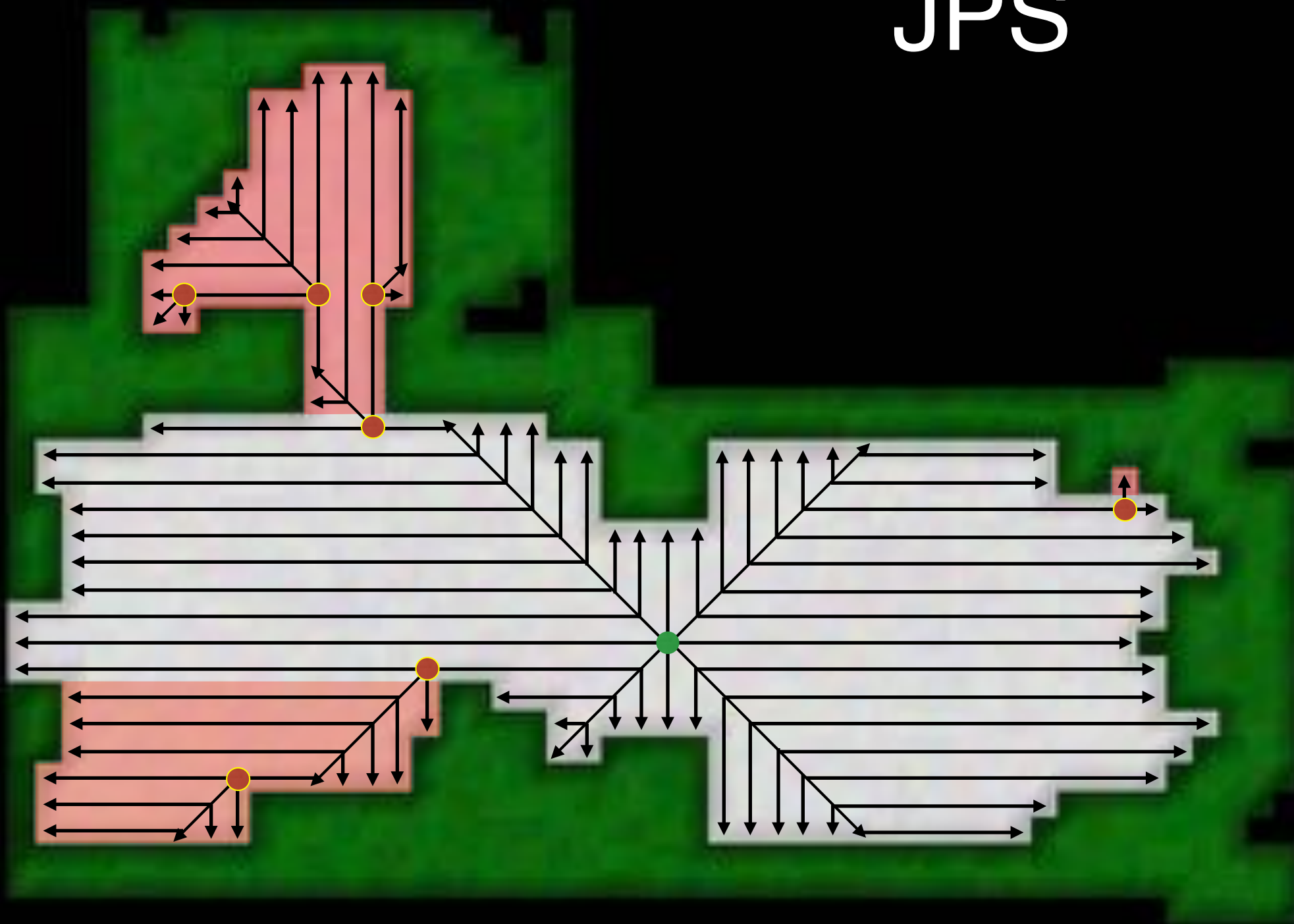


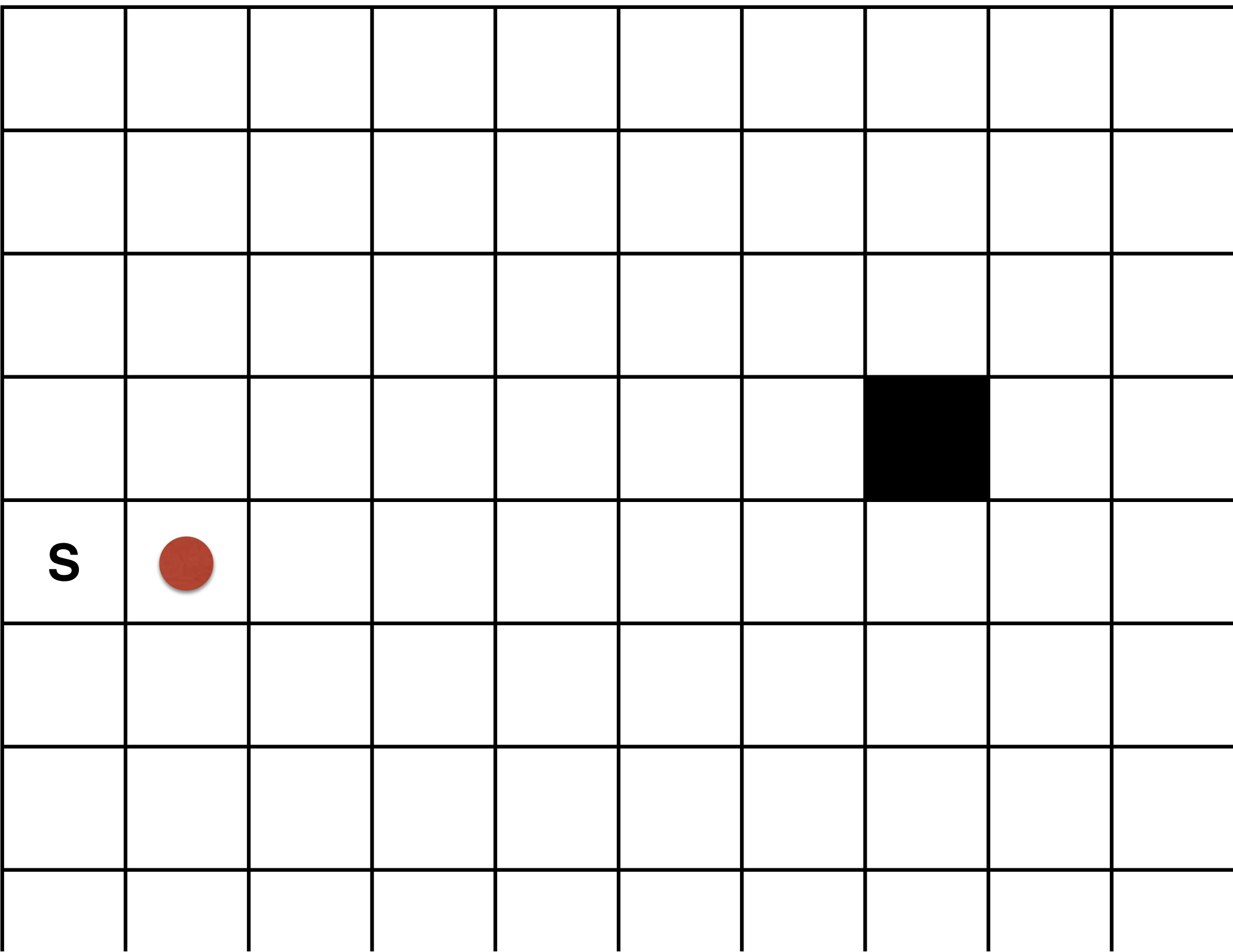


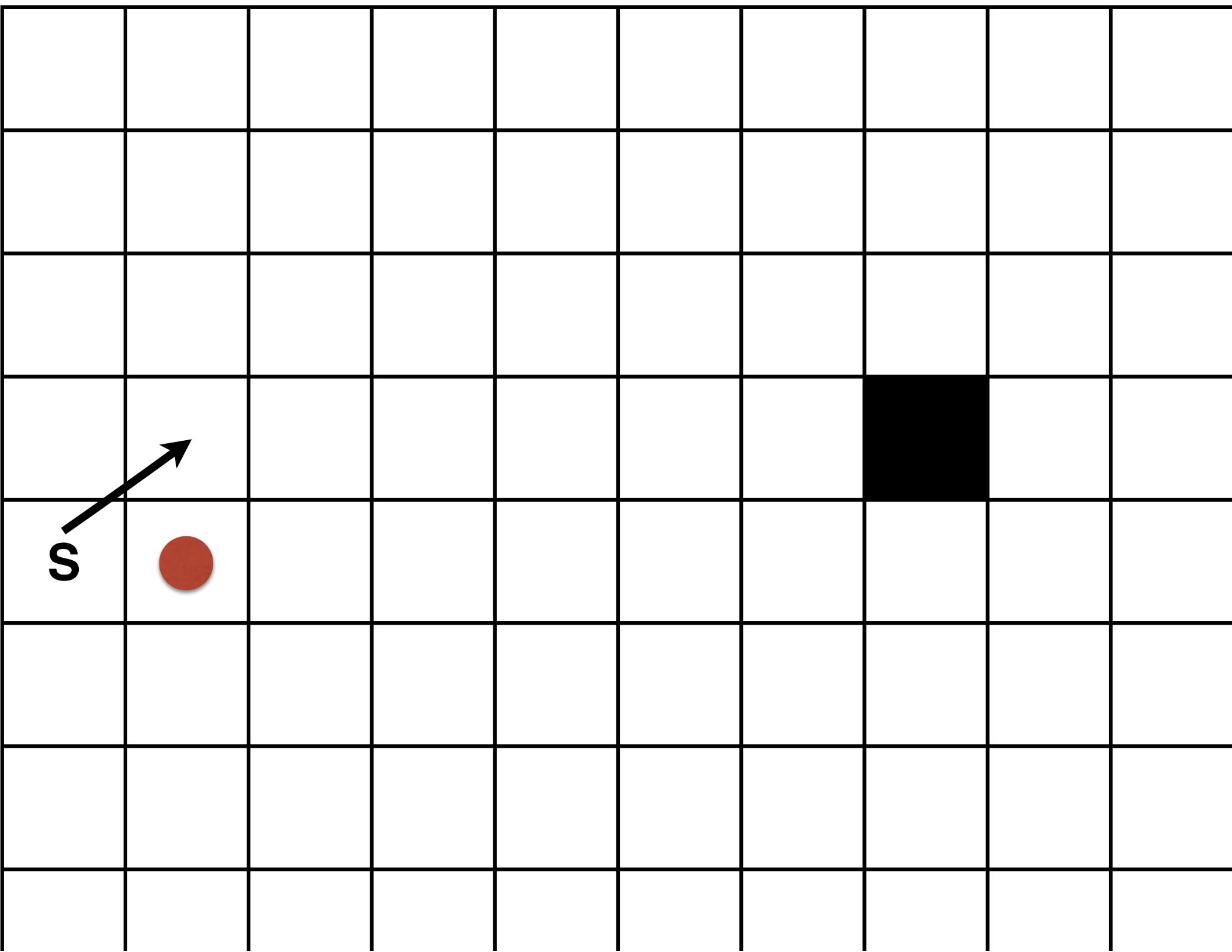
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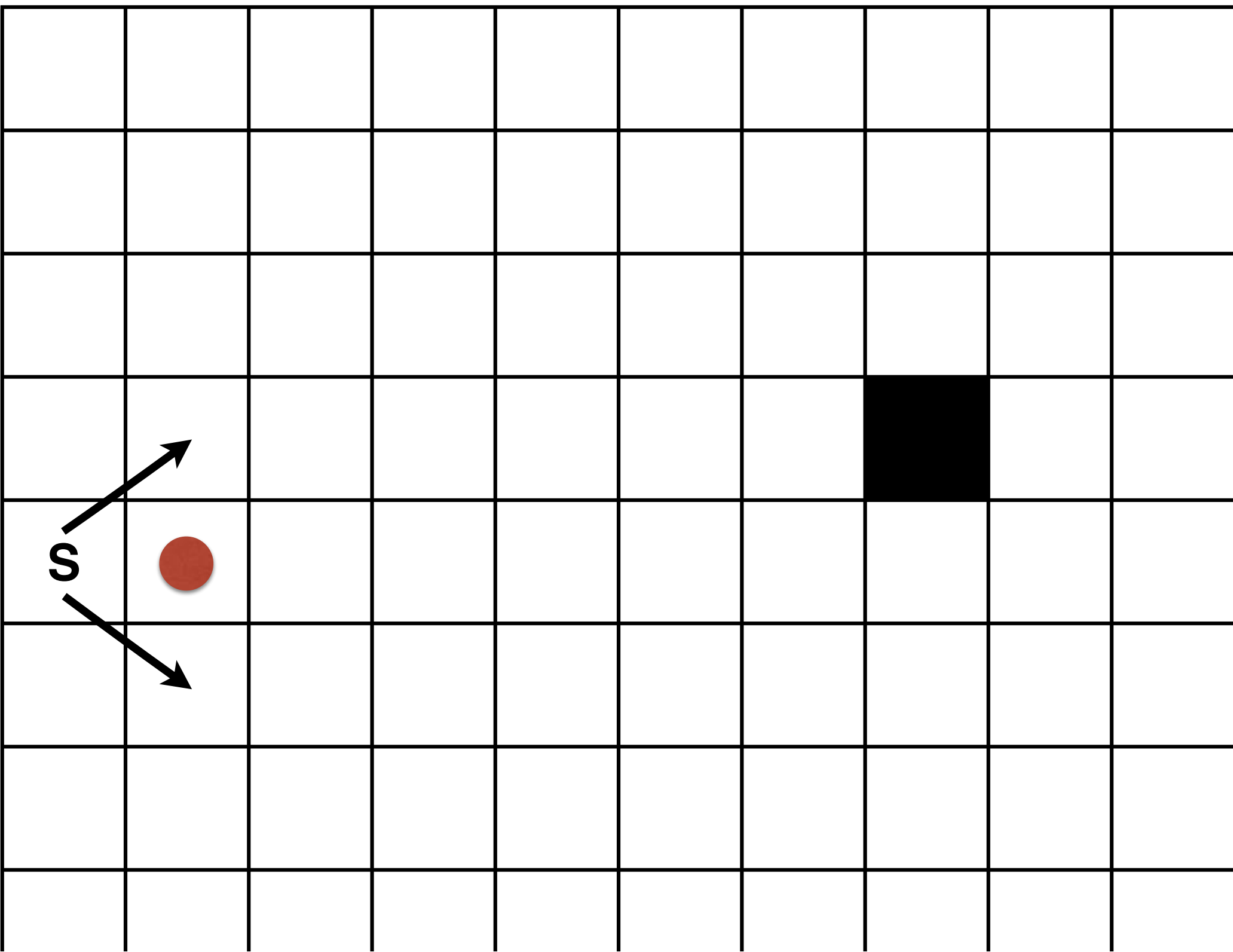


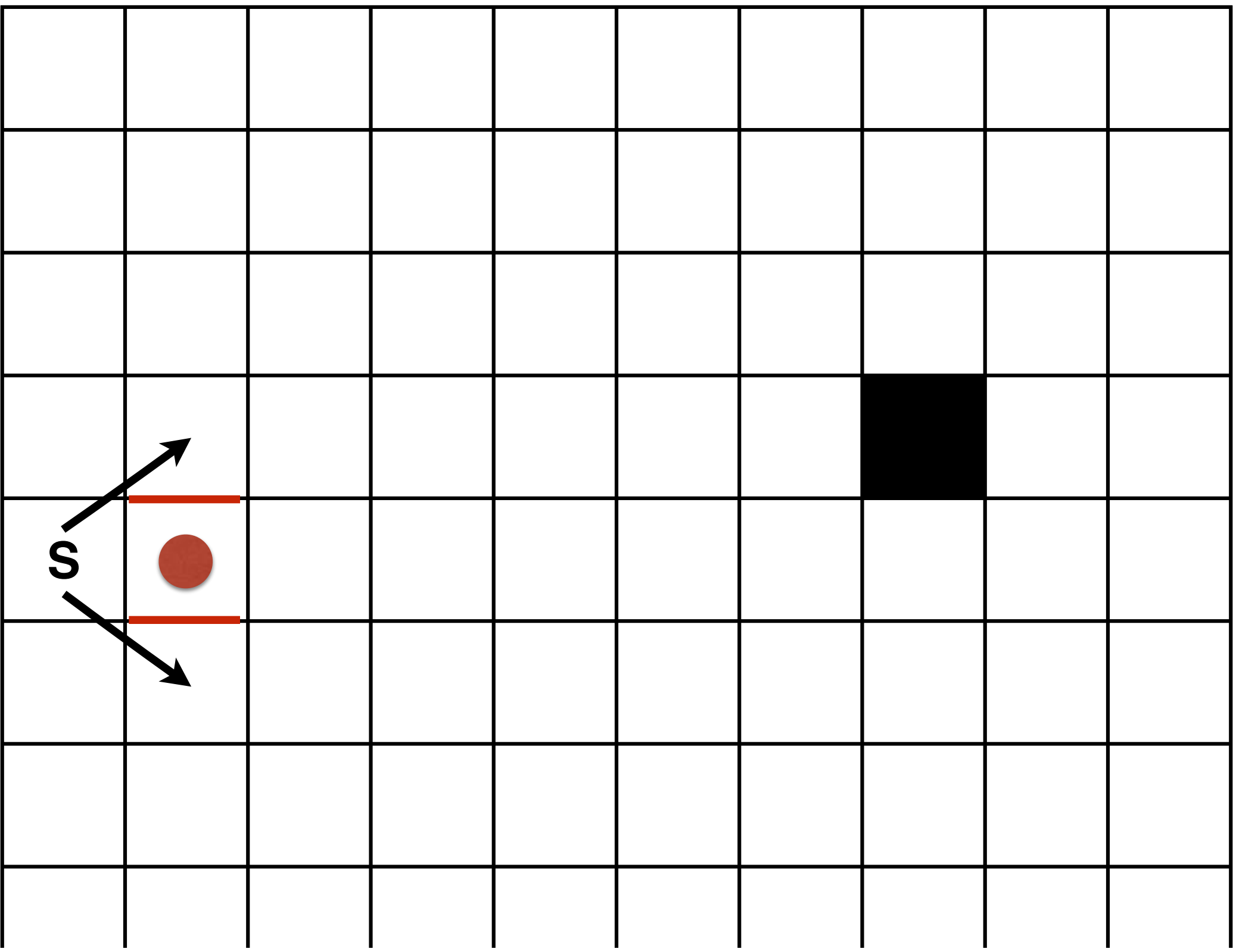
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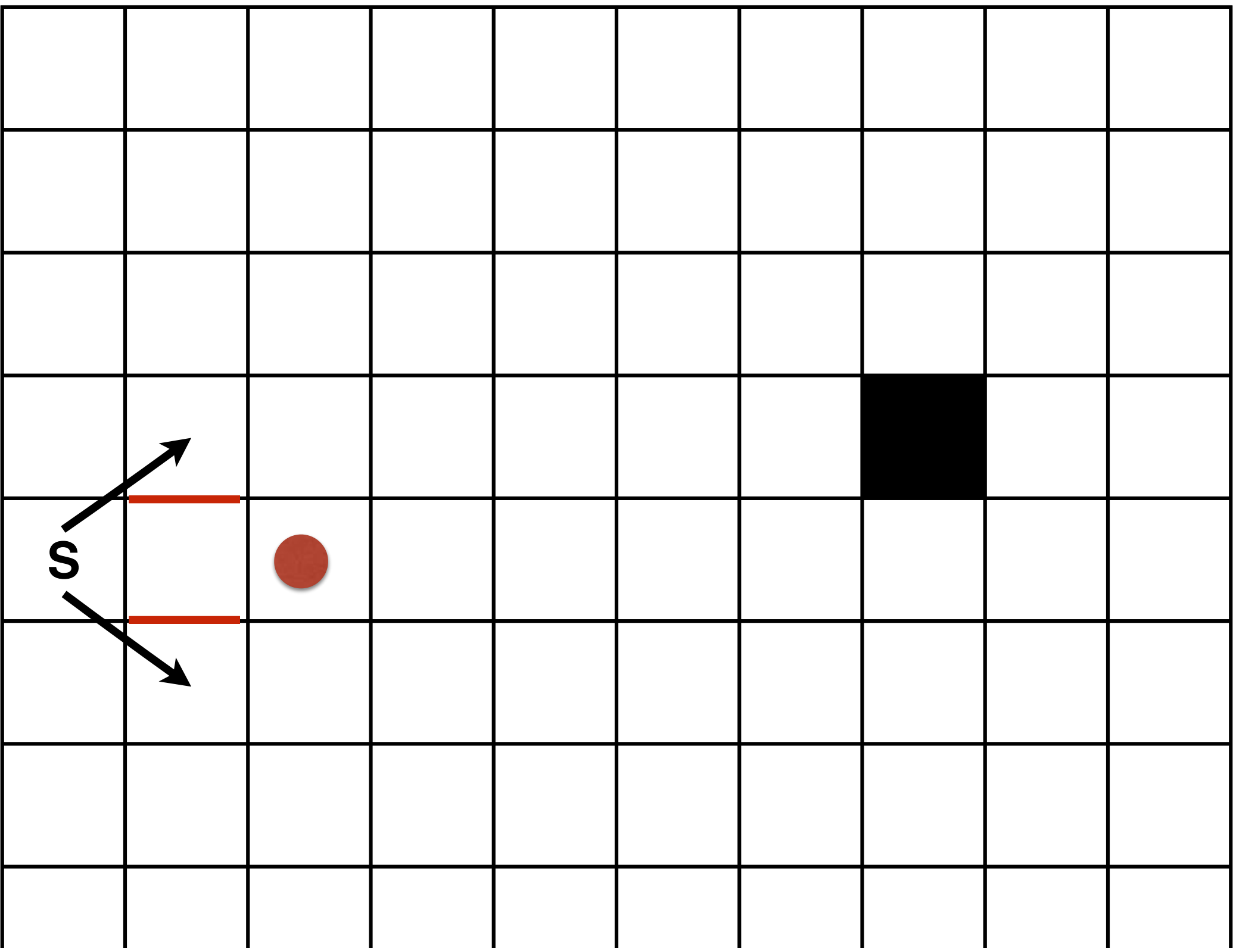






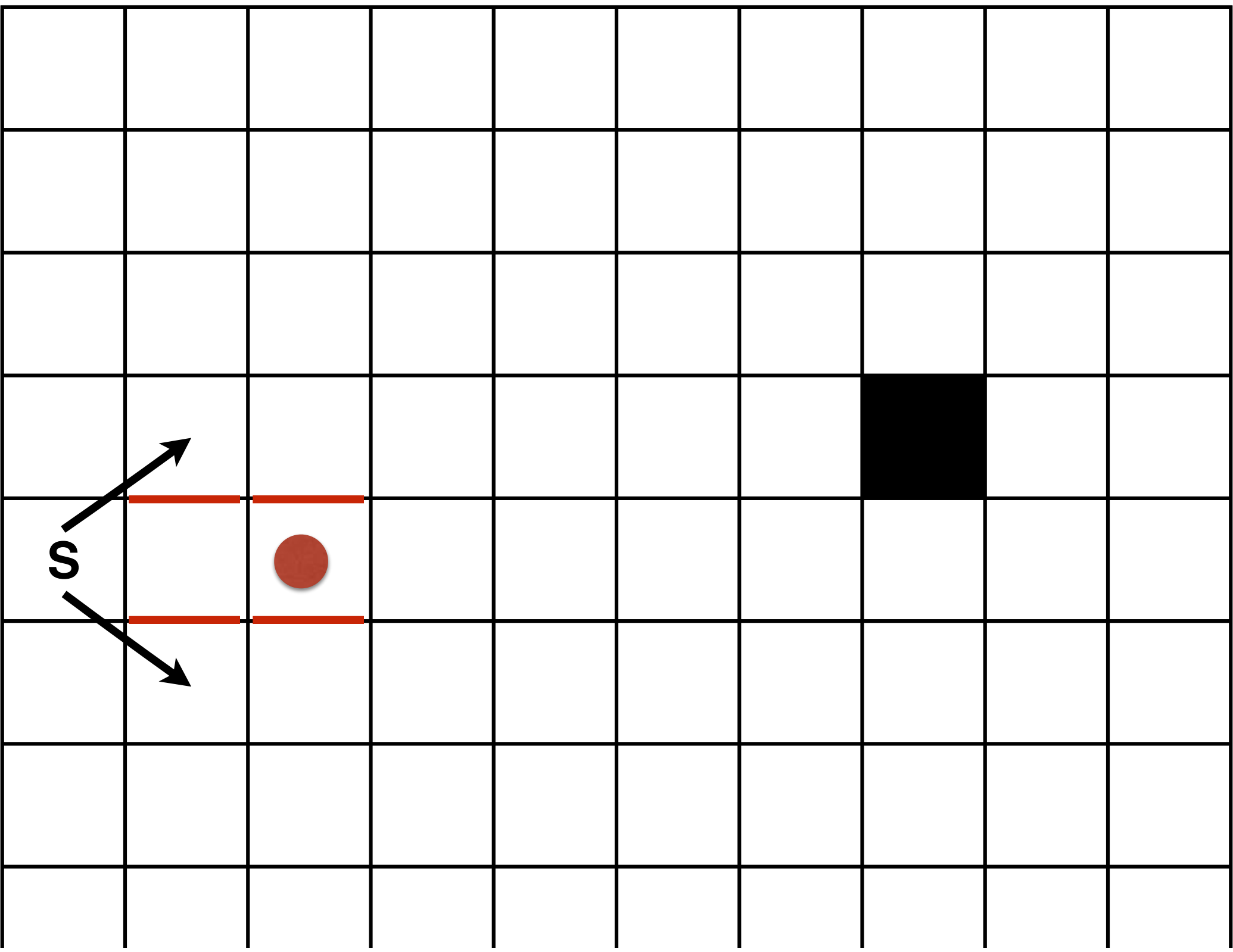




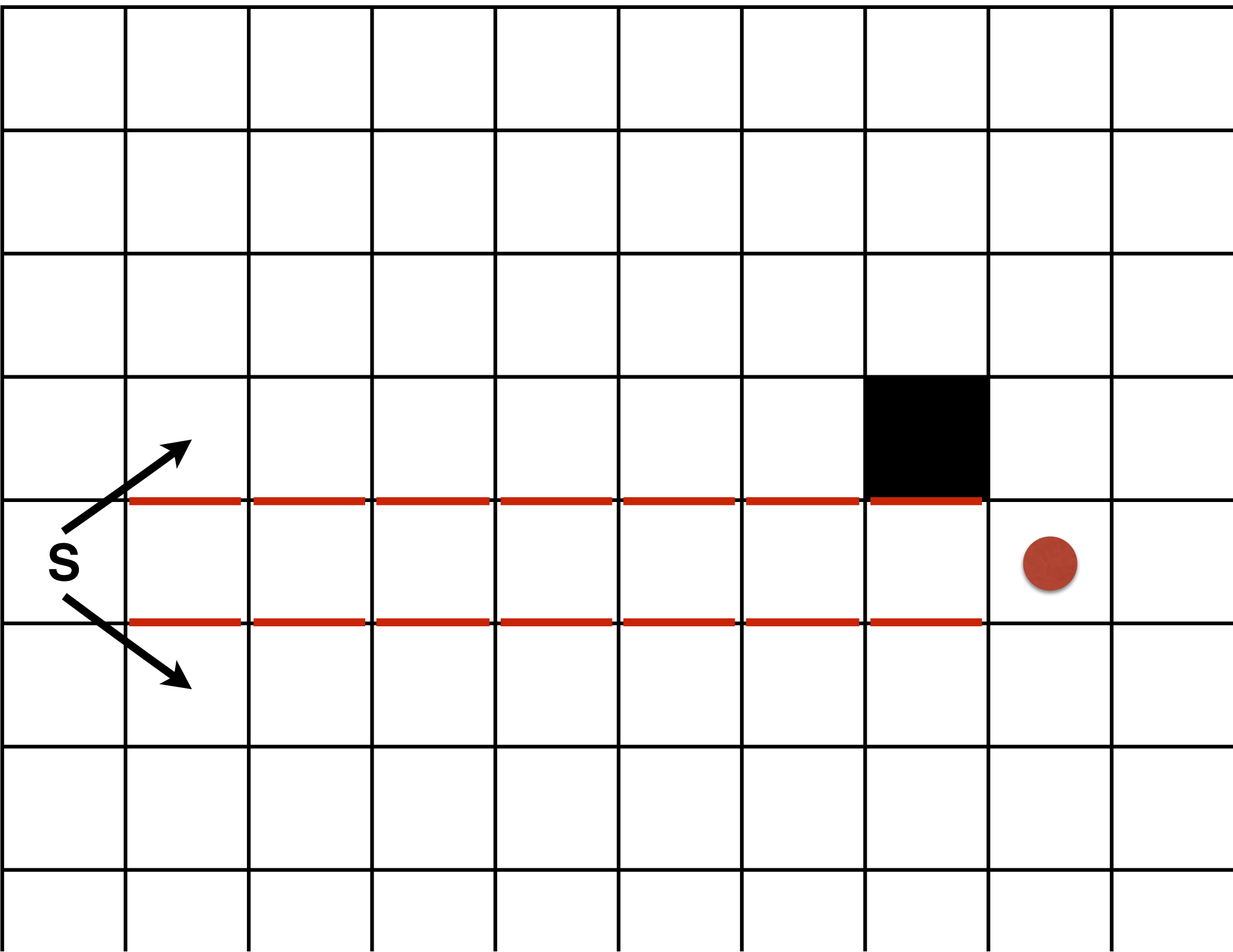


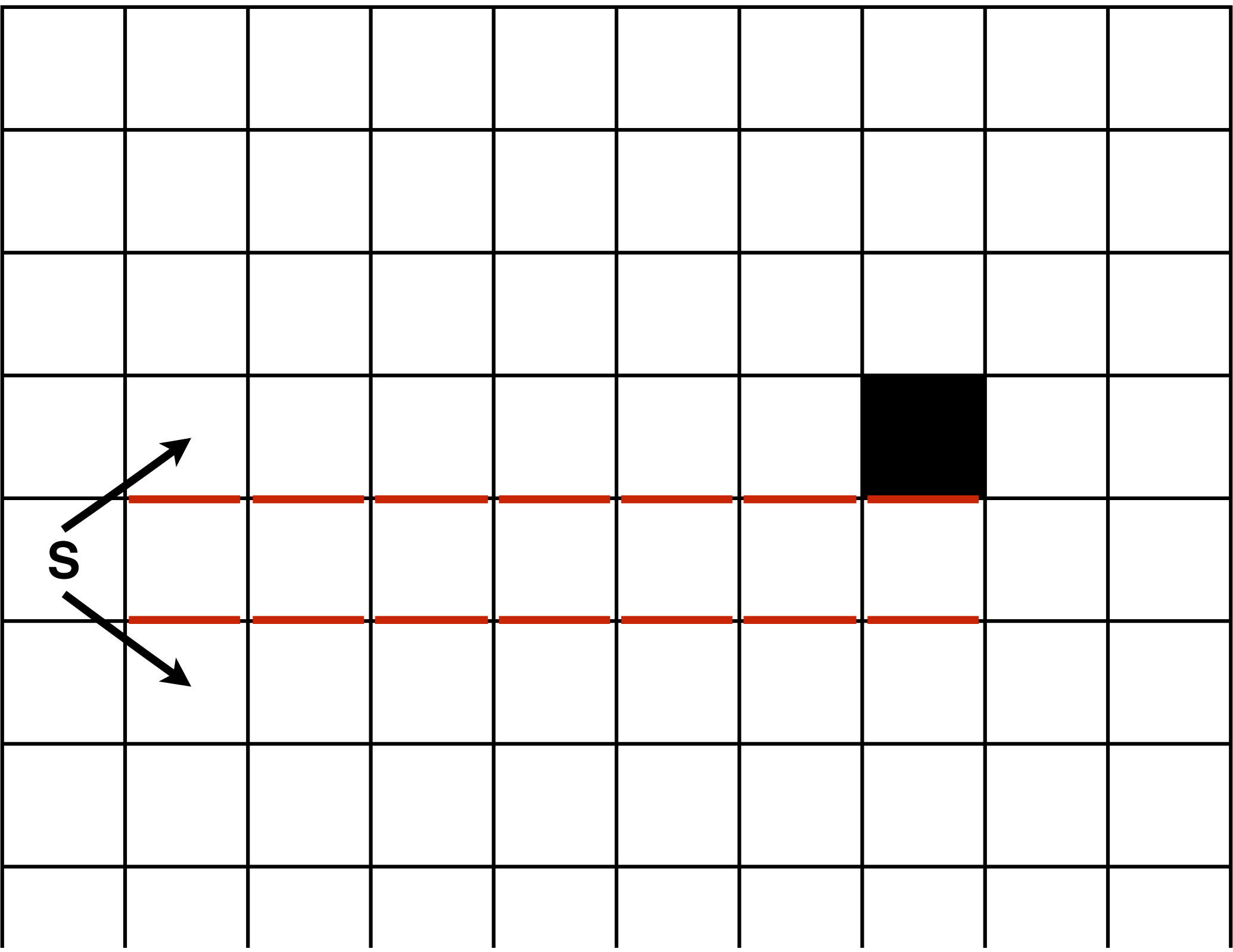
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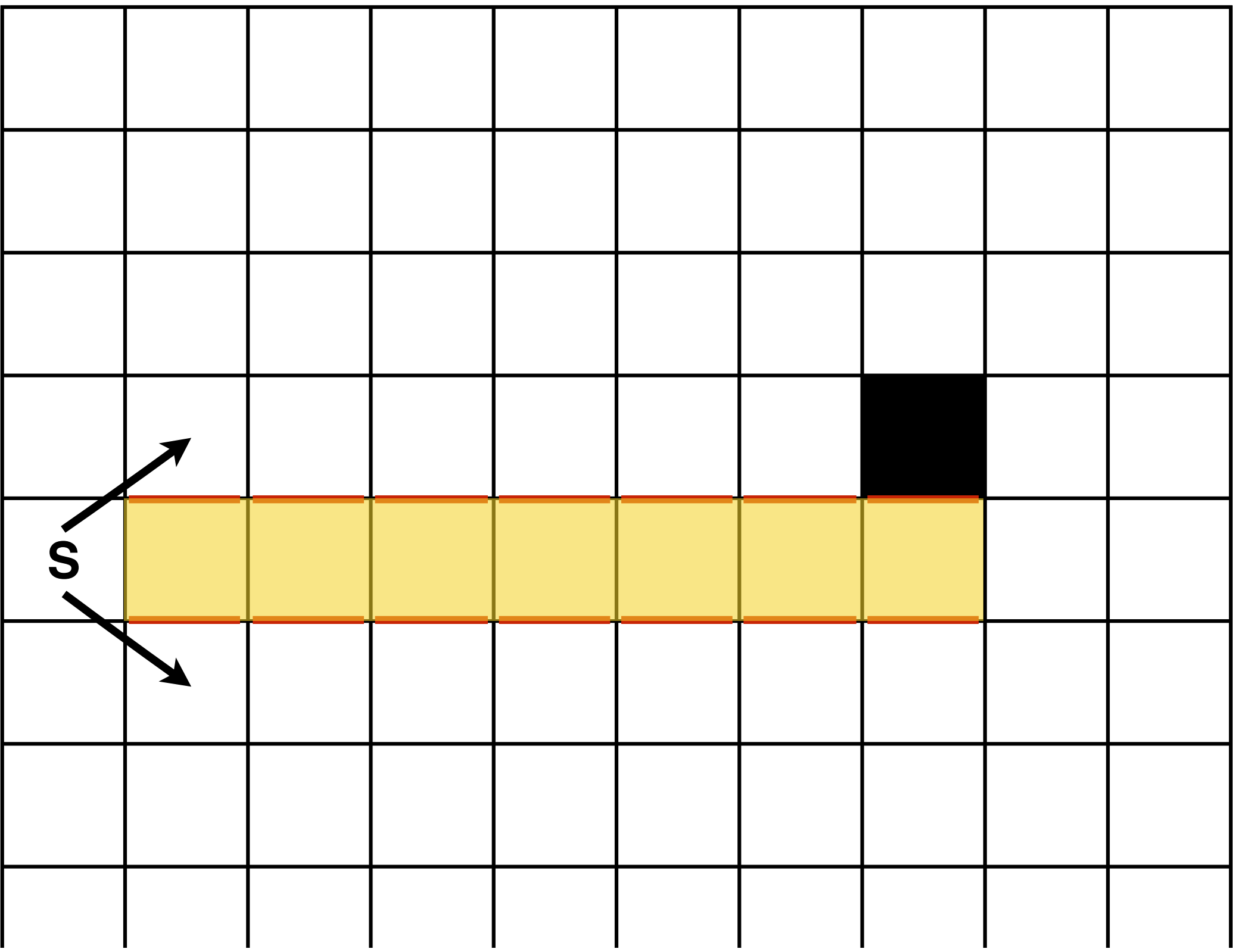






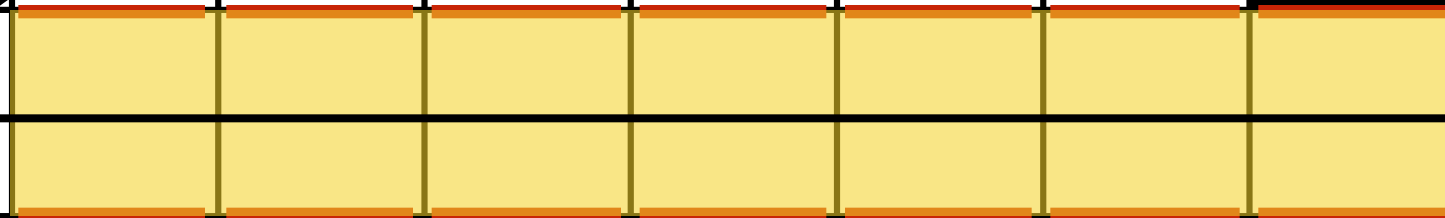
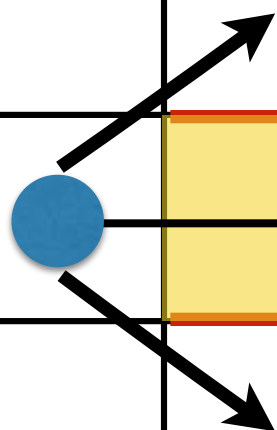






s





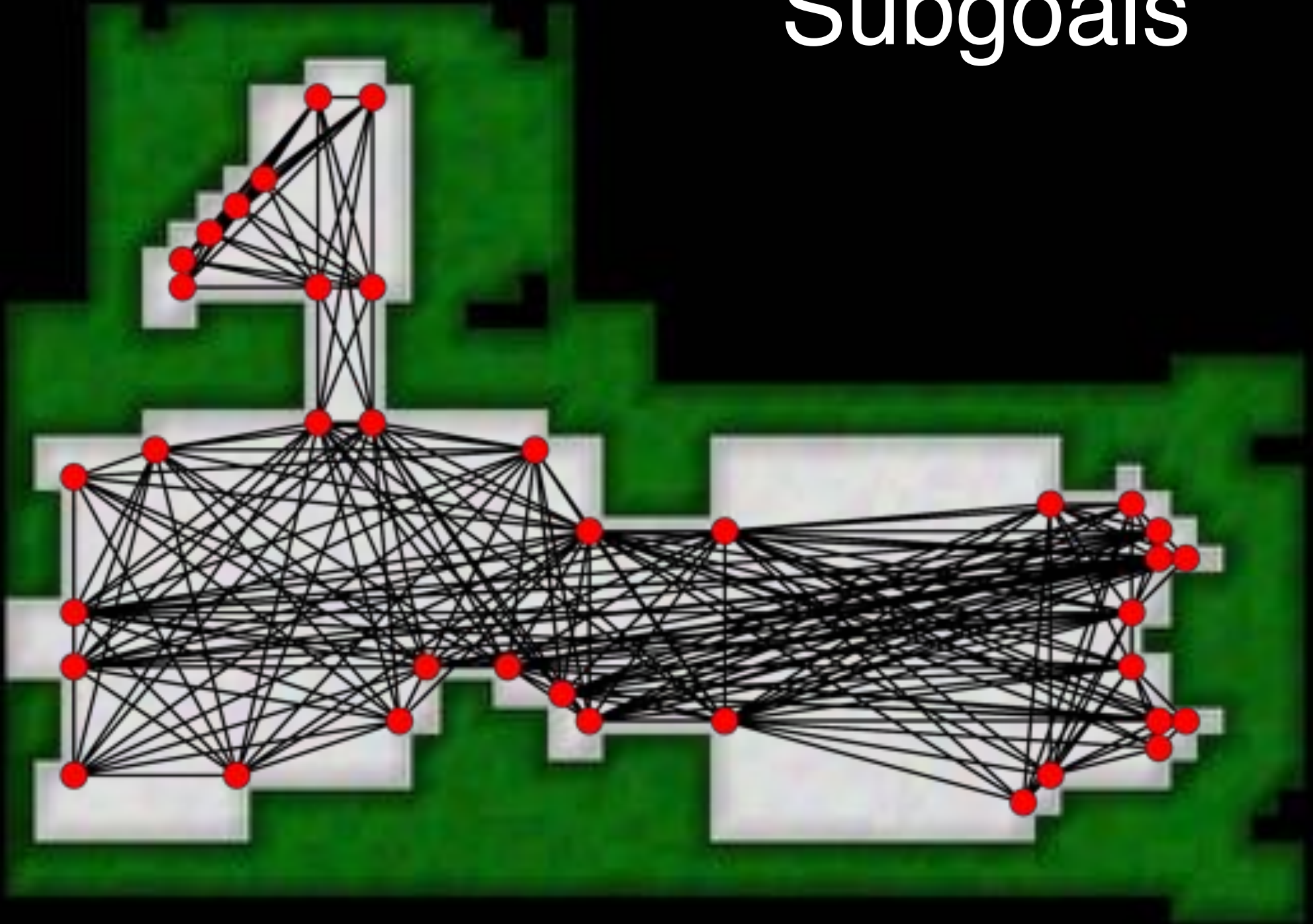
# Subgoals



# Subgoals



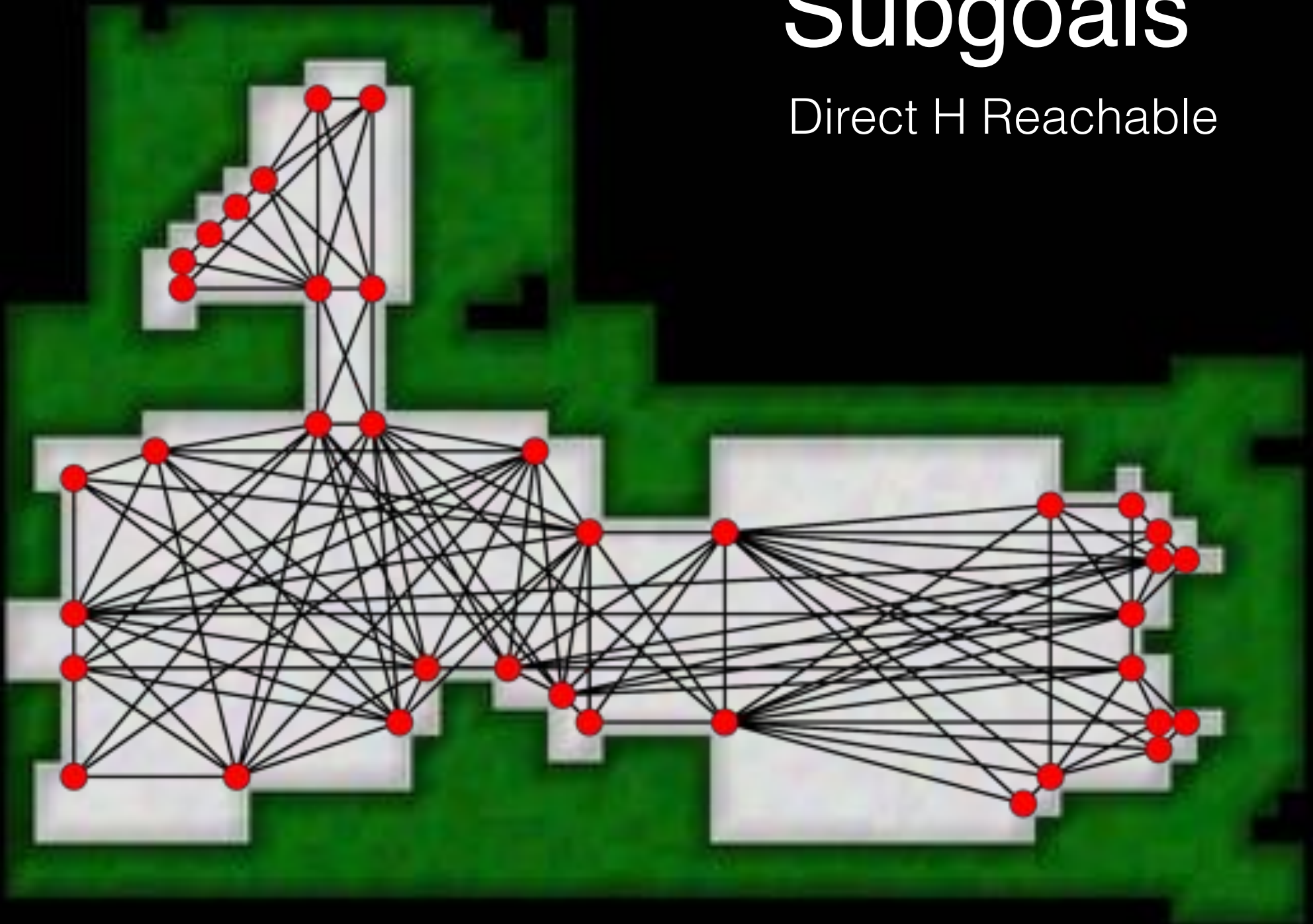
# Subgoals





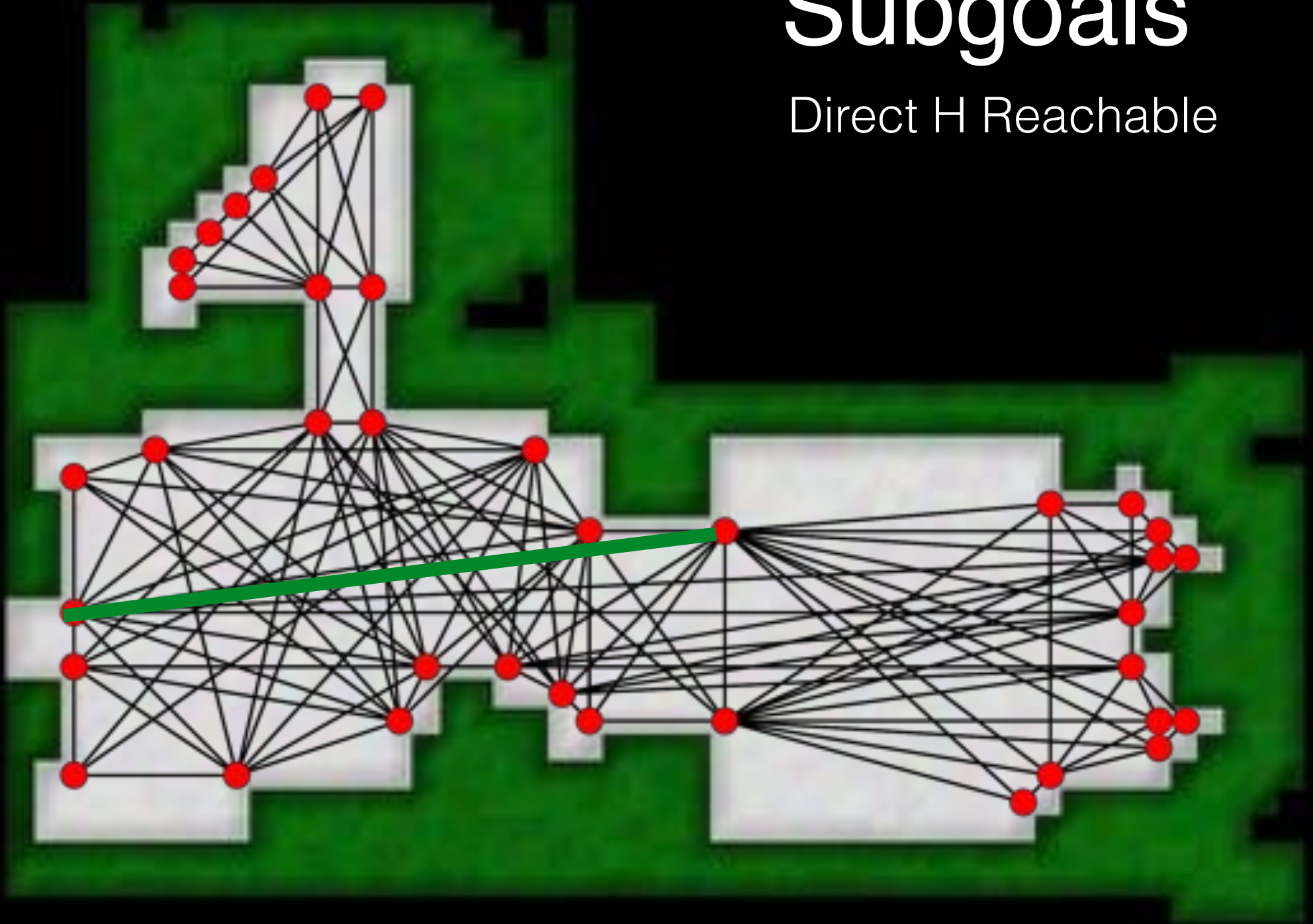
# Subgoals

Direct H Reachable



# Subgoals

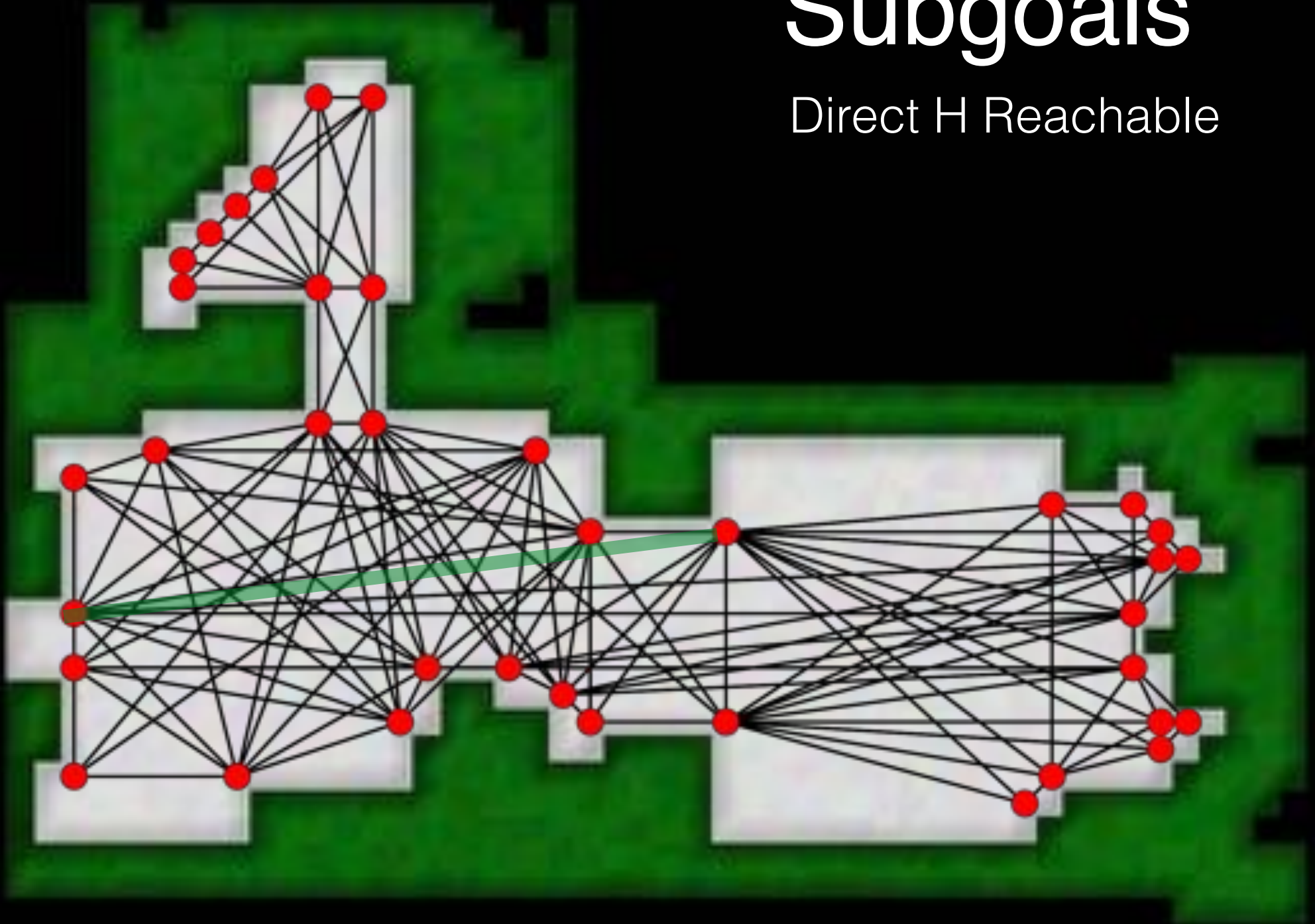
Direct H Reachable





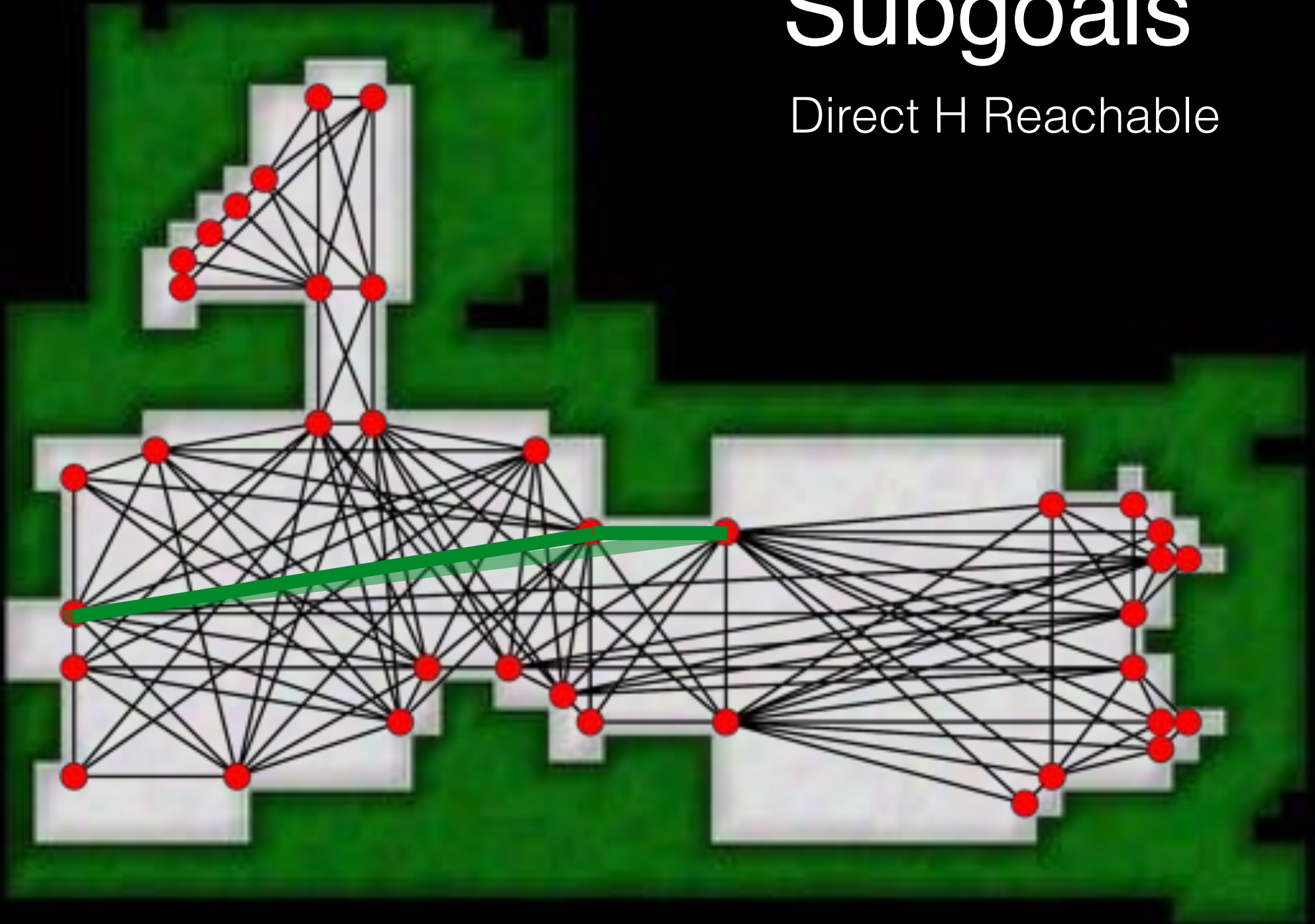
# Subgoals

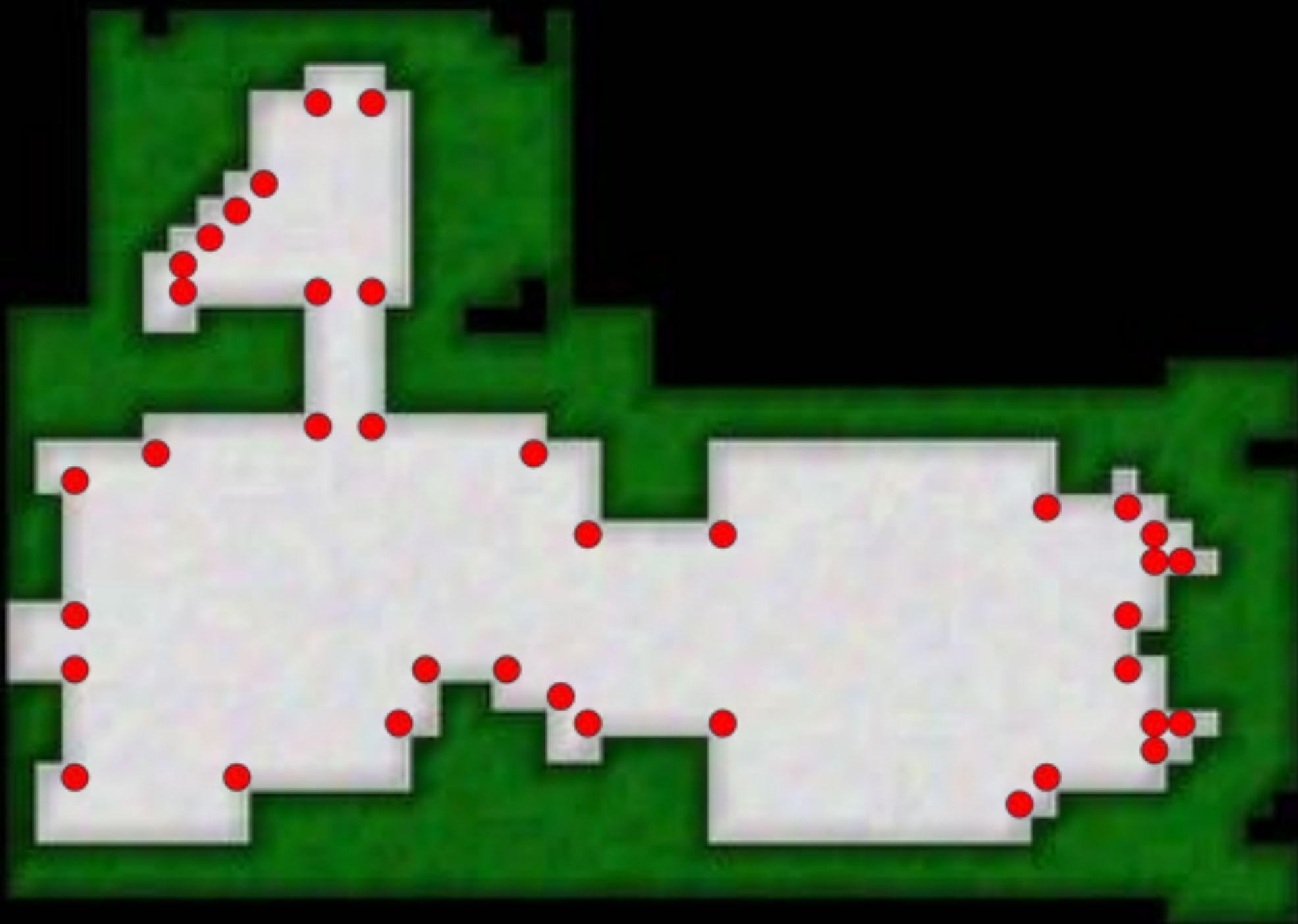
Direct H Reachable



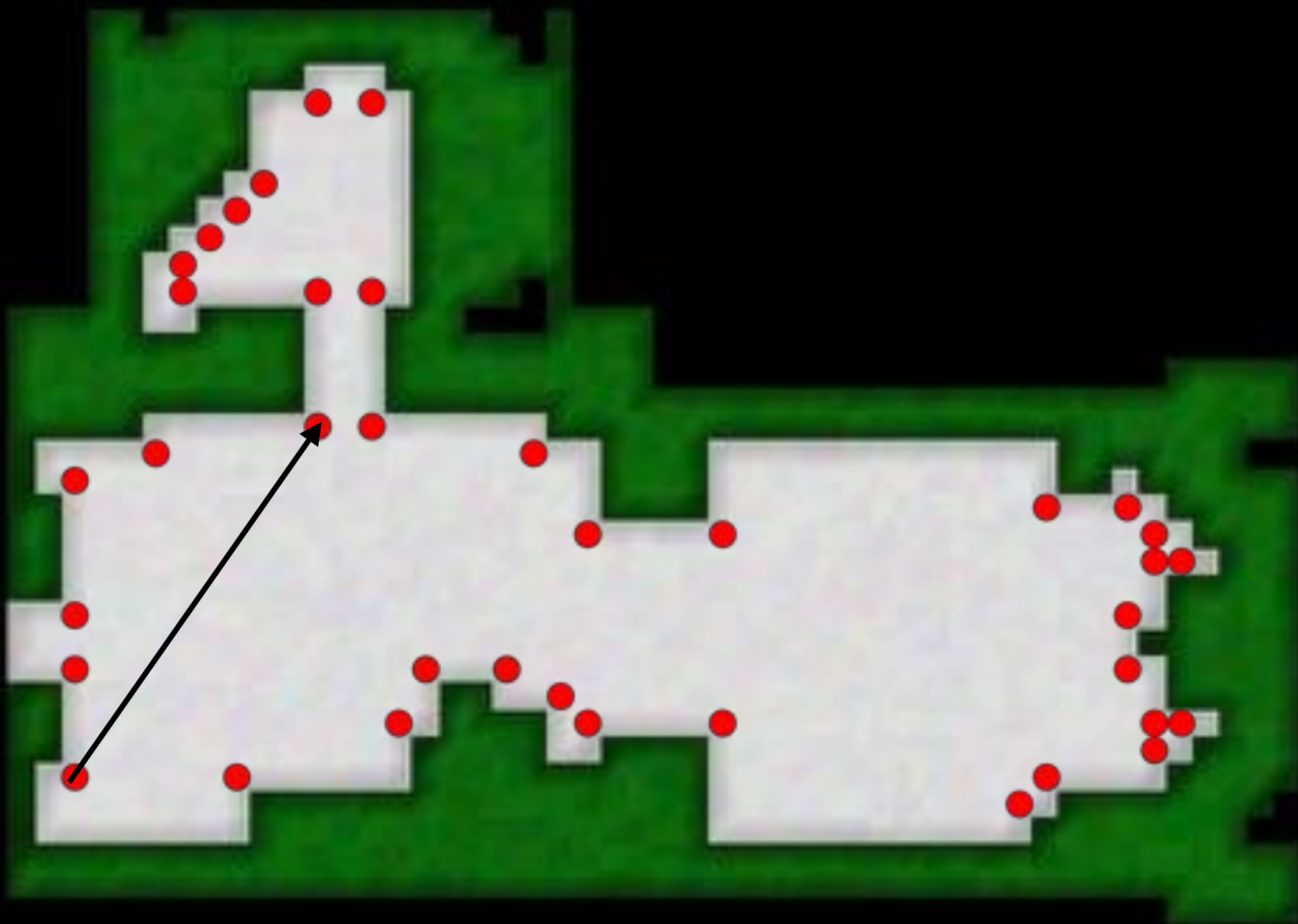
# Subgoals

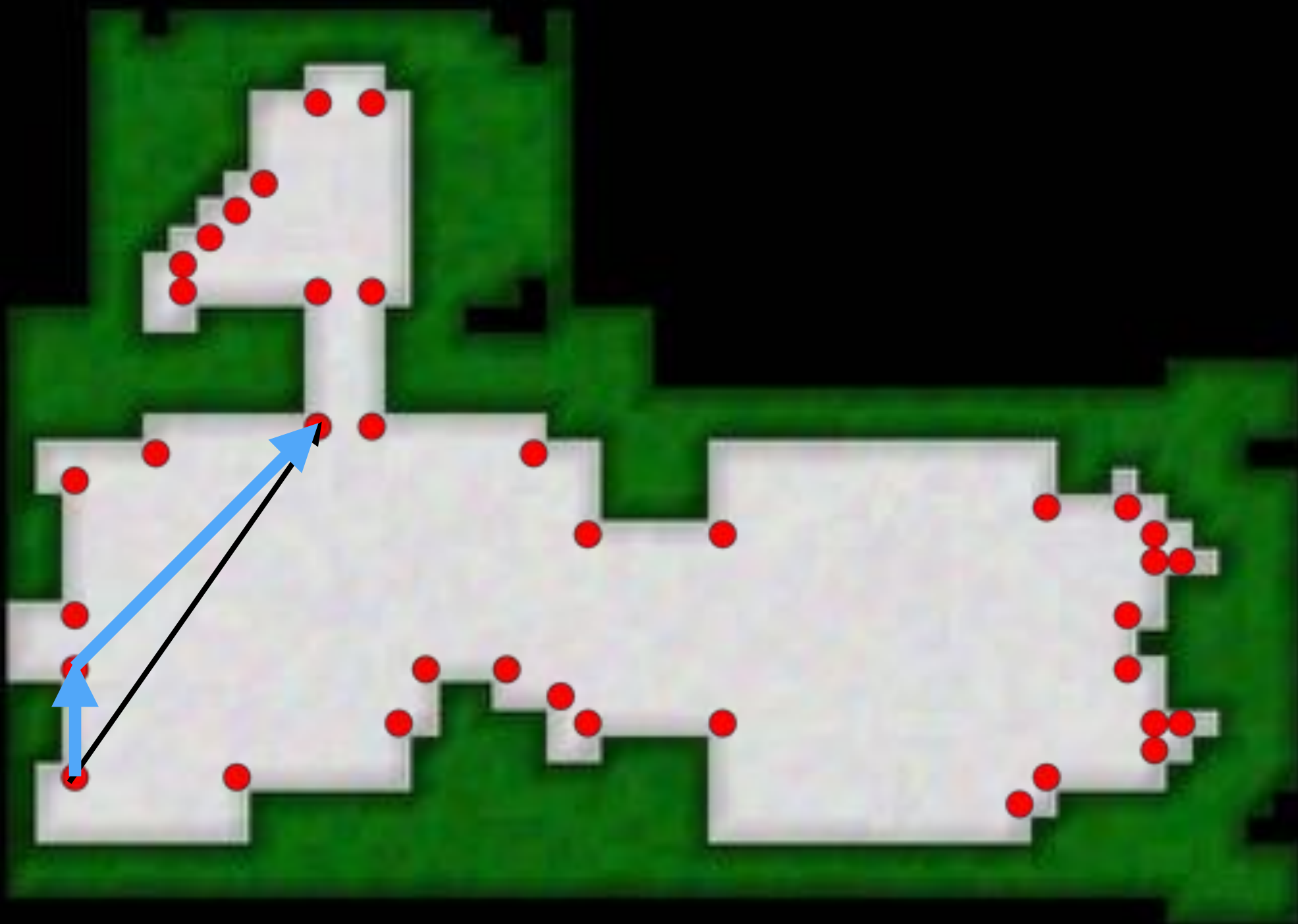
Direct H Reachable

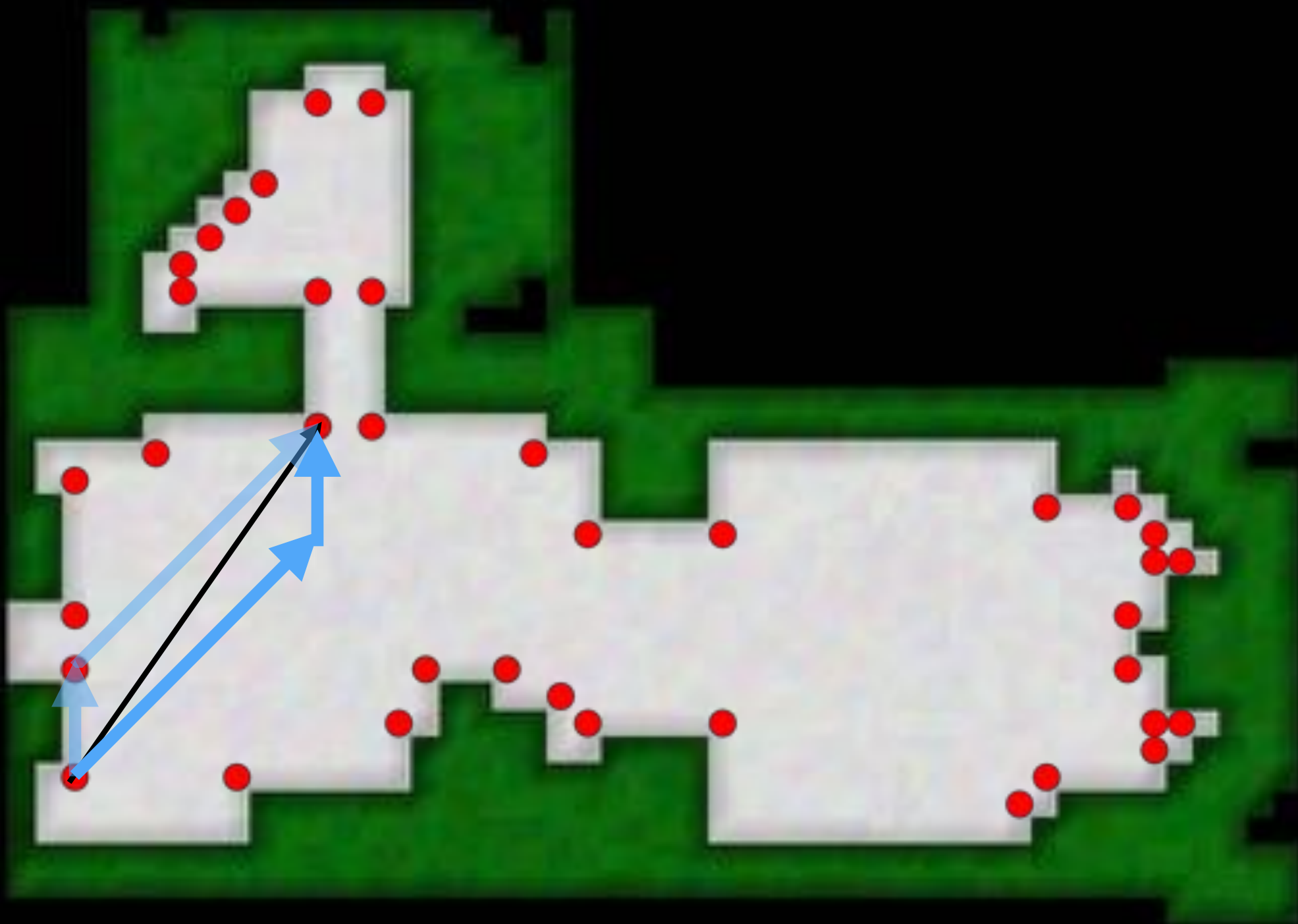




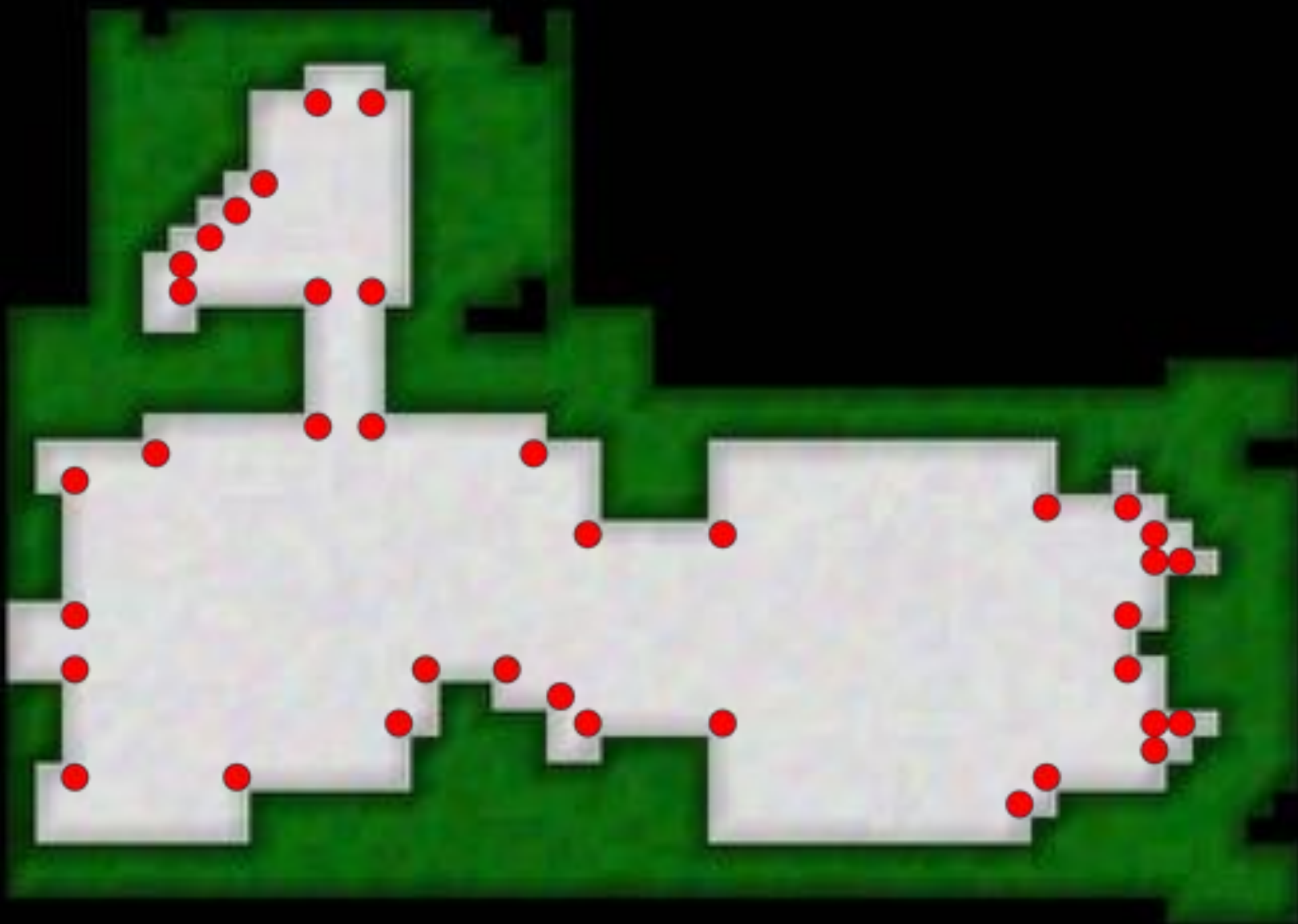














# Other contractions

- Dead-end heuristic
  - Yngvi Björnsson and Kári Halldórsson, 2006
- Swamps
  - Nir Pochter, Aviv Zohar, Jeffrey S. Rosenschein, Ariel Felner [2008 - 2010]
- Dead/redundant states
  - N.R. Sturtevant, V. Bulitko and Y. Bjornsson, 2010
- What is the correct way to contract a map?

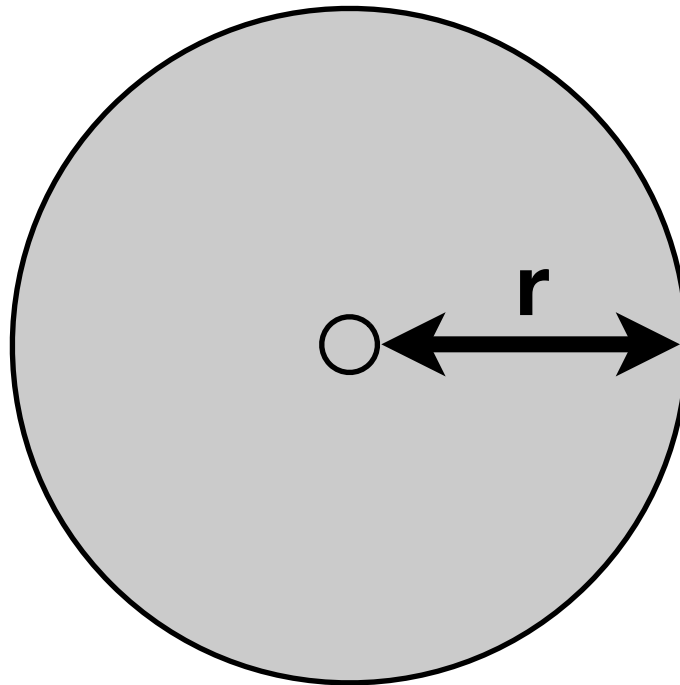
# Highway Dimension

Highway Dimension, Shortest  
Paths, and Provably Efficient  
Algorithms [Abraham et. al., 2010]



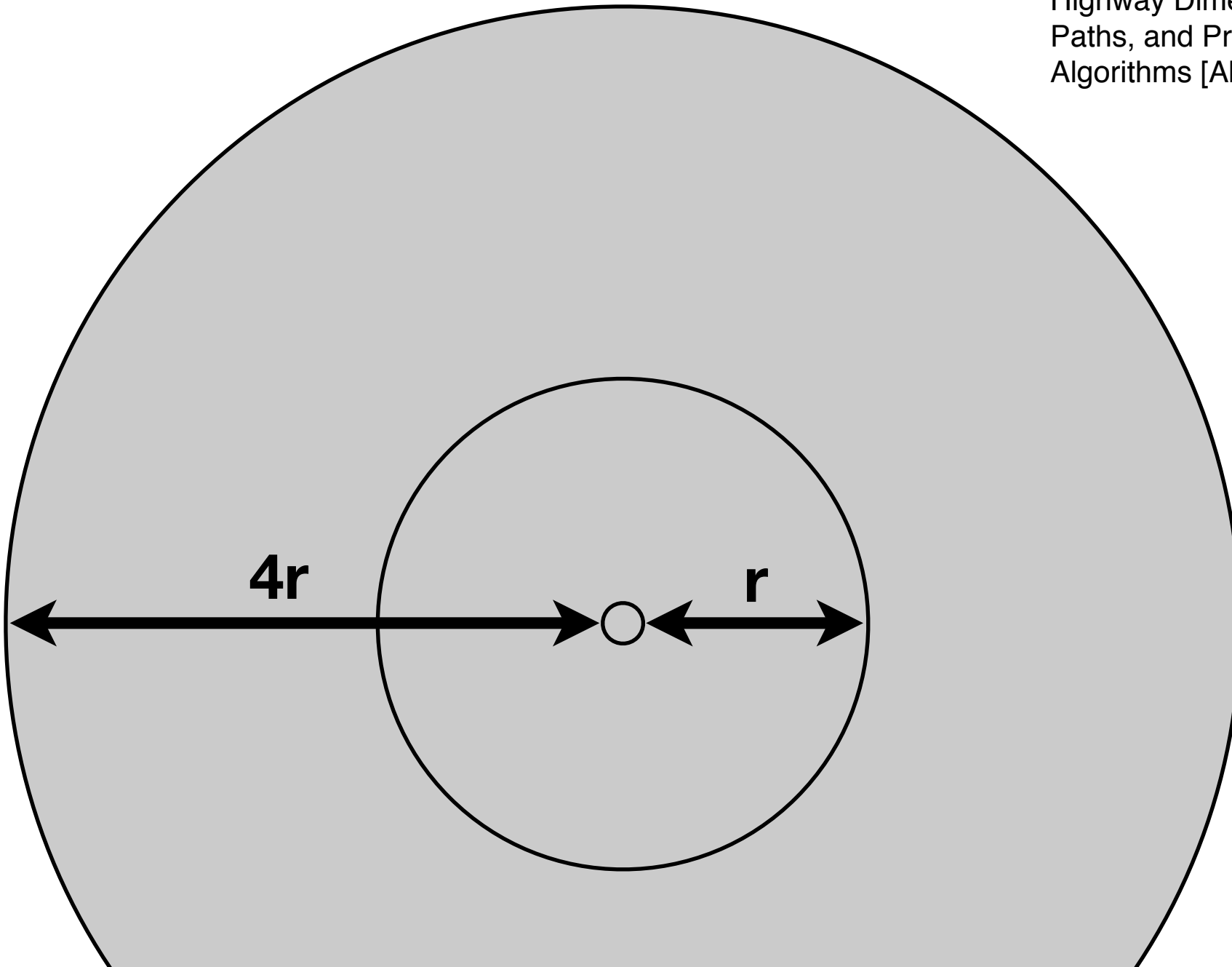
# Highway Dimension

Highway Dimension, Shortest  
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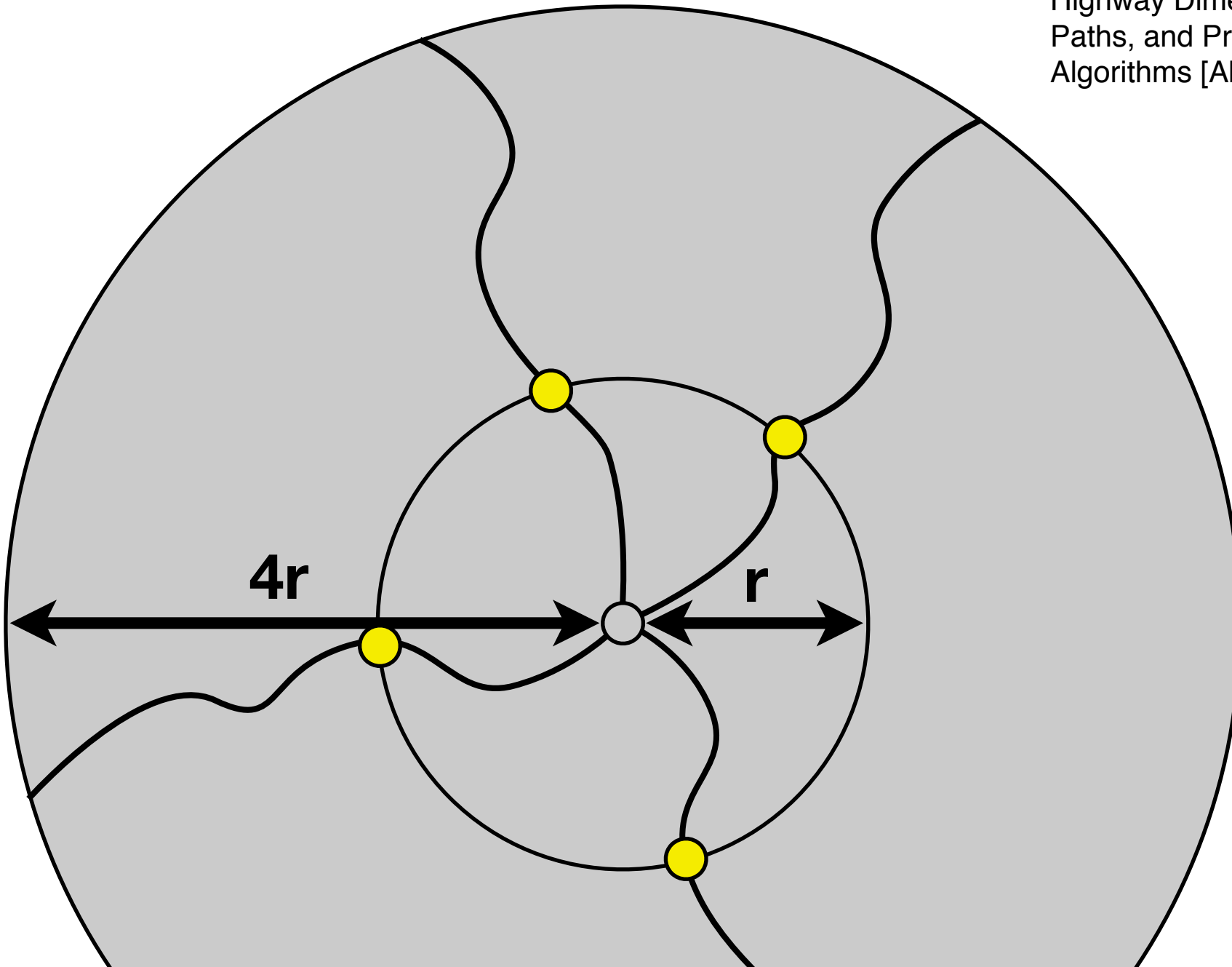
# Highway Dimension

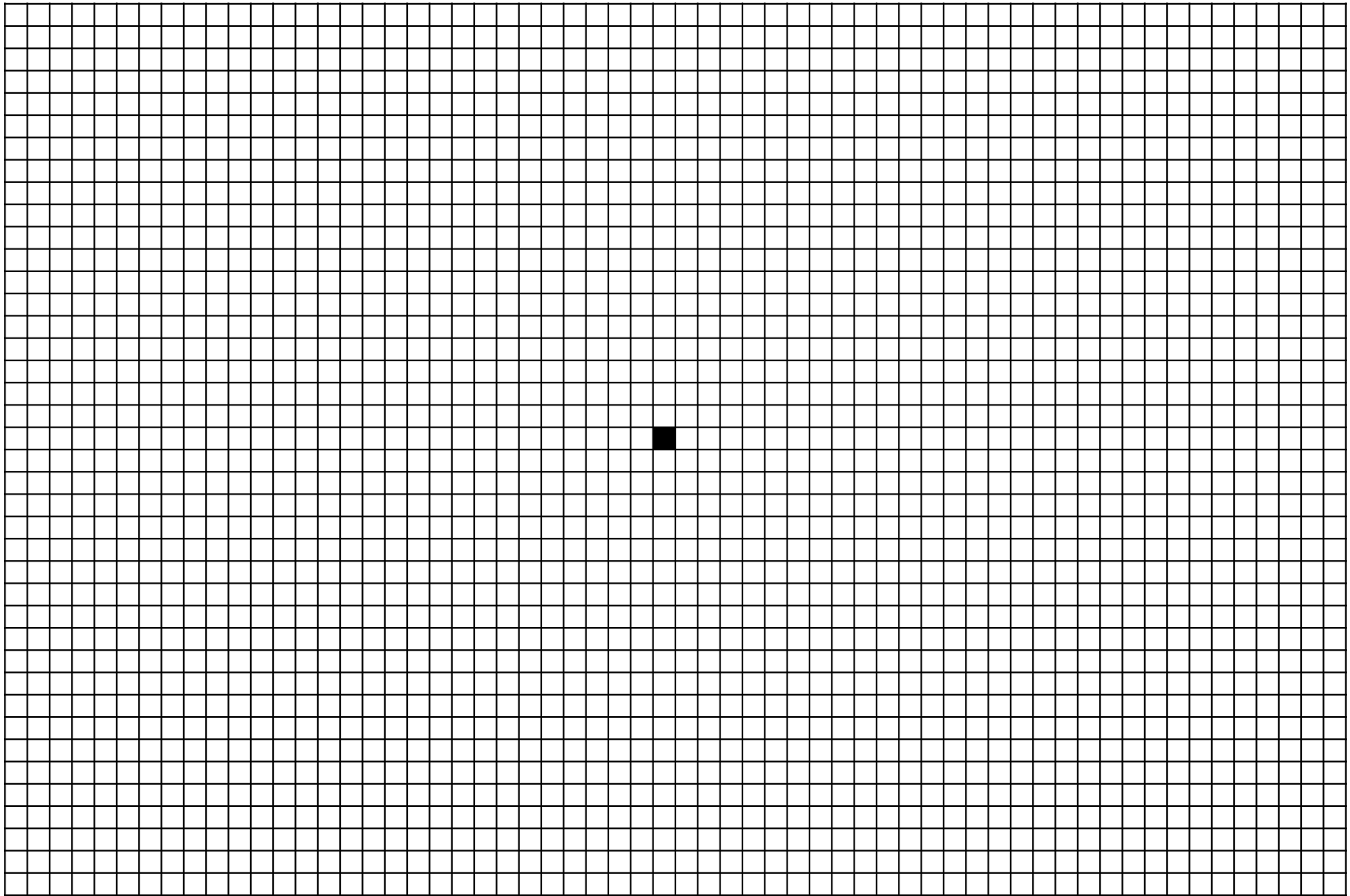
Highway Dimension, Shortest  
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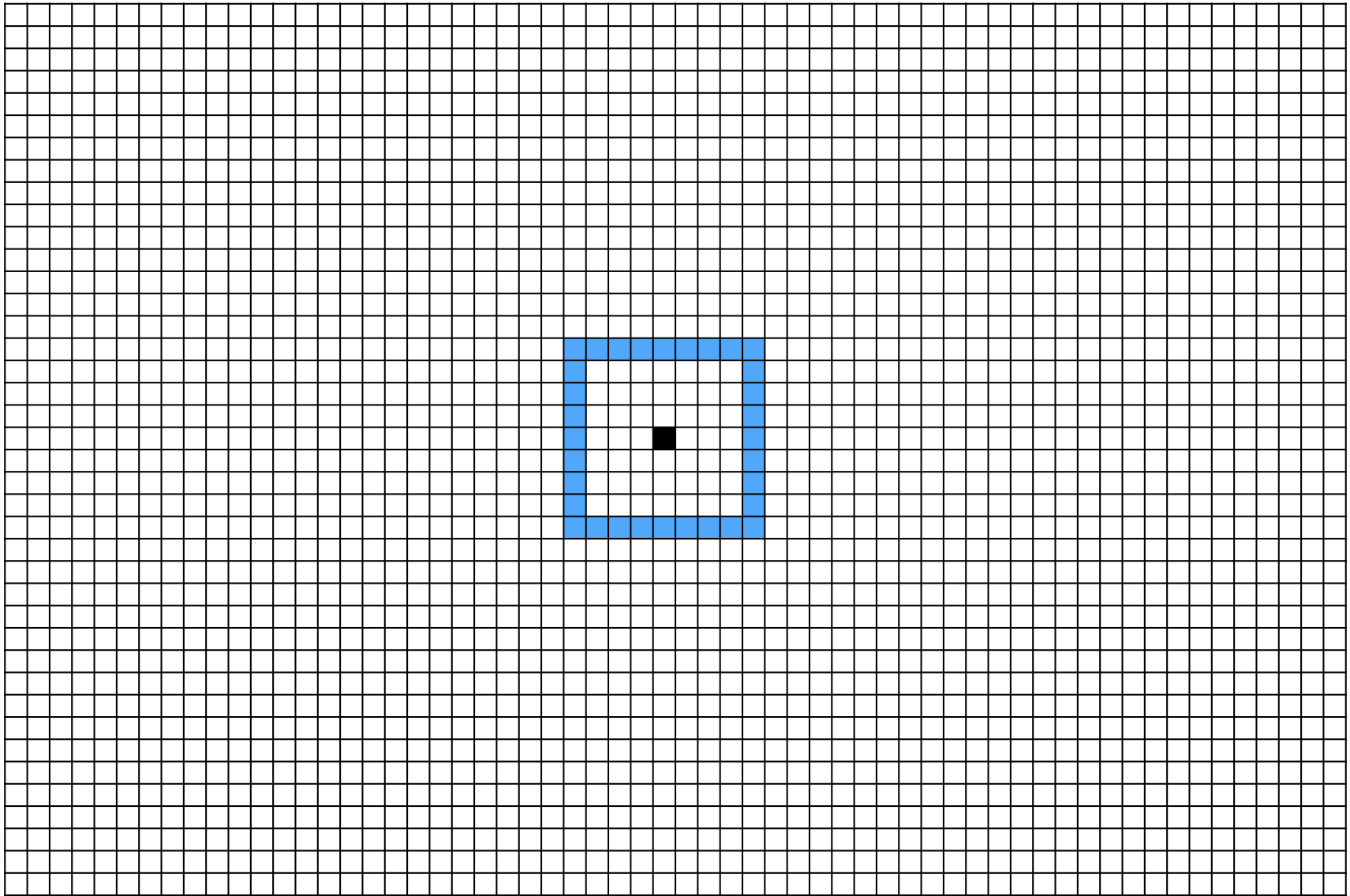


# Highway Dimension

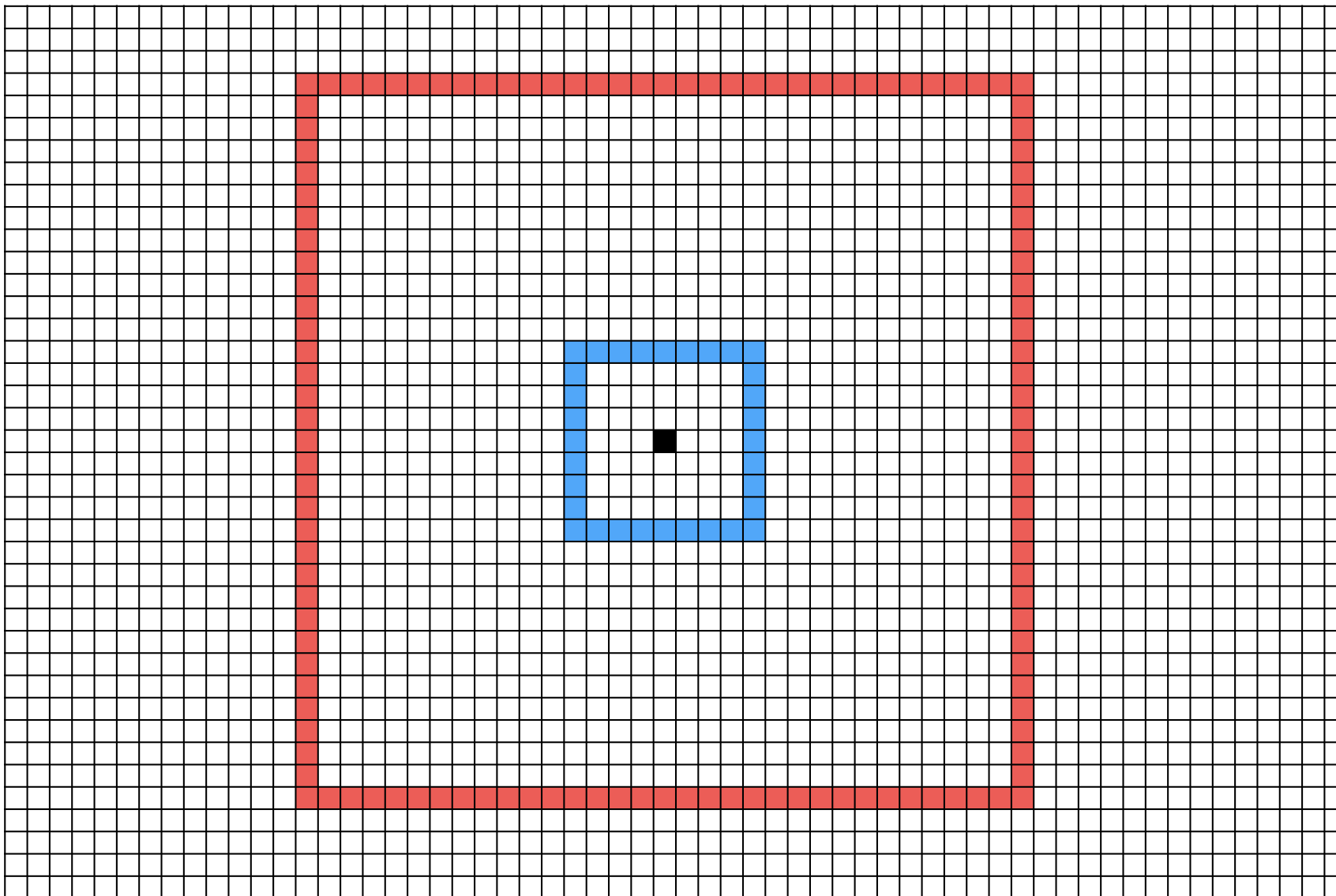
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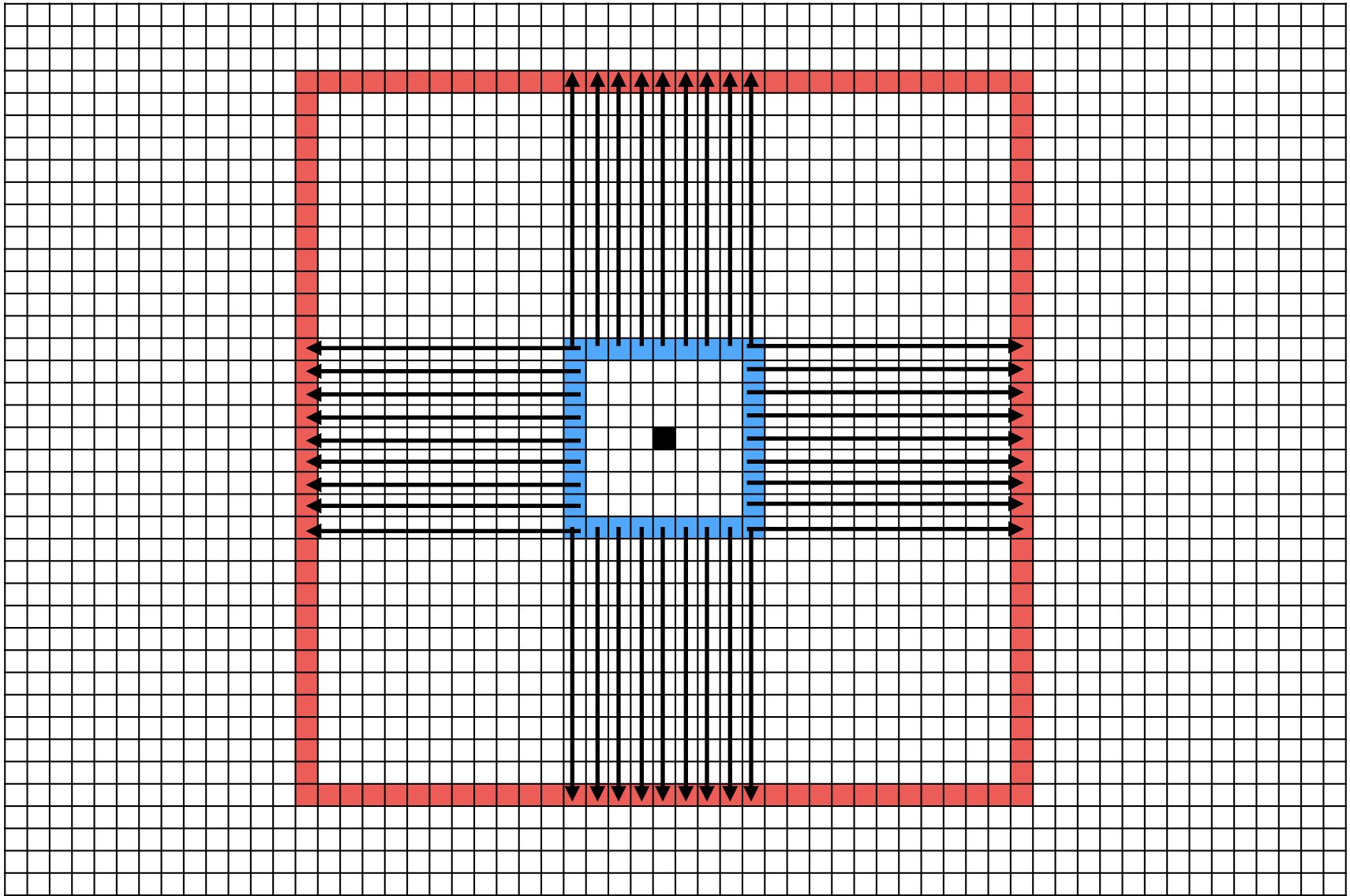


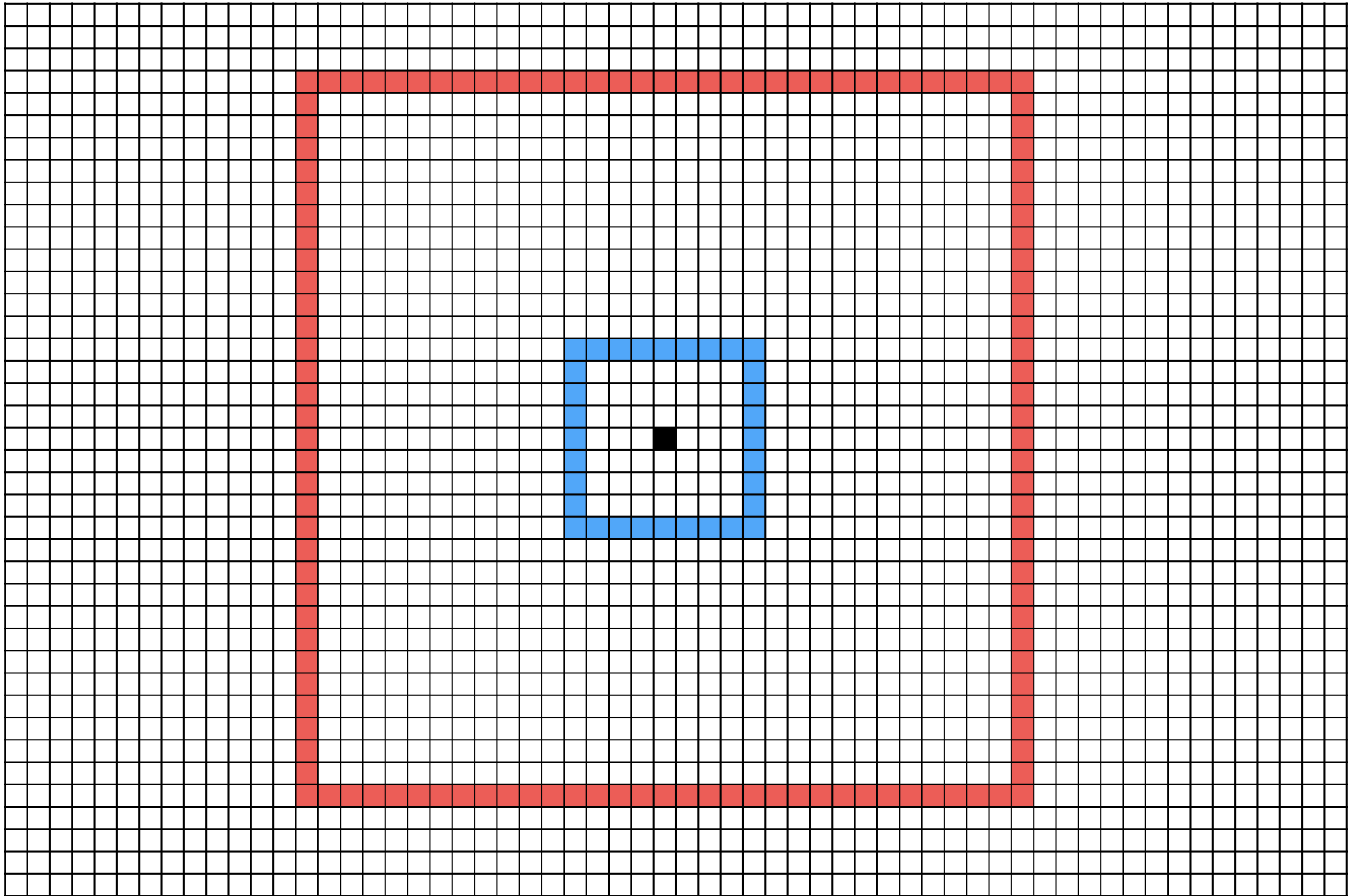


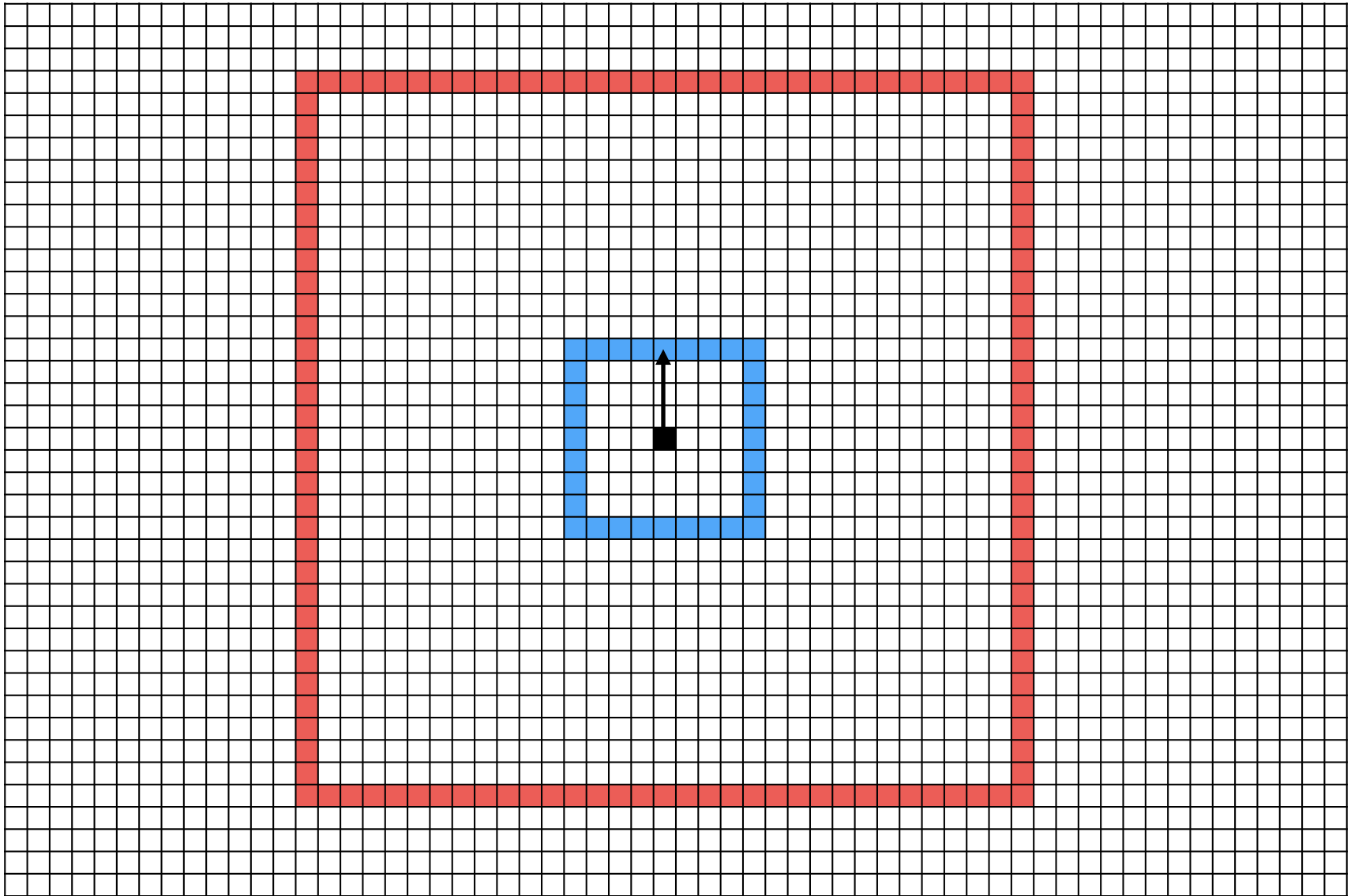


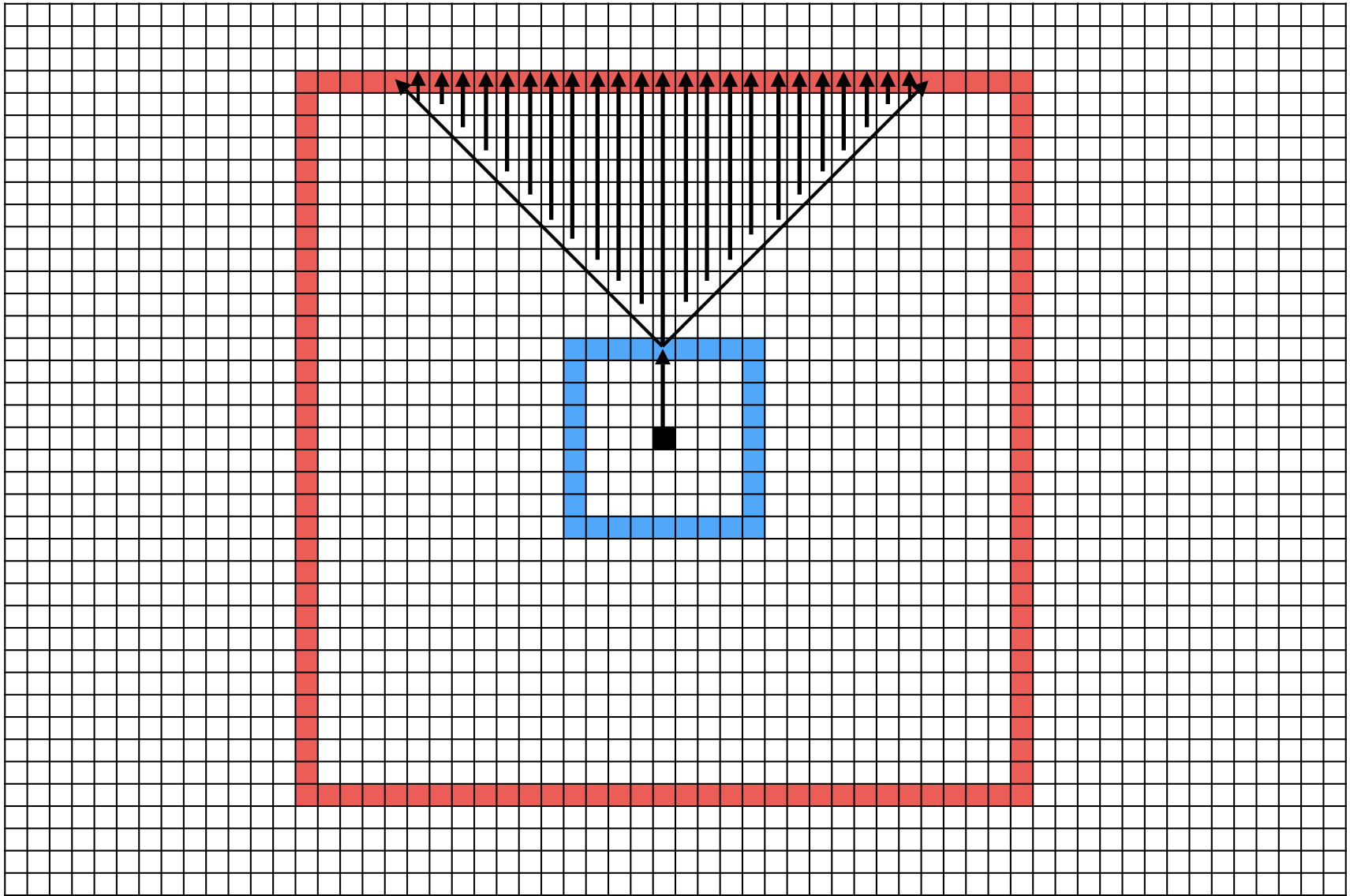


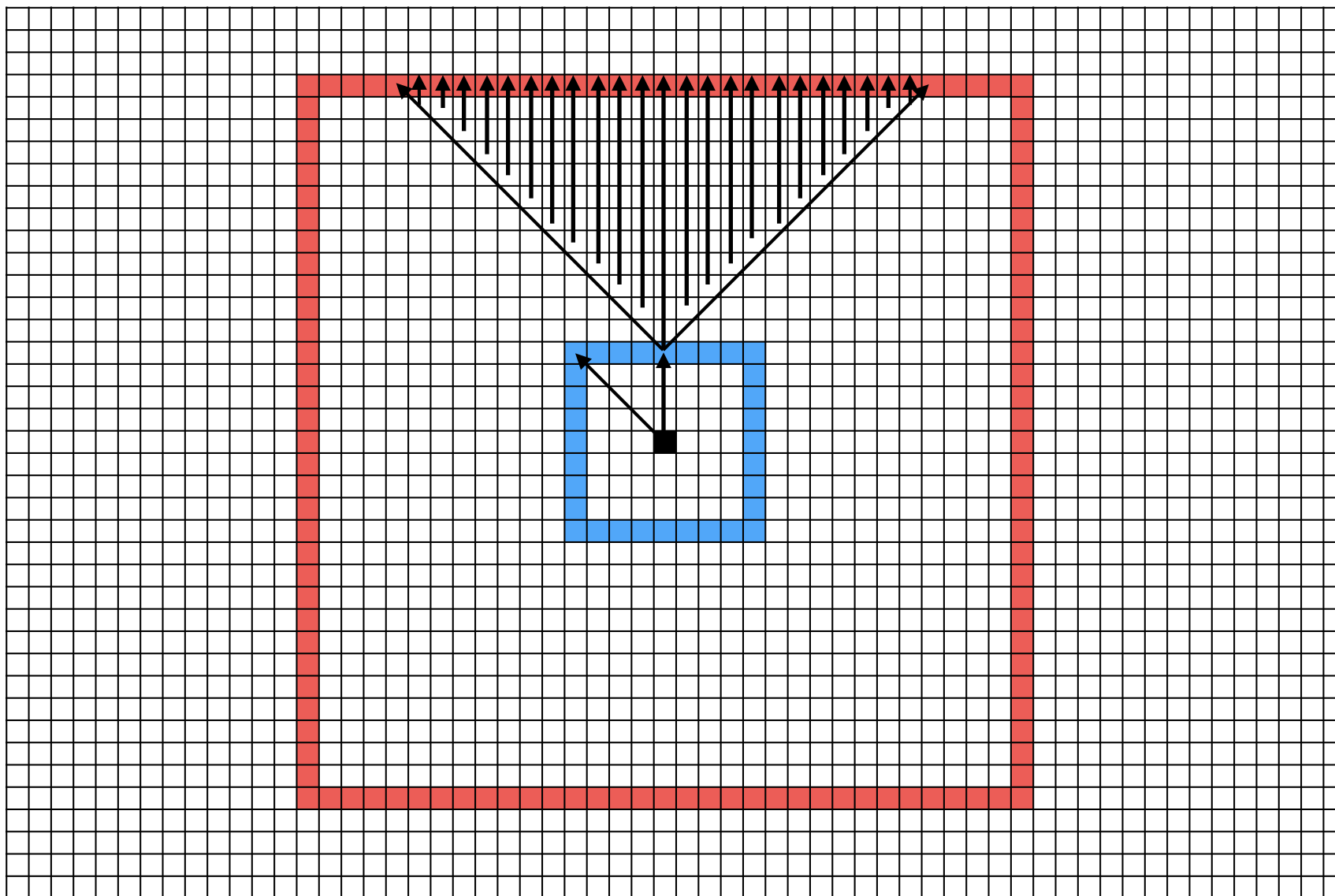


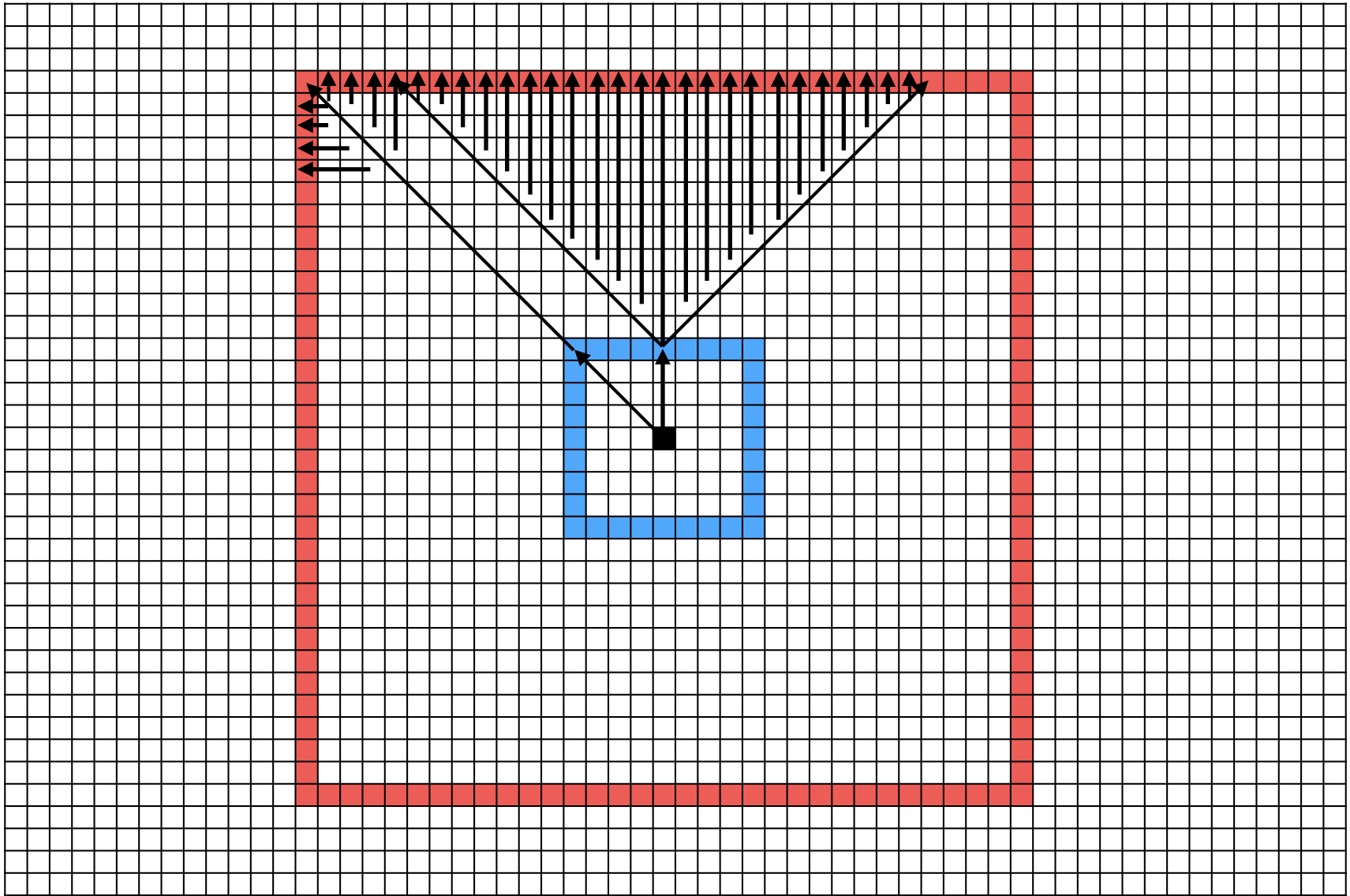


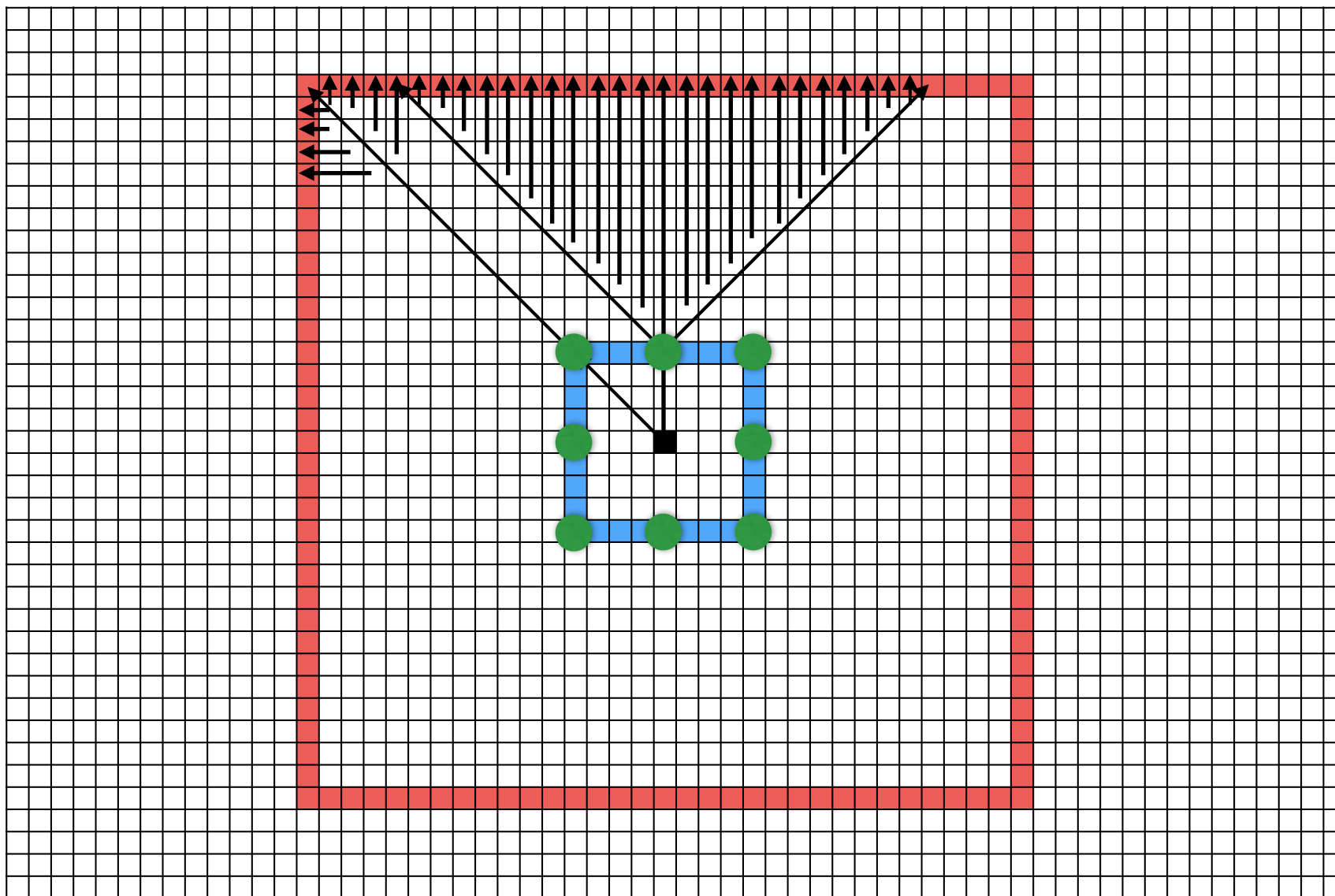
















# Cross-Fertilization

- Many road network ideas being used in grids
- Didn't originally know how to apply them properly
  - Contraction Hierarchies on Grid Graphs
    - Storandt, 2013
  - TRANSIT Routing on Video Game Maps
    - Antsfeld, Harabor, Kilby & Walsh, 2012



# Further use of contractions?

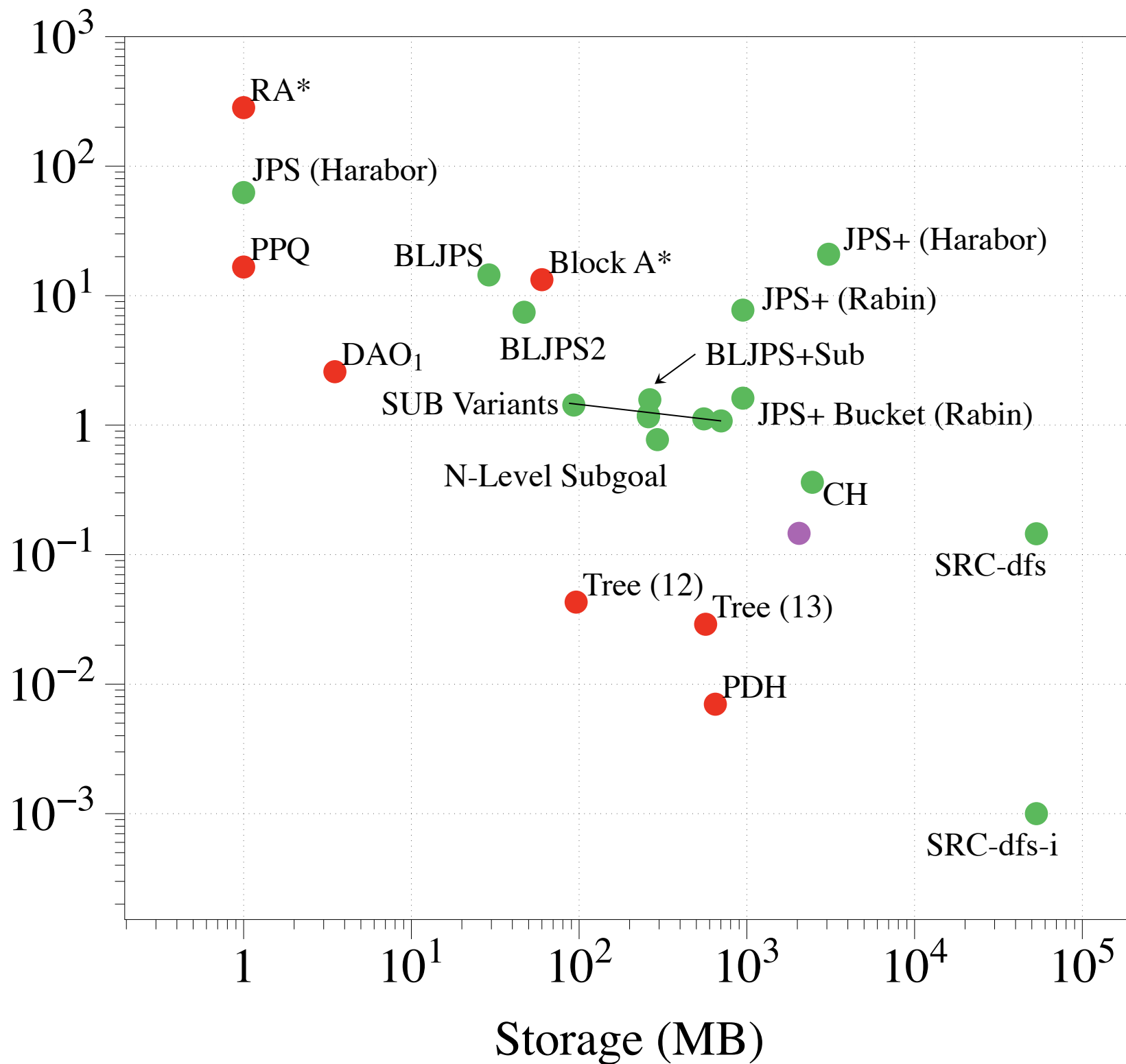
- Where else could we apply contractions?
  - Robotics?
  - 3D worlds?
  - Alternate representations? (polygons)



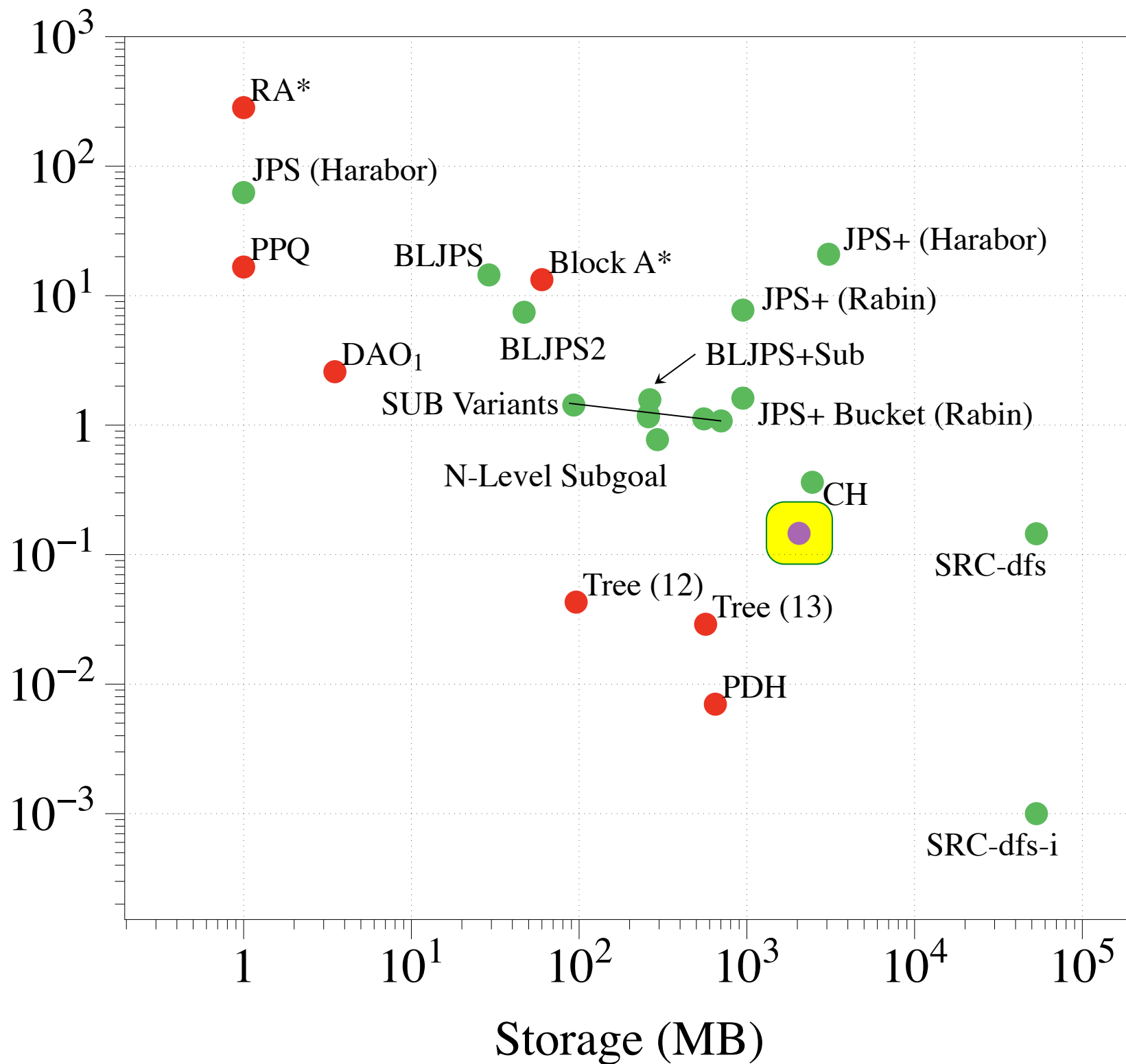
# The Future

- Have we reached the limits of our performance?
- Where is there significant room for improvement?
- Other future directions?

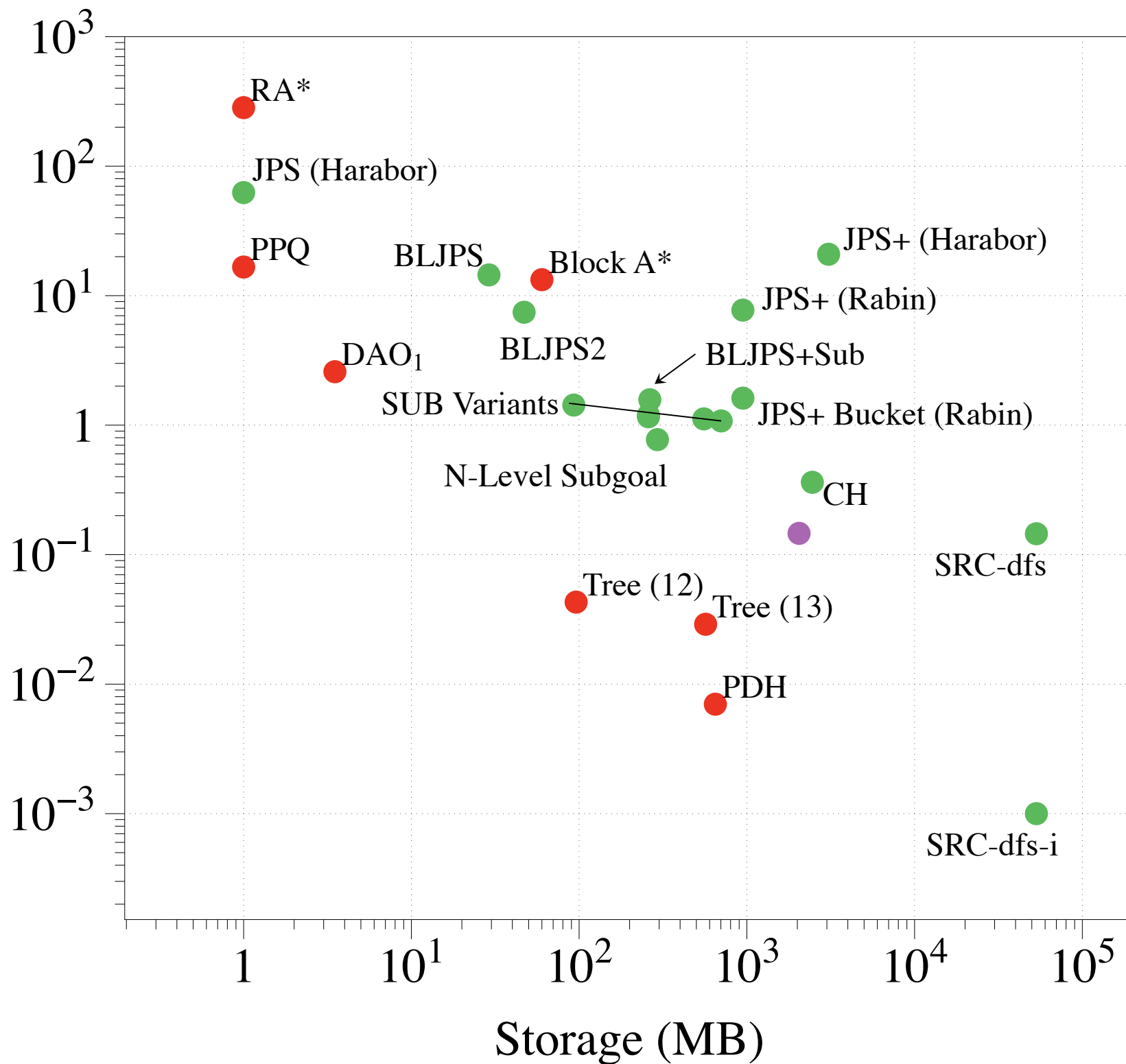
Max Time per Segment (ms)



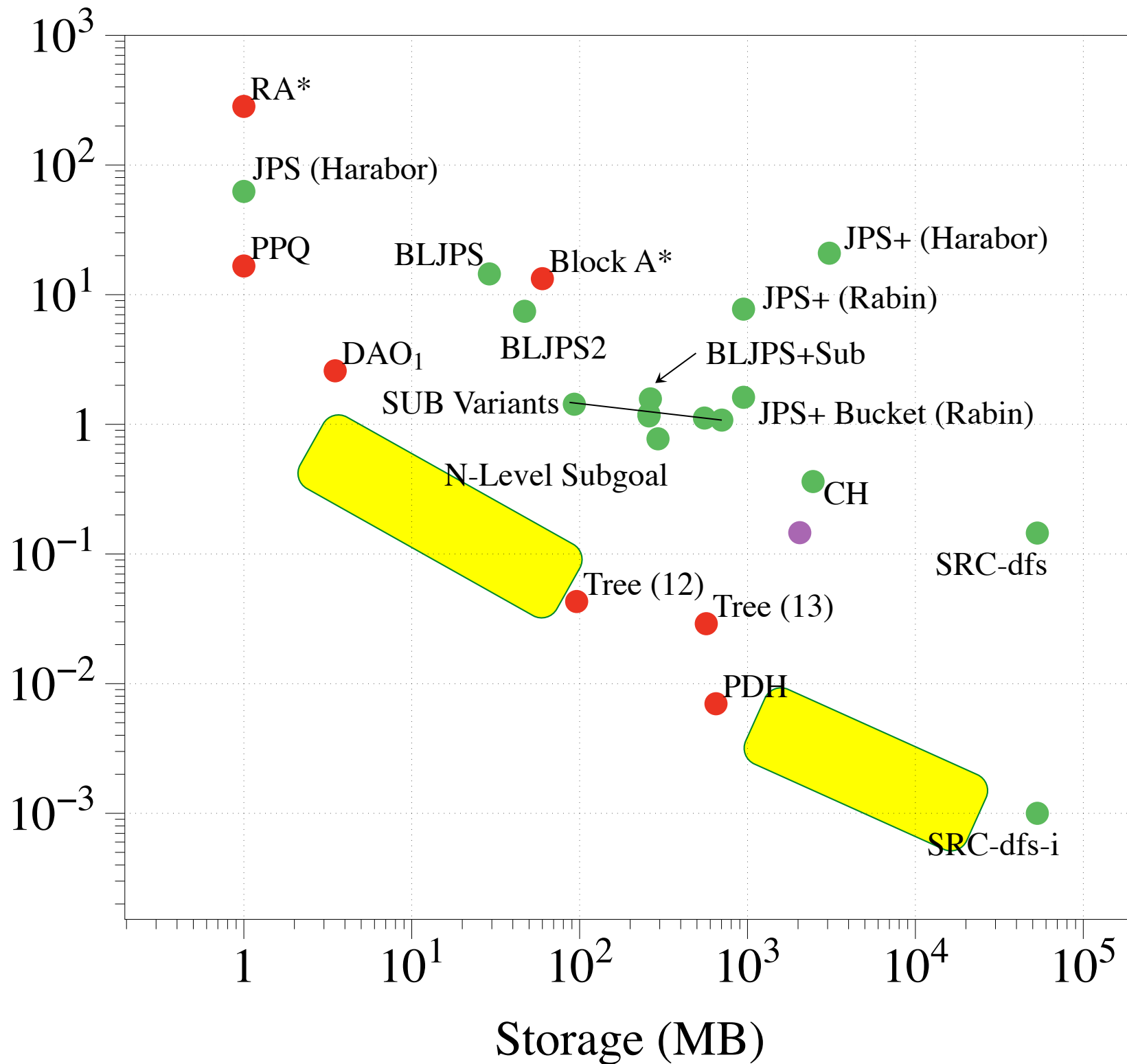
Max Time per Segment (ms)



Max Time per Segment (ms)



Max Time per Segment (ms)



# Is this the real problem?

- Dynamic world
  - Costs change, connectivity changes
- Cell costs







# Open Question

- Are we building insight?



# Open Question

- Are we building insight?
  - The benchmarks are helping drive research



# Open Question

- Are we building insight?
  - The benchmarks are helping drive research
  - Work is leading to new theoretical understanding

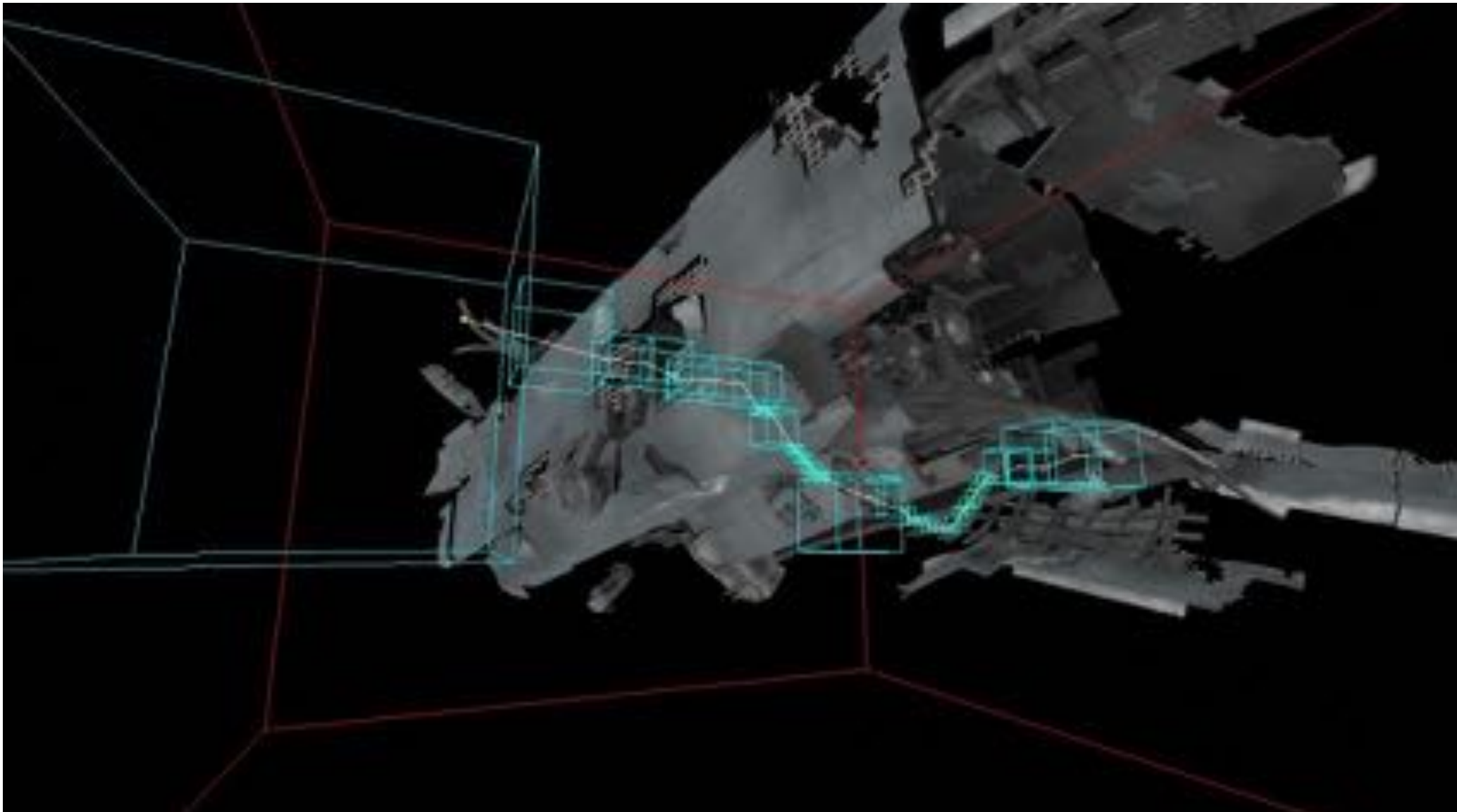


# Open Question

- Are we building insight?
  - The benchmarks are helping drive research
  - Work is leading to new theoretical understanding
- Thanks to SoCS chairs for the chance to contribute to the understanding

# One more thing!

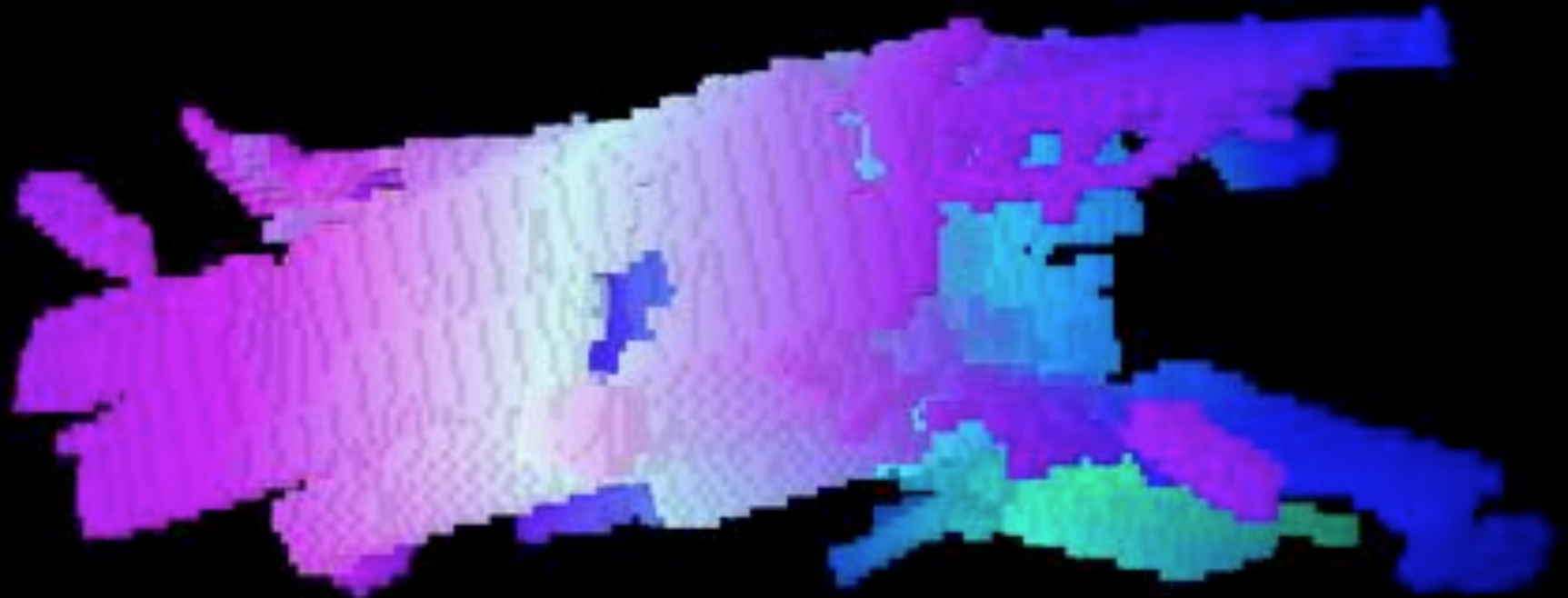
# Warframe - Digital Extremes





# New repository coming

- 3D voxel world
- Challenging new path planning domain
- Thanks to Digital Extremes and Daniel Brewer!







# Thanks

- Students/Collaborators

- Renee Jansen
- Sally Li
- Michael Buro
- Vadim Bulitko
- Robert Geisberger

- <http://movingai.com/GPPC/>



- Games Industry

- BioWare
- Digital Extremes
  - Daniel Brewer
- Troy Humphreys

- GPPC Participants

- SoCS Organizers